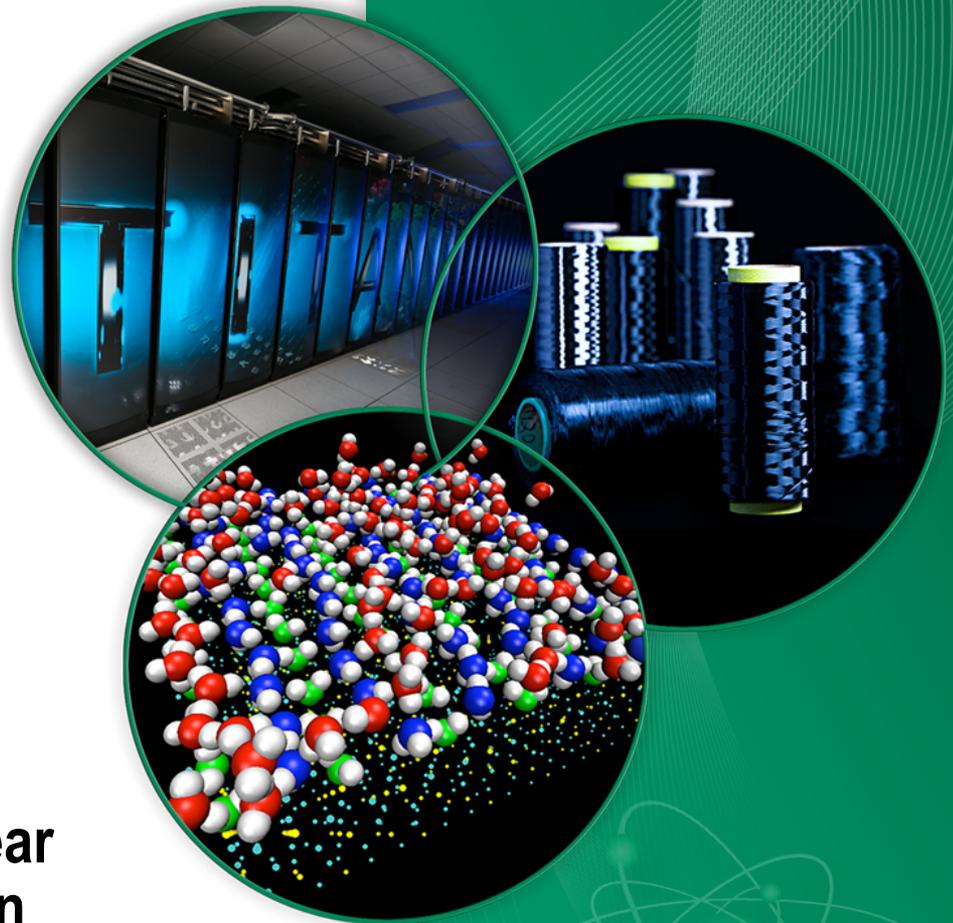


Coupled-Channel Computation of Direct Neutron Capture on Non- Spherical Nuclei

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**Fourth Joint Meeting of the Nuclear
Physics Divisions of the American
Physical Society and The Physical Society
of Japan**

Hilton Waikoloa Village, HI, October 7-11, 2014



Direct Neutron Radiative Capture (n,γ)

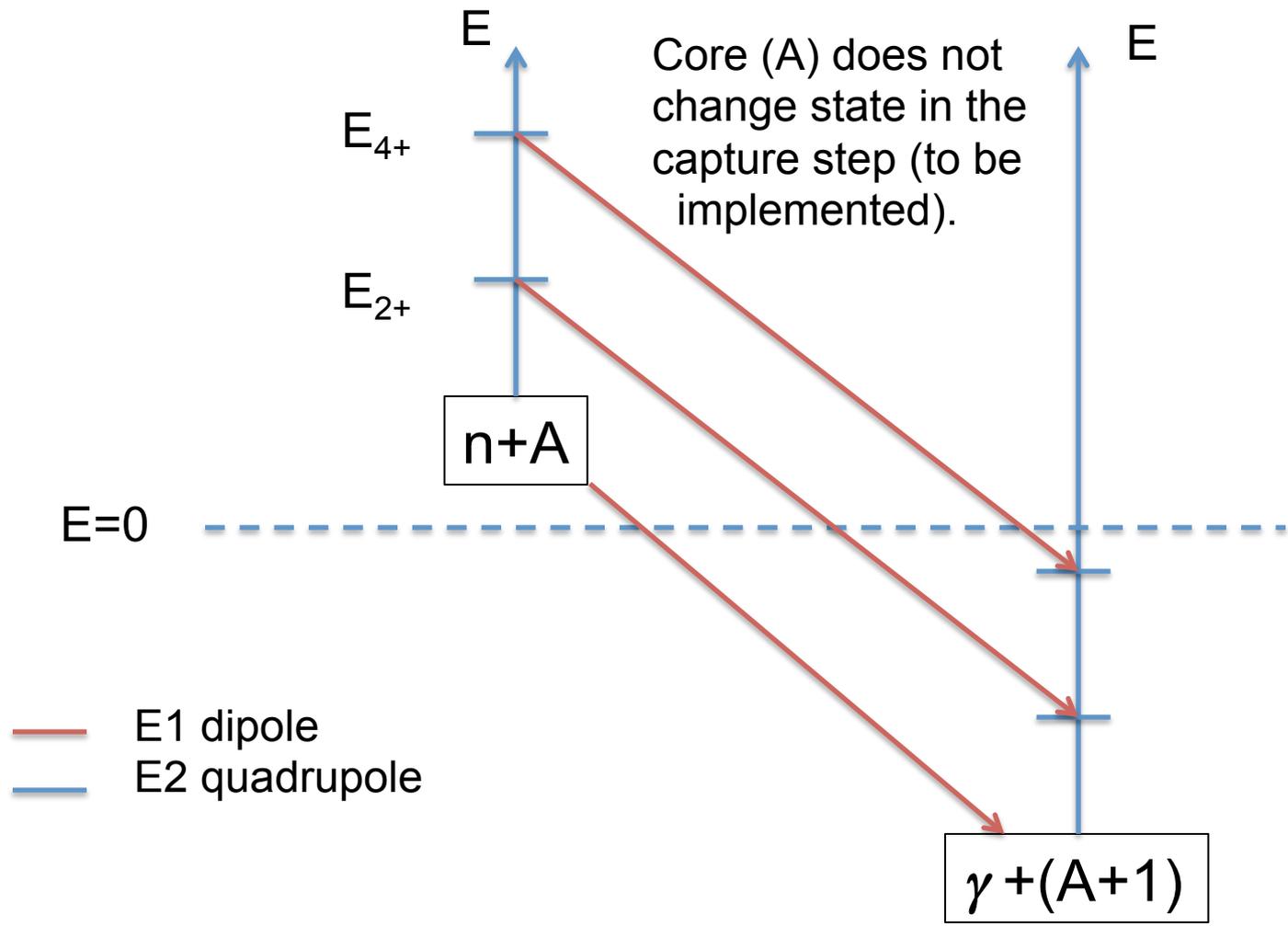
- Useful for studies of structure and reactions
- Needed for astrophysical nucleosynthesis models
 - Especially for light, and neutron rich nuclei where it may be greater than compound (statistical) neutron capture
- Needed for data evaluations of light and medium mass nuclei
- R-matrix resonance parameter fitting for resolved resonances

Direct Neutron Radiative Capture (n,γ)

- The effect of non-spherical shapes on direct capture has previously to this work been studied only in the incoming channels or the outgoing channels (bound states), but not in both
- We outline a coupled-channel approach to that self-consistently computes effects of non-spherical shape in incoming and in outgoing partitions
- We compute direct capture with and without the effect of deformation for the even calcium isotopes:
Ca-40,42,44,46,48
 - By coupling 2+ and 4+ states with non-zero deformation lengths

Schematic Coupled Channel Model

- Initial and final partitions couple to 2+, 4+ states



Advantages of Ca even mass isotopes

- Wide range of deformational strengths and 2+ excitation energies
- Thermal capture cross sections known to better than 10%, and
 - Thermal neutron: measured prompt γ -ray energies and branching ratios
- Mostly E1 capture: 82%, 93% 98% 96% 100% for Ca-40,42,44,46,68
 - Good for testing models of direct capture
- Mostly direct capture at the thermal neutron energy
 - Compound resonant capture measured but small.
 - Its contribution can be computed via R-matrix formalism
 - Small fraction of s-wave neutron E1 capture is compound resonant

Theory of Direct Capture

- Siegert's theorem (1937):
 - Expresses EM operator in terms of charge density form
- Coupled channels (FRESCO)
 - I.J. Thompson, F.M. Nunes, “Nuclear Reactions for Astrophysics”, (2009)
- Core excitations in incoming (n +core) or outgoing (γ +(n +core)) partitions:
 - 2+, 4+ state of a rotational band with deformation lengths from TALYS
 - Core remains in the same state (0+,2+,or 4+) during the capture step

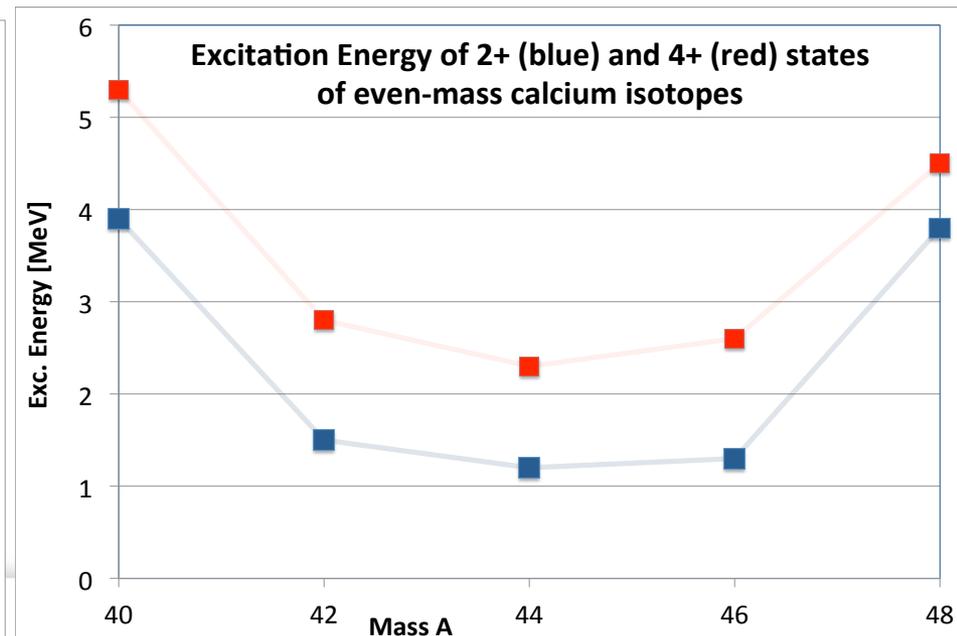
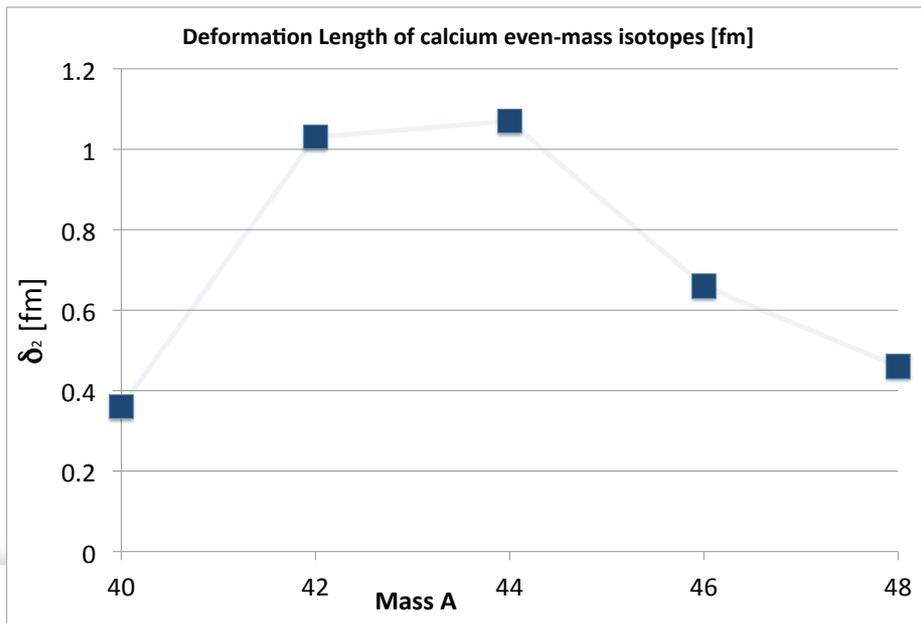
$$\mathbf{T}_{\gamma\alpha_i} = -\frac{1}{k} \frac{k}{\hbar c} \frac{q}{i} \sqrt{\frac{8\pi\hbar c(J+1)}{Jk}} \sum_{\alpha} \langle i^J F_J \phi_b | \psi_{\alpha\alpha_i} \rangle \quad (4.7.16)$$

$$\sigma_{\text{cap}}^J = \frac{4\pi}{k_i^2} \frac{1}{(2I_p+1)(2I_t+1)} \frac{c}{v_i} \sum_{J_{\text{tot}}} (2J_{\text{tot}}+1) |\mathbf{T}_{\gamma\alpha_i}^{J_{\text{tot}}\pi}|^2. \quad (4.7.20)$$

- Later we may implement core transitions in the capture step itself

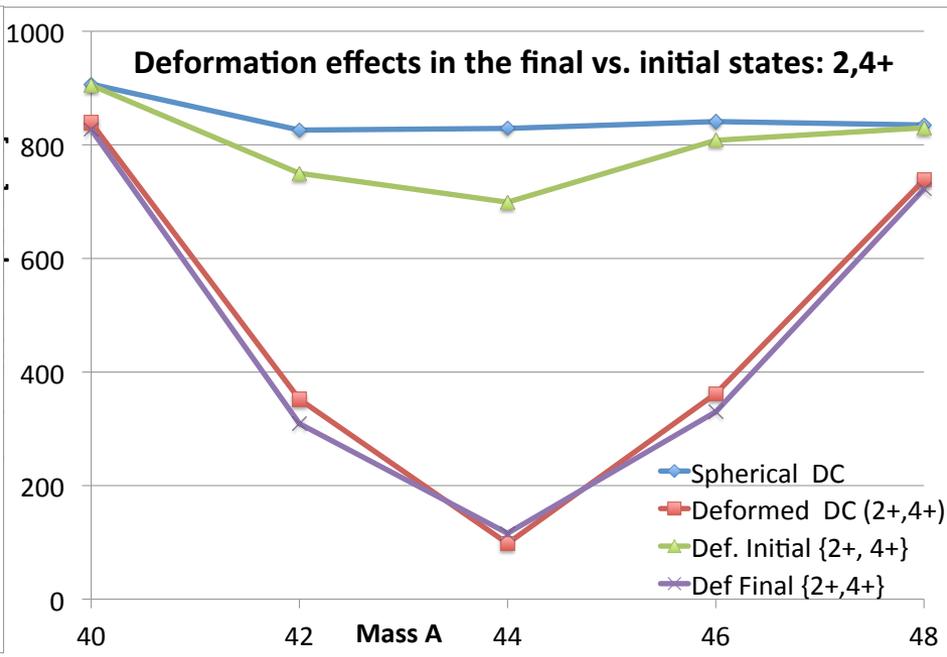
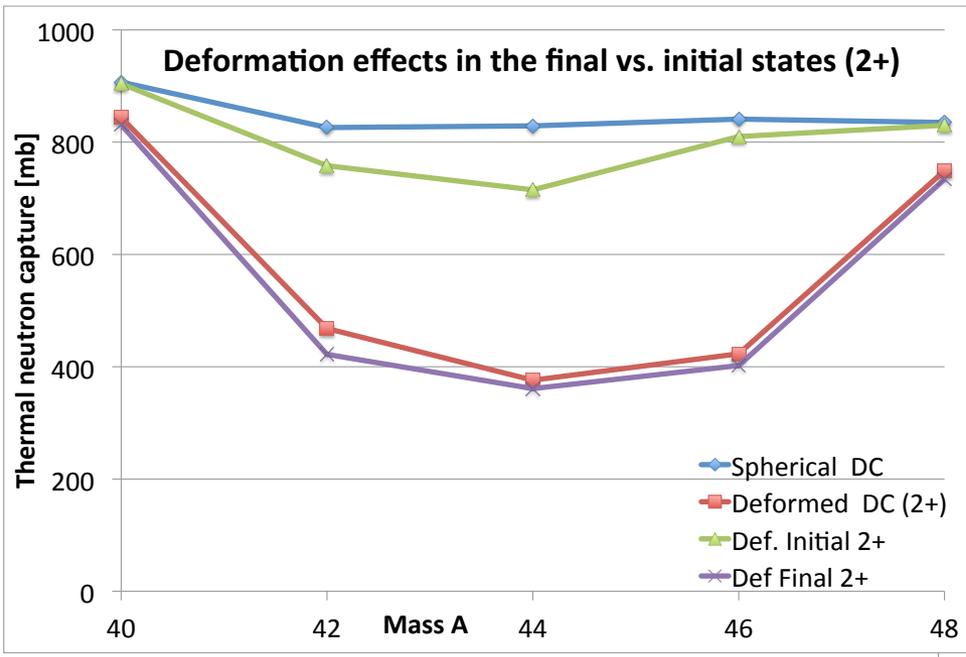
FRESCO Calculation Input

- Koning-Delaroche complex optical potential at $E=0$ MeV
 - Good for thermal neutron capture and sufficient for low-energy
- Deformation length parameters from TALYS database from $B(E2)$
- Compute direct capture for Ca-40,42,44,46,48
 - No deformation; $2+$; $\{2+,4\}$, in initial and final channels
 - Deformation $2+$; $\{2+,4+\}$; in initial channel only, or final channel only



Deformation in initial vs. final states

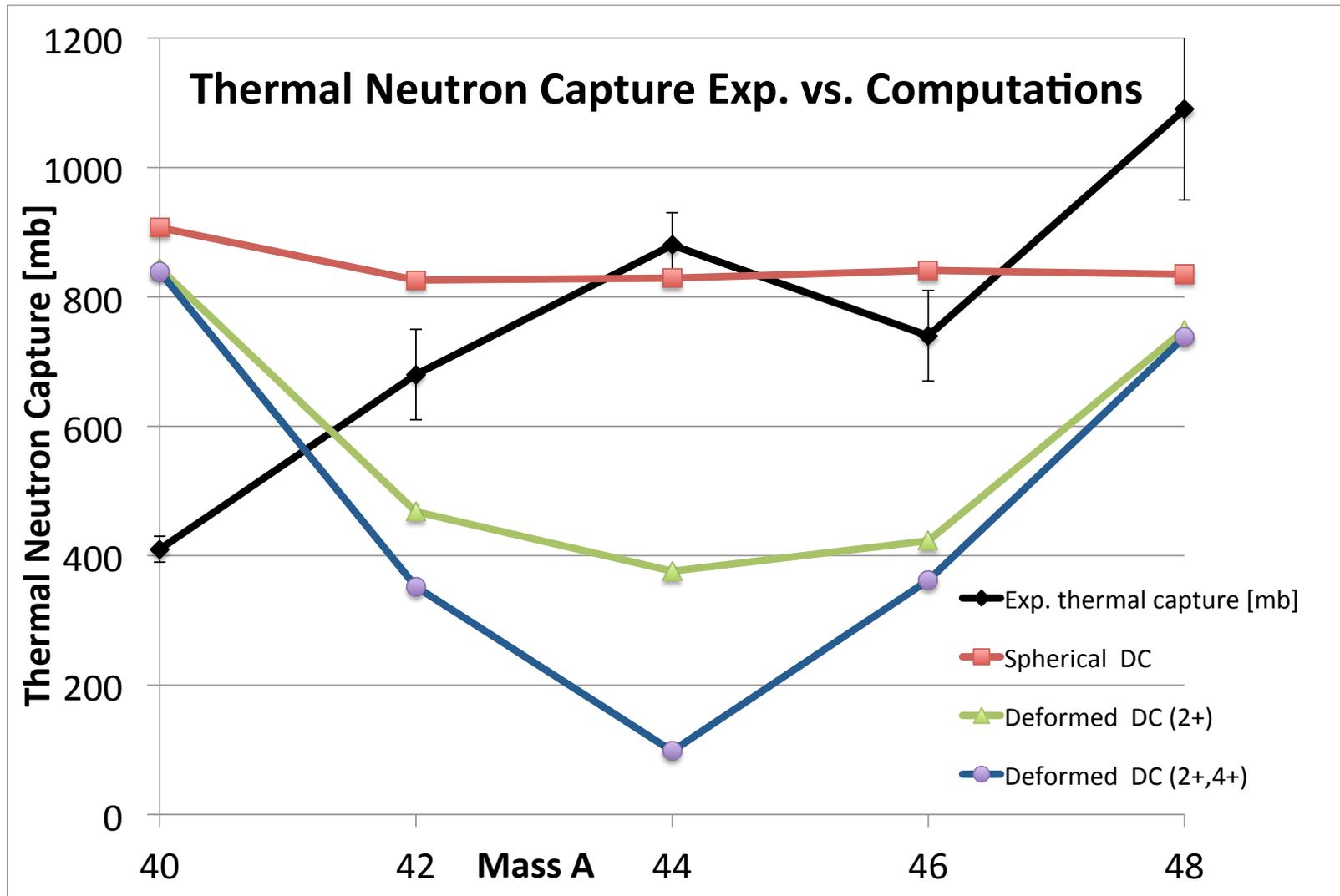
- The effect of deformation in the final neutron bound state is greater than in the initial neutron scattering state
 - Assumed by Boison and Jang, Nucl. Phys. A189 (1972) 334-352
 - Using bound spectroscopic factors (SF) from Kahane et al. (1987)
 - Plots below are for thermal neutron capture



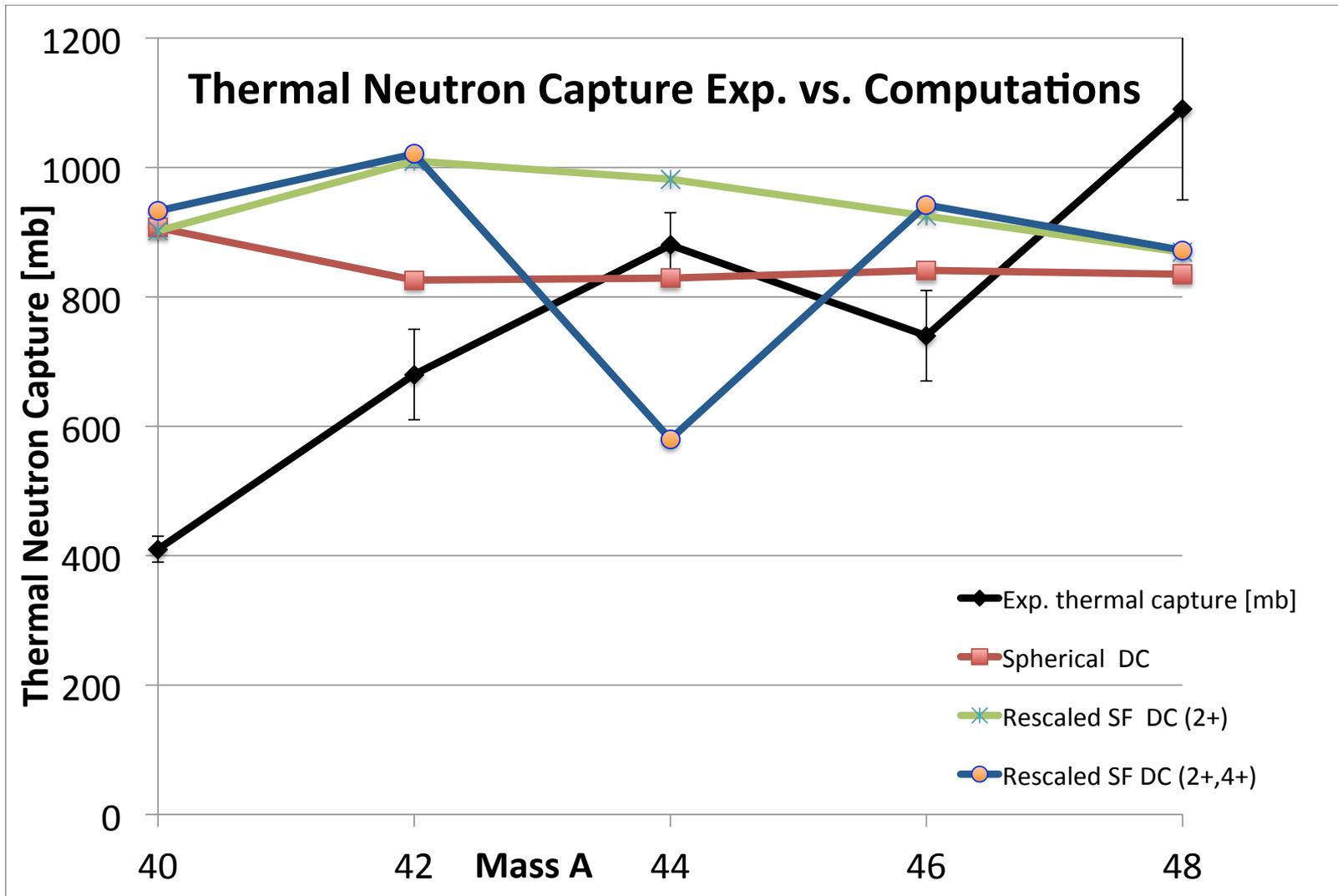
Experimental determination of SF's

- SF were determined by fitting (d,p) cross sections w/o deformation (spherical potentials)
- But, in bound states, the fraction of the core in its GS diminishes with coupling to 2+ and 4+ core states. This upsets (d,p) fits.
- We compensated, *approximately*, by rescaling overall SF in order to make the GS component the same as was fitted before
- Most of the direct capture occurs into the core in the GS, so a decrease in the fraction of the core in the GS decreases capture
- Later, should revisit (d,p) reactions with couplings to (2+, 4+) states

Thermal capture results vs. data

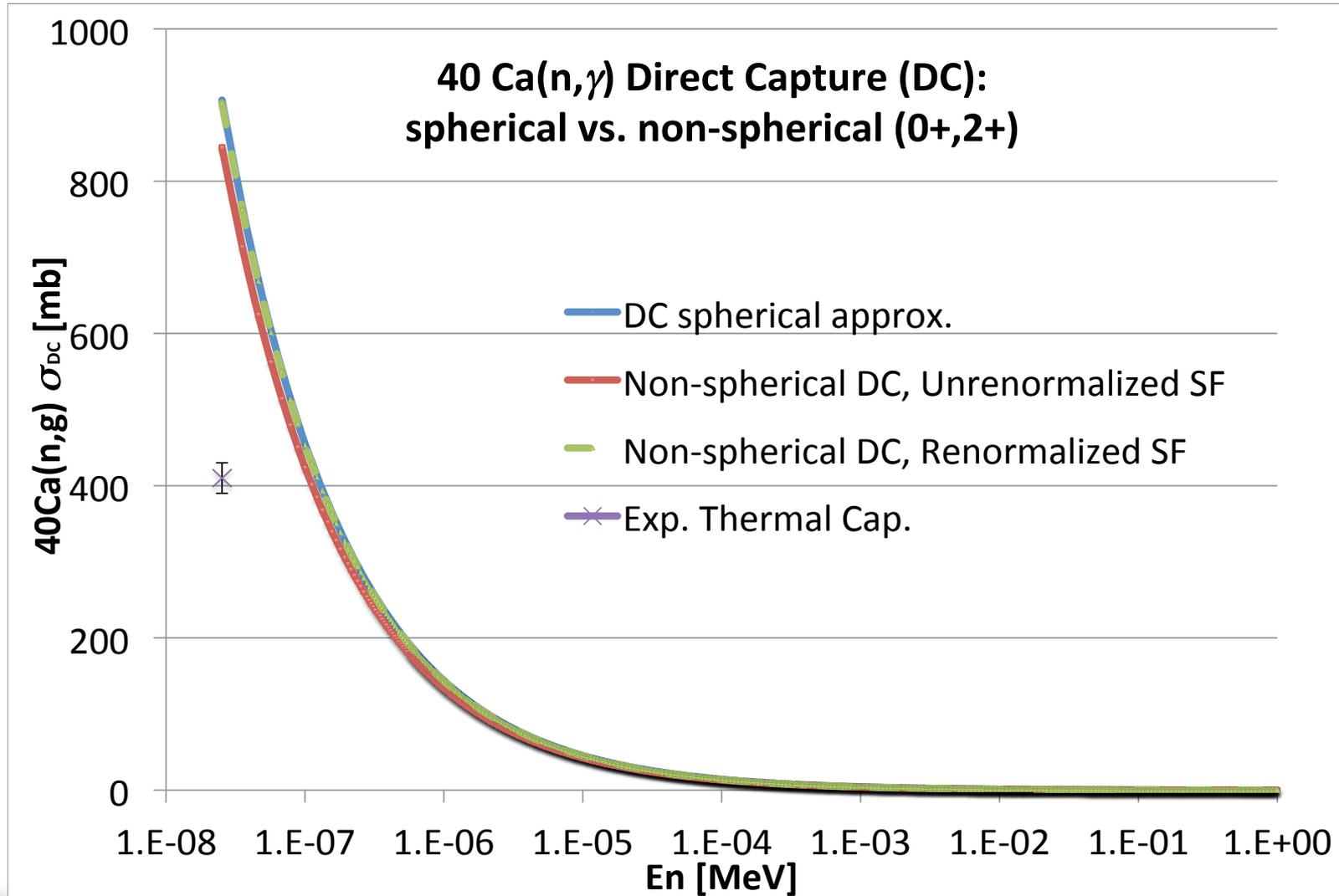


Thermal capture results vs. data



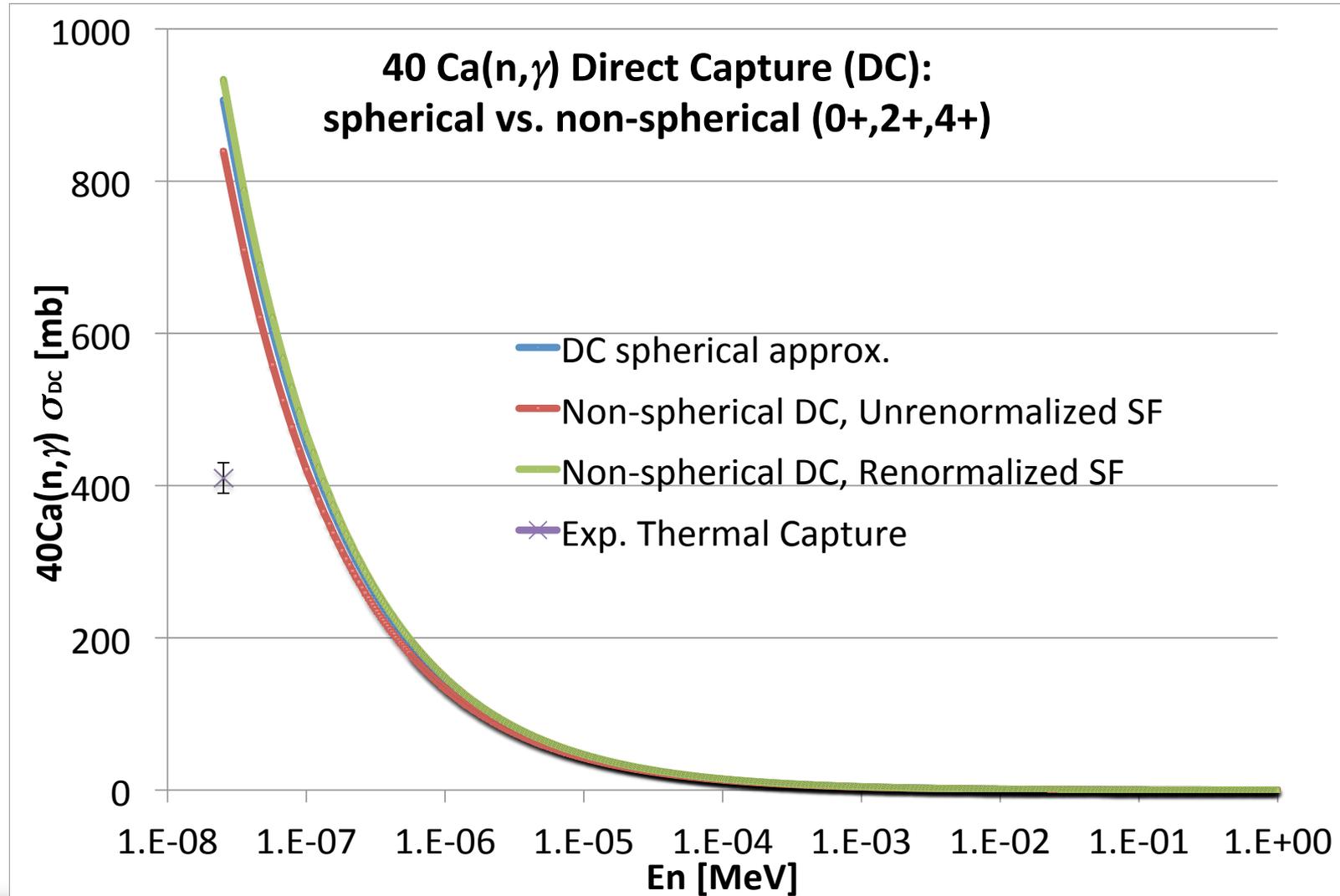
$^{40}\text{Ca}(n,g)$ spherical vs. CC ($0+,2+$)

- Computations of capture over-predict thermal cap. by a factor of 2



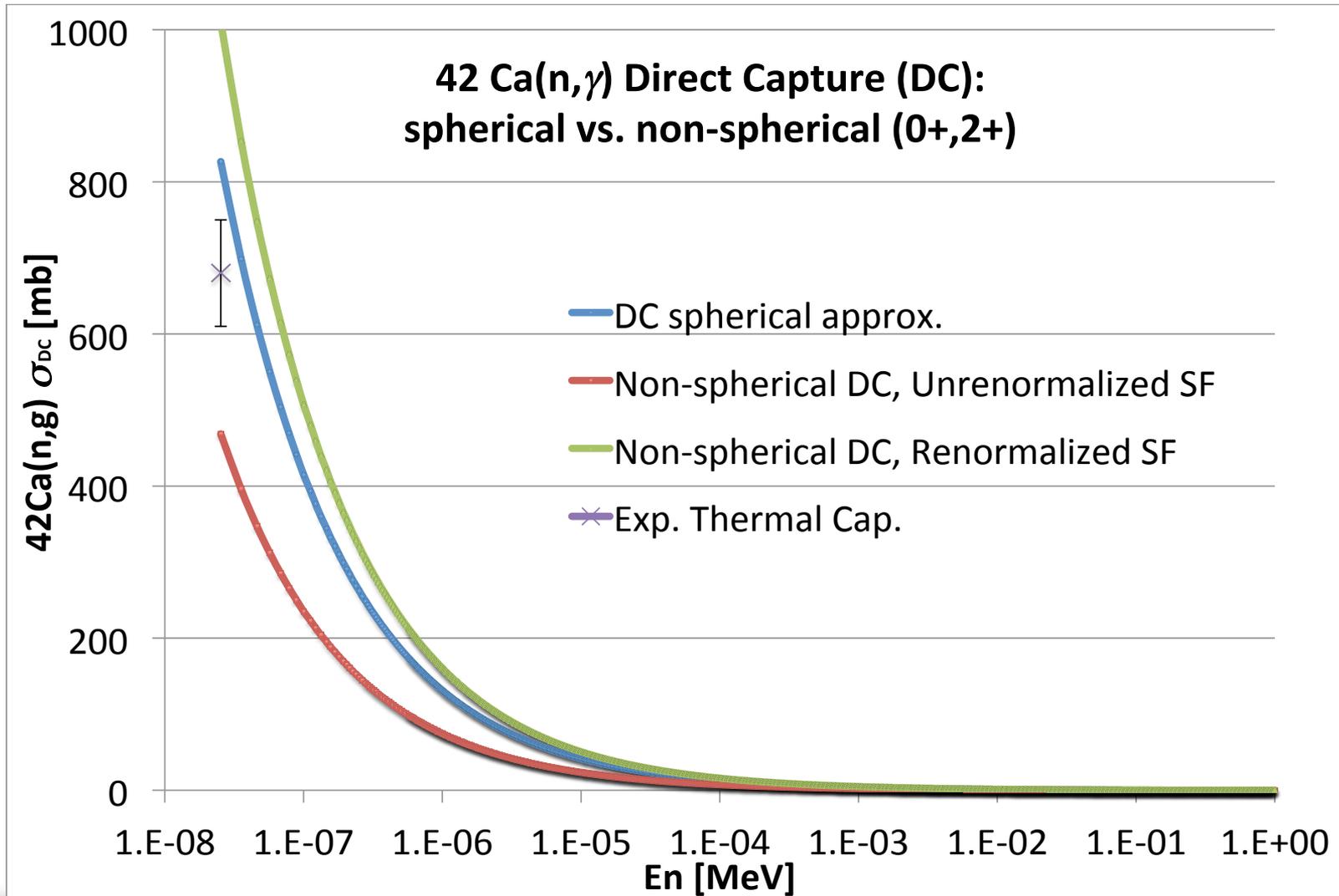
$^{40}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

- Computations of capture over-predict thermal cap. by a factor of 2



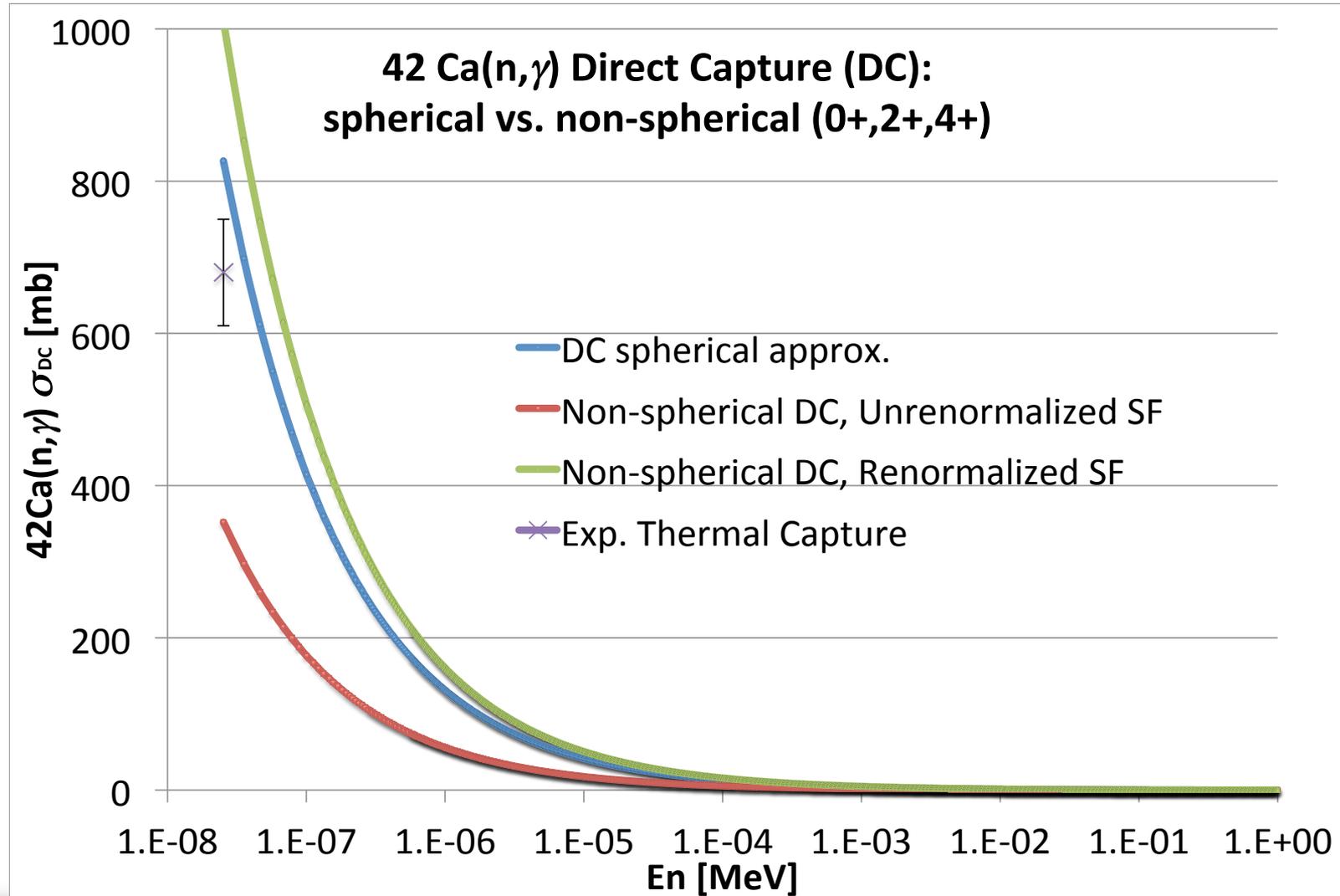
$^{42}\text{Ca}(n,\gamma)$ spherical vs. CC (0+,2+)

- DC with rescaled SF is larger than thermal capture expt.



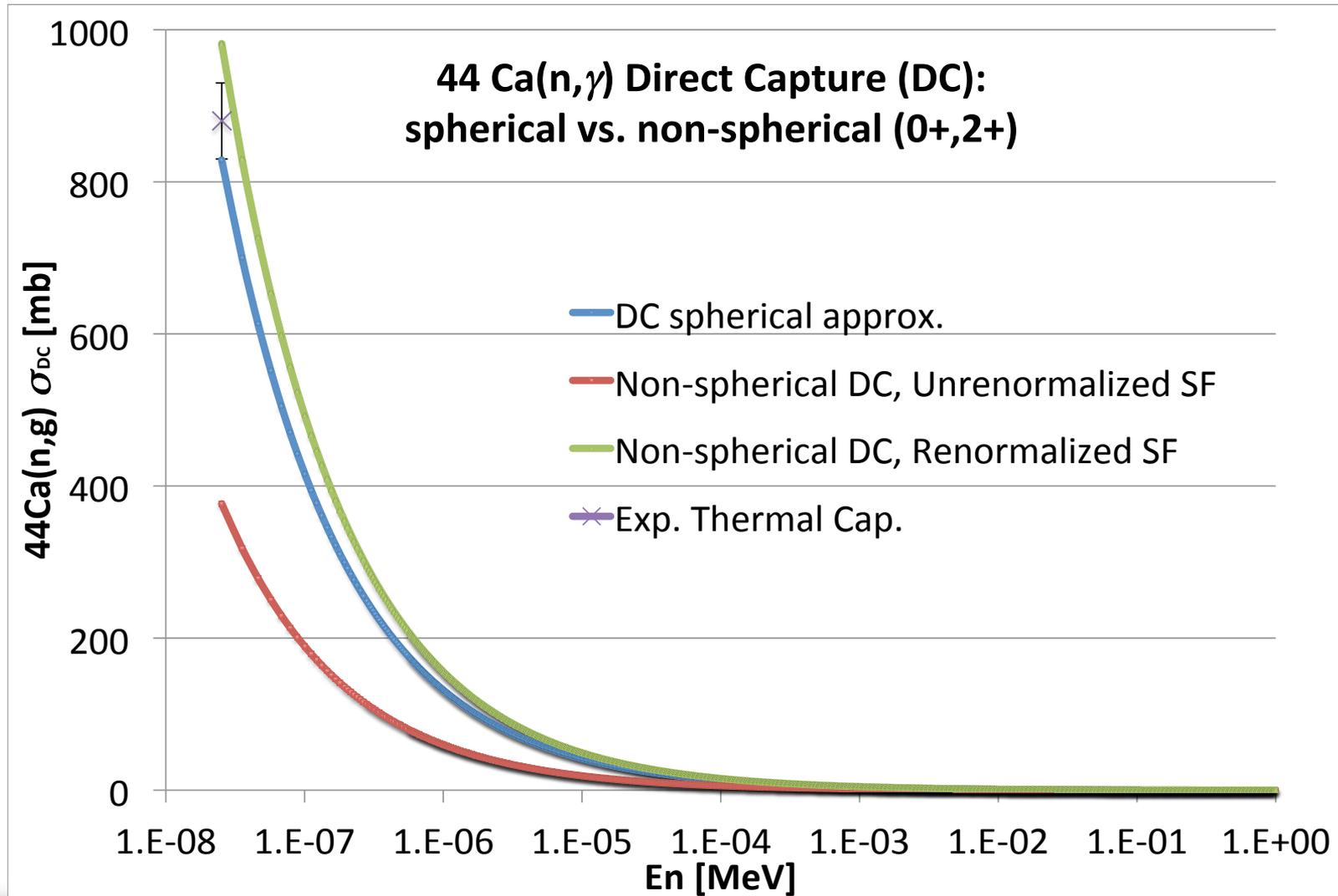
$^{42}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

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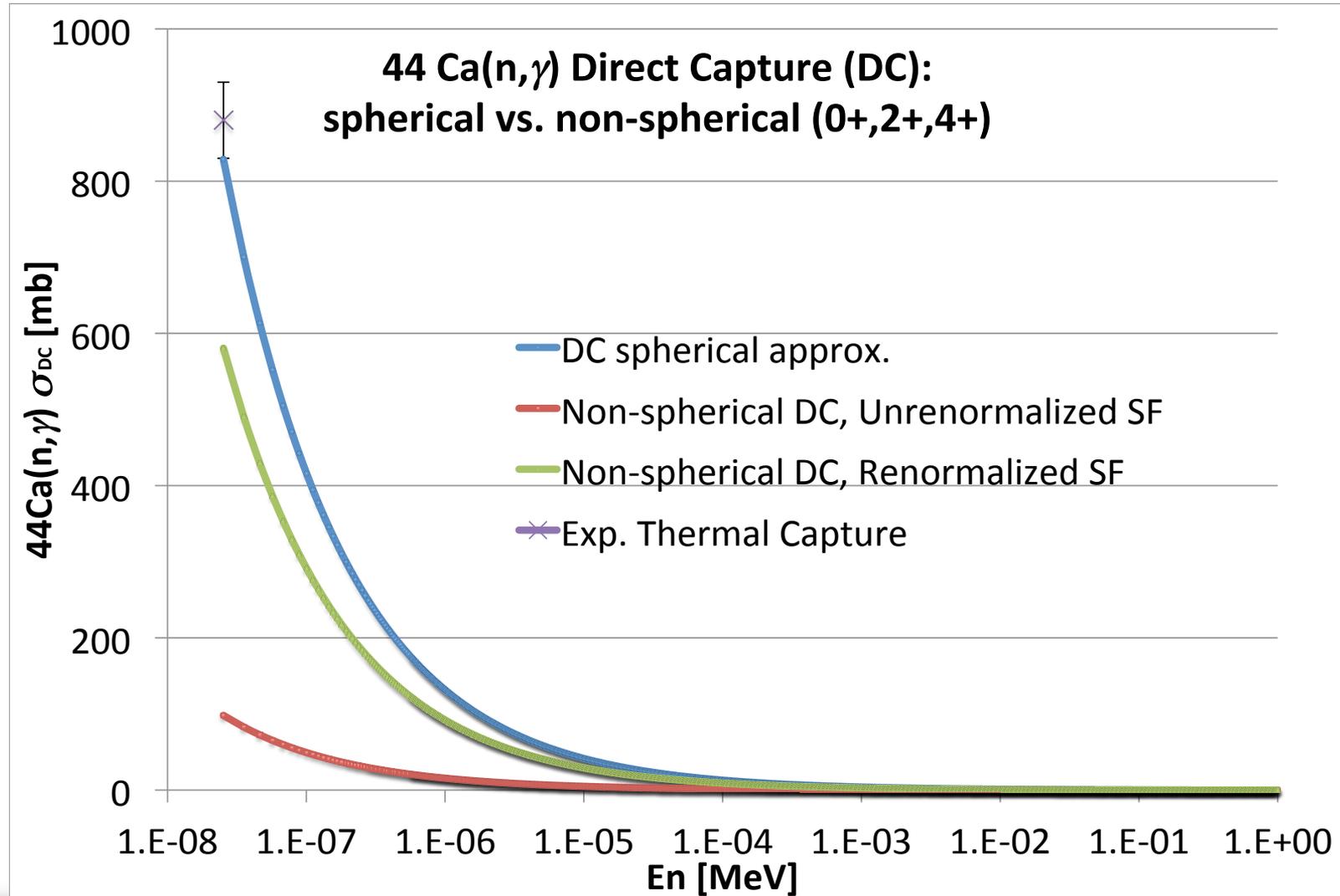
$^{44}\text{Ca}(n,g)$ spherical vs. CC (0+,2+)

- Renormalization of SF yields capture compatible with experiment



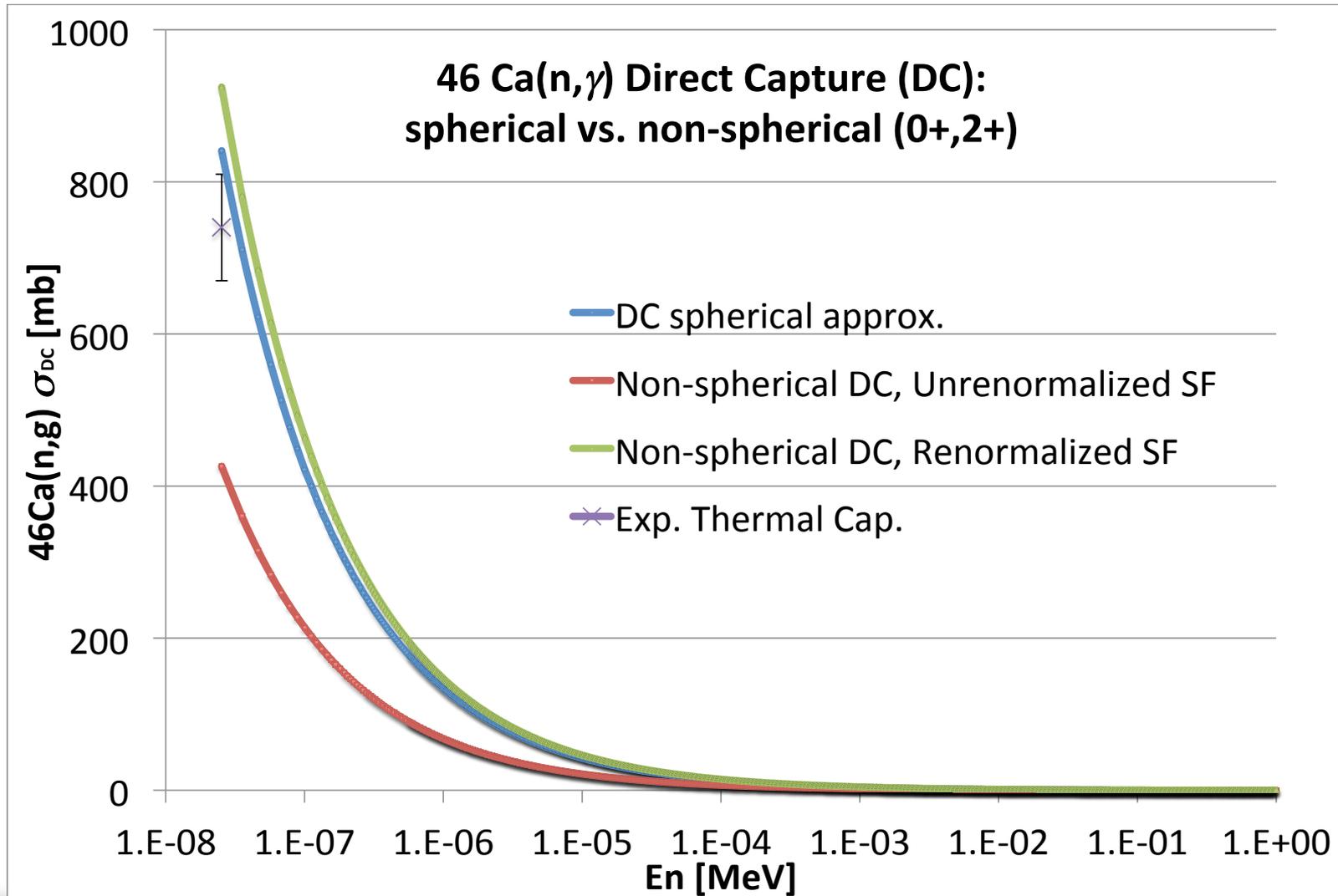
$^{44}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

- Renormalization of SF yields thermal capture smaller than expt.



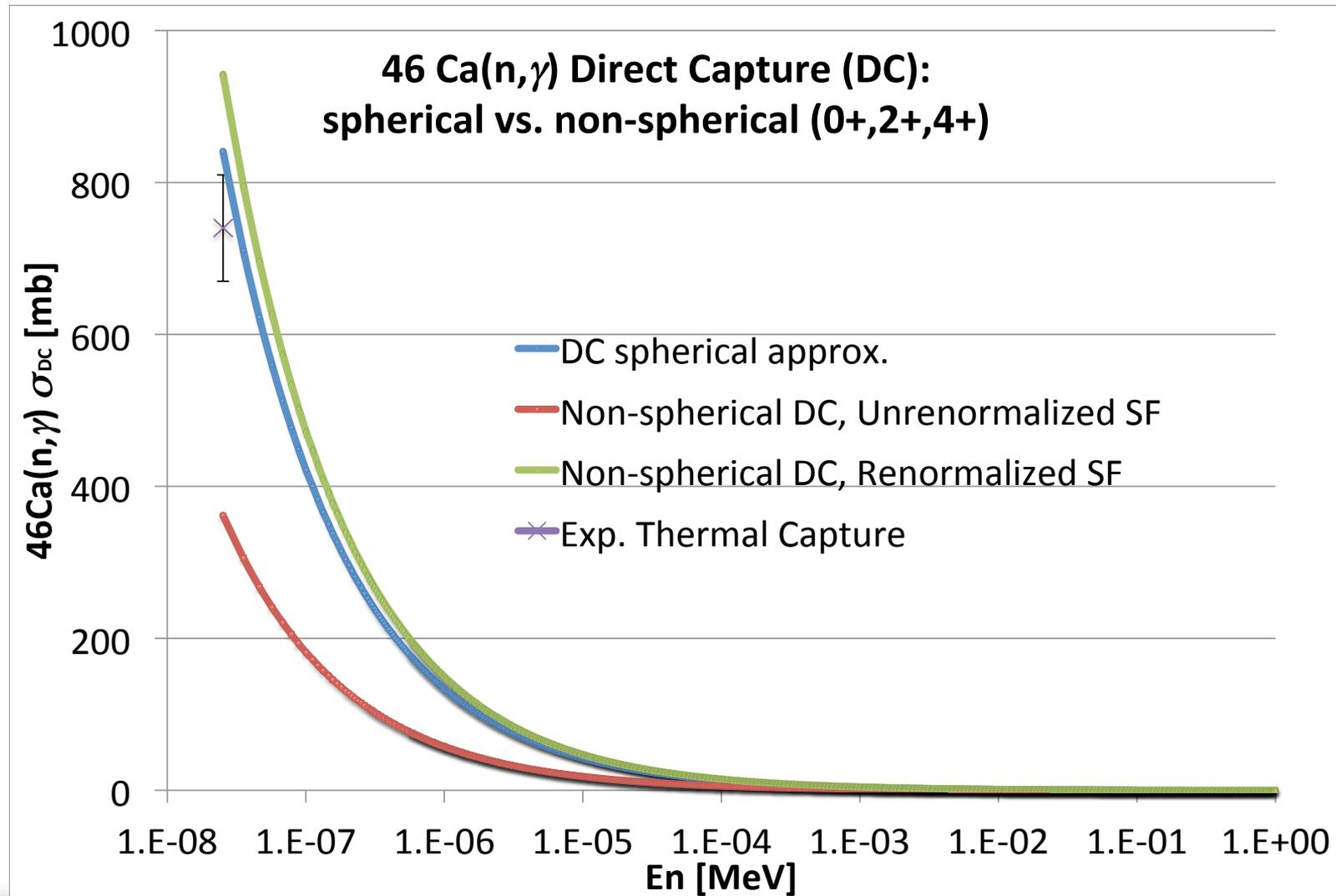
$^{46}\text{Ca}(n,g)$ spherical vs. CC (0+,2+)

- Rescaling of SF yields thermal capture larger than expt.



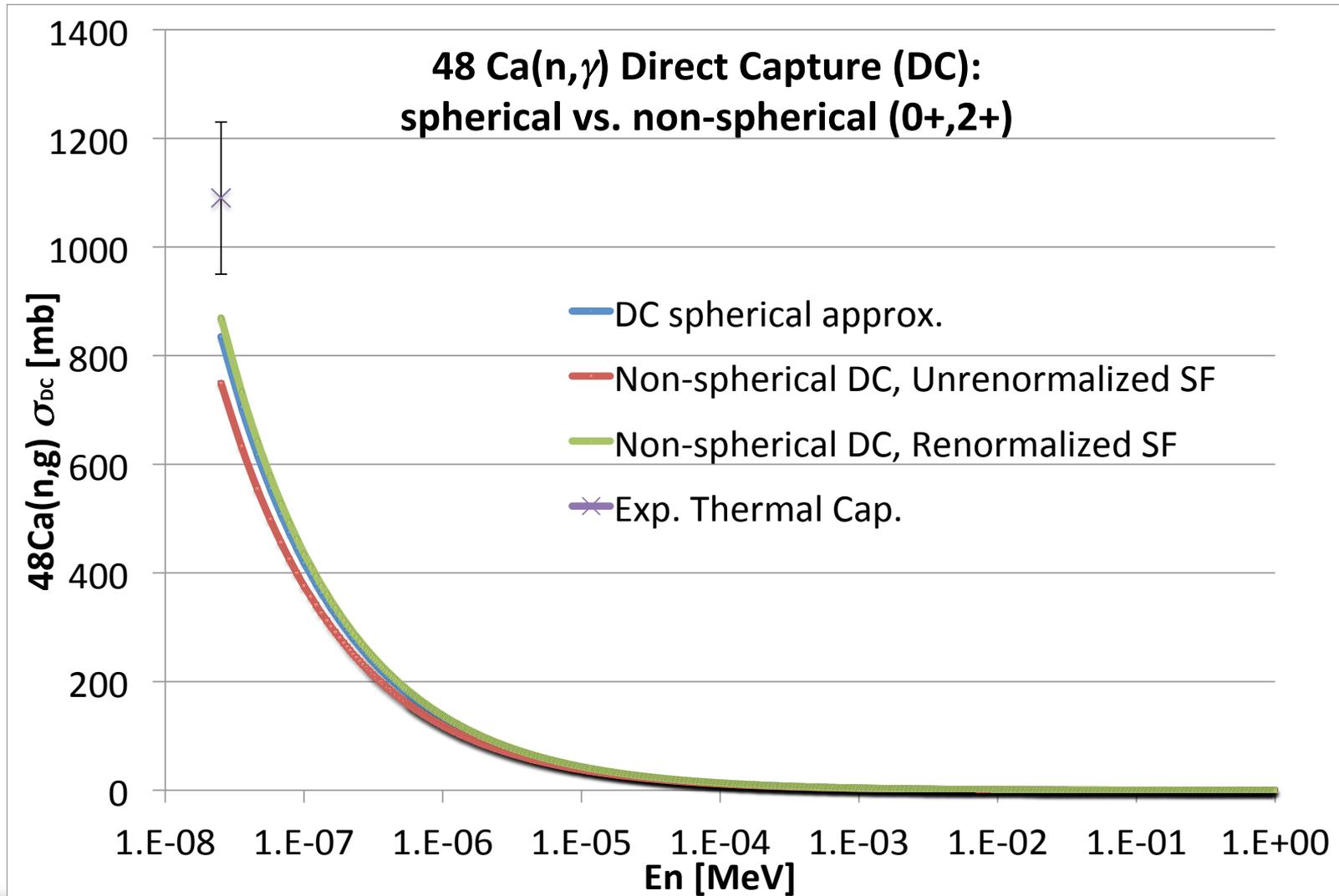
$^{46}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

- Rescaling of SF yields thermal capture larger than experiment



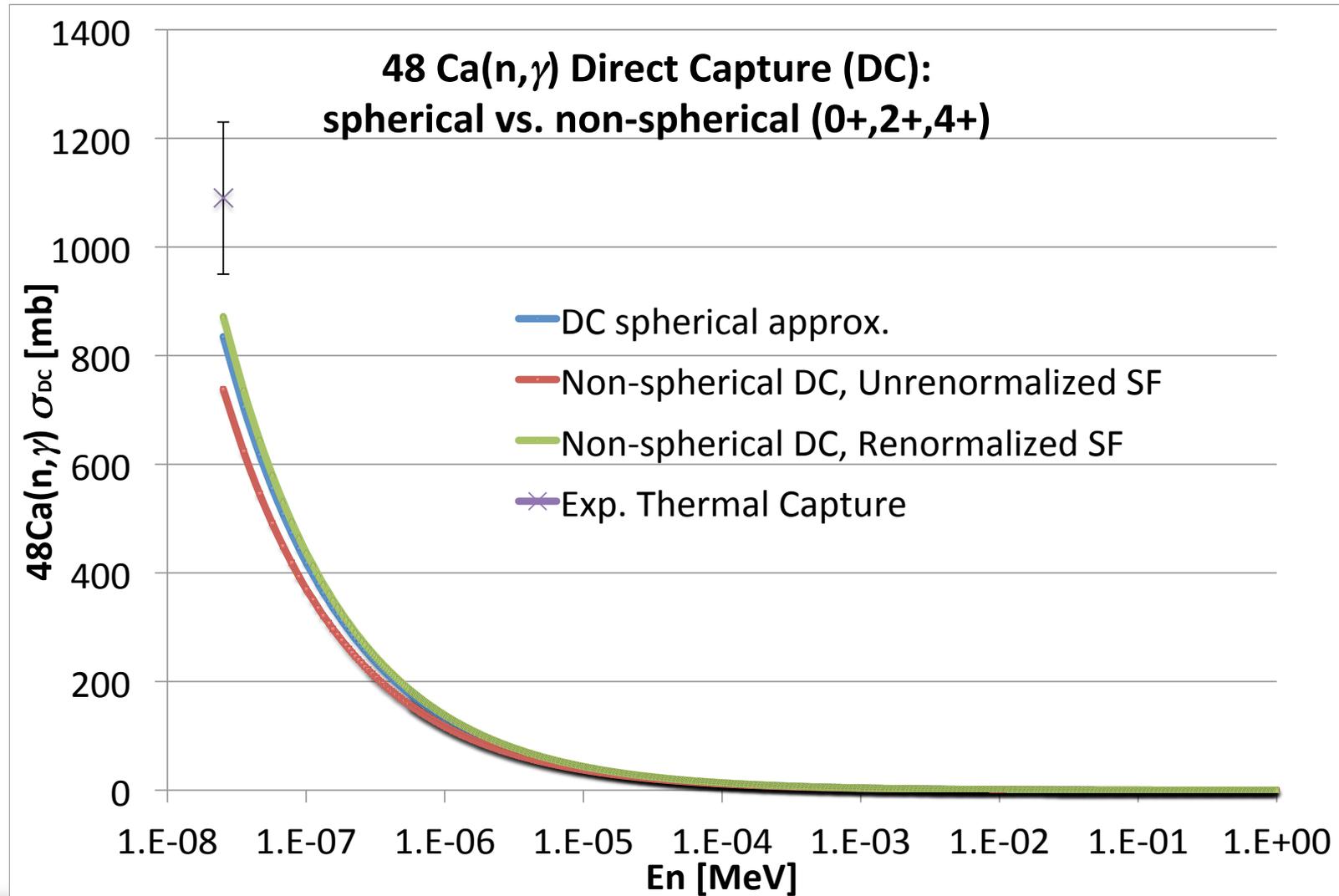
$^{48}\text{Ca}(n,g)$ spherical vs. CC ($0+,2+$)

- All methods yield thermal capture cross sections smaller than expt.



$^{48}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

- All methods yield thermal capture cross sections smaller than expt.



Conclusions

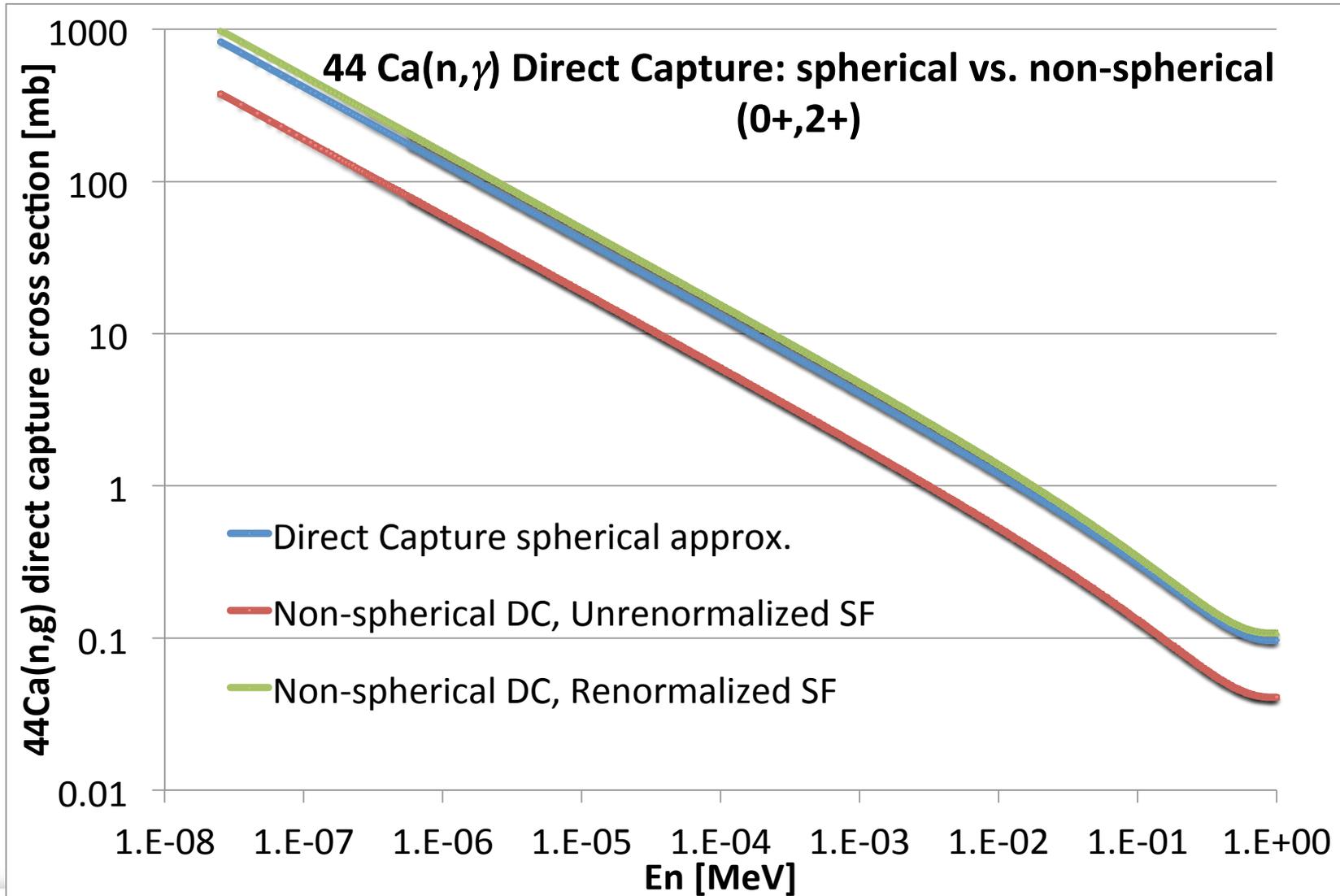
- These quadrupole-core couplings have strong effects on capture away from closed shell.
 - Even if spherical models come close to the data
- Effect of non-spherical shapes are larger for final (bound) state
 - Bound states become fractionated among core states (0^+ , 2^+ , 4^+)
 - This fractionation diminishes fraction of the core in GS and direct capture
- To restore the original experimental spectroscopic amplitudes some renormalization of bound states may be necessary

Future research (TORUS Collaboration)

- Allow for core (de-)excitations in the capture step itself
 - Findings may yield insight on the SF renormalization method
- Revisit (d,p) reactions with couplings to (2^+ , 4^+) states
 - It may affect values and interpretation of SF

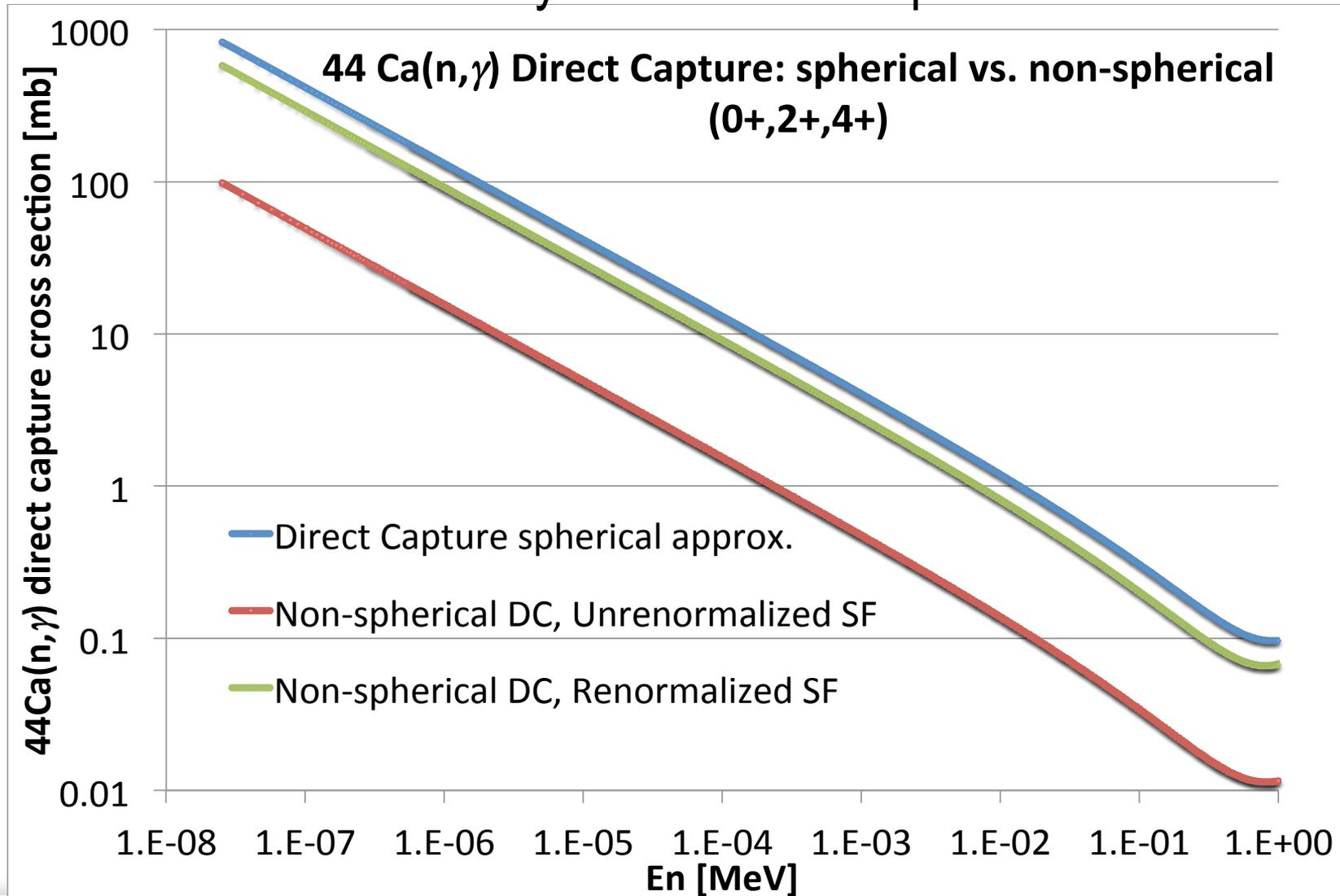
$^{44}\text{Ca}(n,\gamma)$ spherical vs. CC (0+,2+)

- Renormalization of SF yields capture compatible with experiment



$^{44}\text{Ca}(n,\gamma)$ spherical vs. CC ($0+,2+,4+$)

- Renormalization of SF yields thermal capture too small



$^{44}\text{Ca}(n,\gamma)$ spherical vs. CC ($0^+,2^+,4^+$)

- Renormalization of SF yields thermal capture too small

