

# Microscopic description of heavy ions collisions around the barrier

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# Plan

## Introduction:

*Why a microscopic approach ?*

### **I) Time-Dependent Hartree-Fock (TDHF)**

- *formalism*
- *practical aspects*

### **II) Applications to fusion**

- *light and medium-heavy systems*
- *fusion hindrance in heavy systems*
- *collision time of  $^{238}\text{U}+^{238}\text{U}$*

## Conclusions and perspectives

# Introduction: *Why a microscopic approach ?*

**Interface between structure and reactions**  
*same formalism for both*

**Predictive power**  
*heavy systems, exotic nuclei, neutron stars...*

**All type of reactions between two nuclei**  
*fusion, transfer, inelastic scattering...*

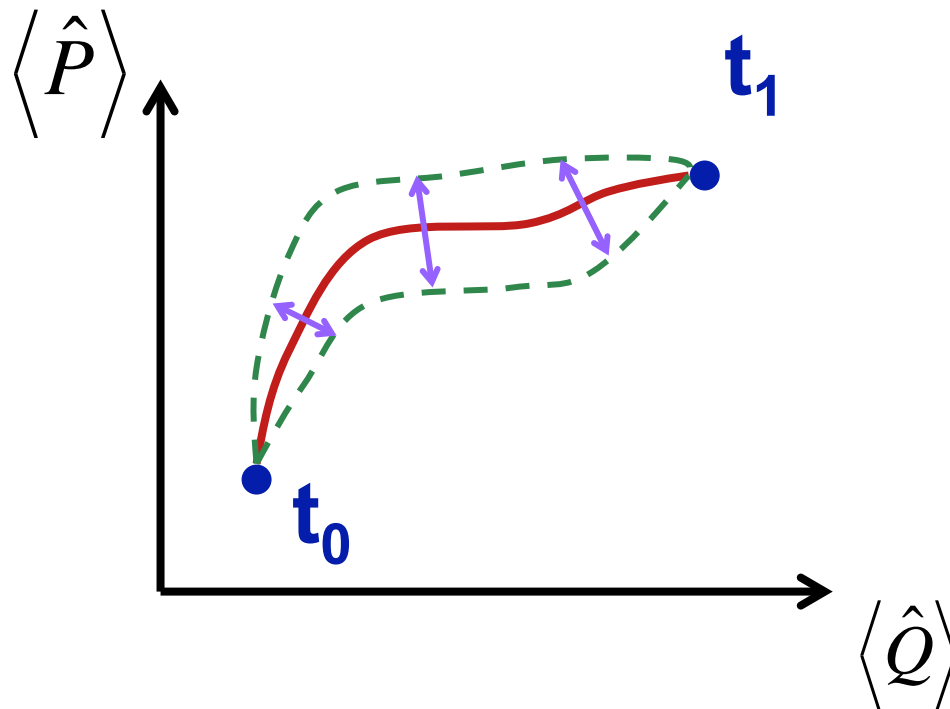
**$N$  interacting fermions (nucleons)**  
*Pauli principle*

# I) TDHF: *Formalism*

**Dirac action**

$$S = \int_{t_0}^{t_1} dt \quad \langle \Psi | i\hbar \frac{d}{dt} - \hat{H} | \Psi \rangle$$

**Variational principle**  $\delta S = 0 \Leftrightarrow$  *Schrödinger*



# I) TDHF: *Formalism*

**Dirac action**  $S = \int_{t_0}^{t_1} dt \langle \Psi | i\hbar \frac{d}{dt} - \hat{H} | \Psi \rangle$

**Variational principle**  $\delta S = 0$

**Subspace of independent particles**

**→ TDHF equations**  $i\hbar \frac{d}{dt} |\varphi_\alpha\rangle = \hat{h}[\rho] |\varphi_\alpha\rangle$   
 $1 \leq \alpha \leq A$

**s.p. hamiltonian**  $h[\rho] = \frac{\delta E[\rho]}{\delta \rho}$

# I) TDHF: *practical aspects*

## Skyrme functional

T. Skyrme, Phil. Mag. **1**, 1043 (1956)

$$E[\rho] \equiv E[\rho(\mathbf{r}), \mathbf{j}(\mathbf{r}), \tau(\mathbf{r}), \mathbf{s}(\mathbf{r})...]$$

*10 parameters fitted on structure properties:*

*saturation, compressibility, neutron matter, symmetry energy, few masses and radii, spin-orbit splitting...*

## TDHF3D (P. Bonche) + SLy4d

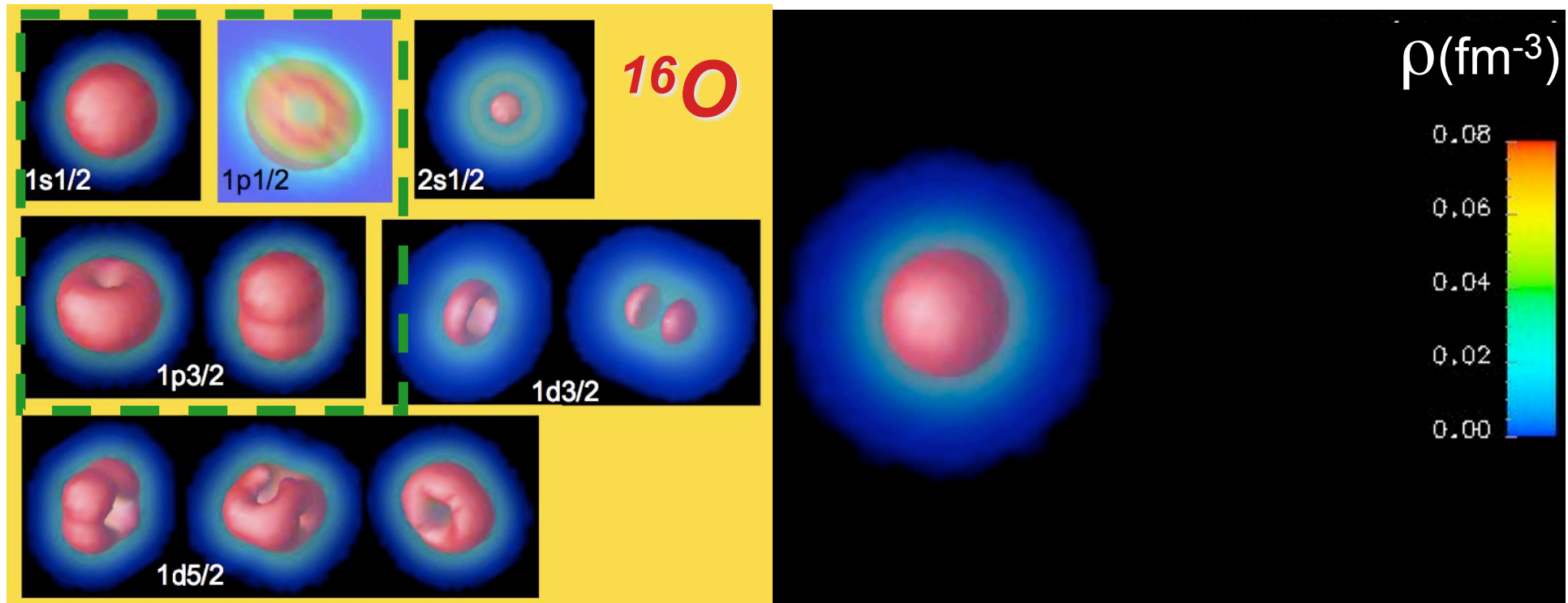
K.-H. Kim, T. Otsuka and P. Bonche, JPG **23**, 1267 (1997)

# I) TDHF: *practical aspects*

## Initial condition

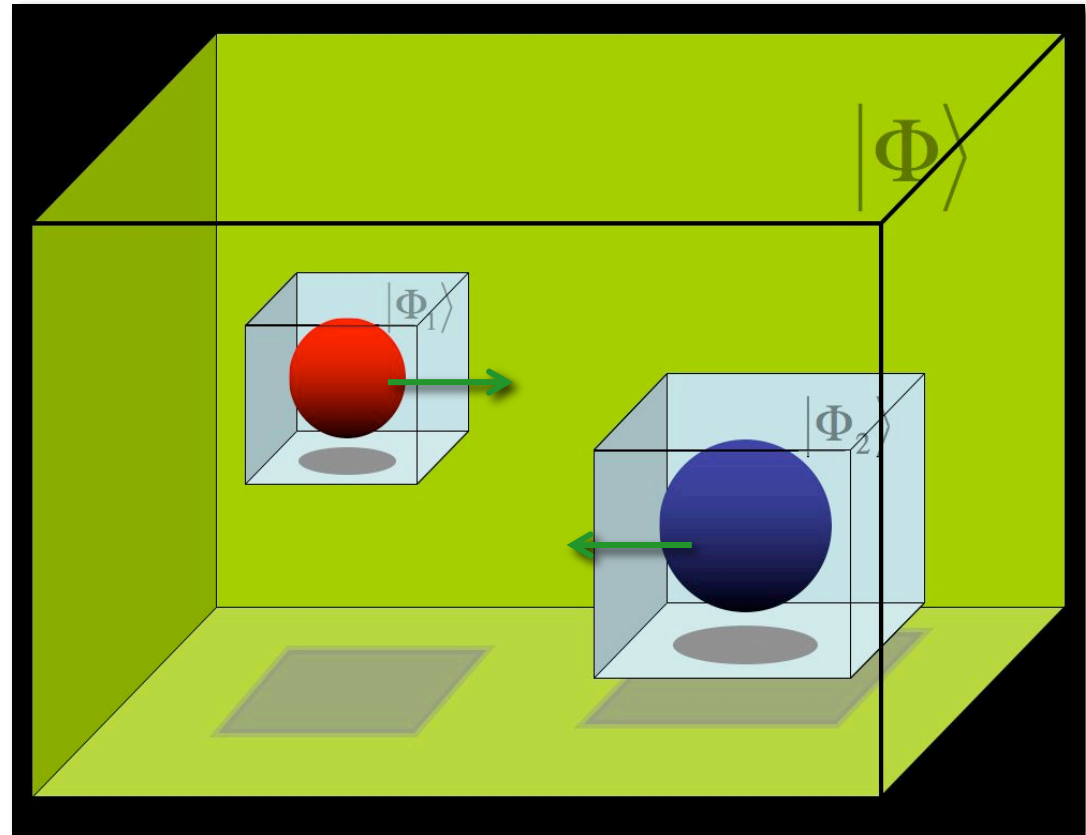
- Rutherford trajectory from  $\infty$  to  $D_0 \sim 40$  fm
- HF ground state at  $D_0$

neutron occupied w.f.



# I) TDHF: *practical aspects*

## Initial state



## Galilean boost

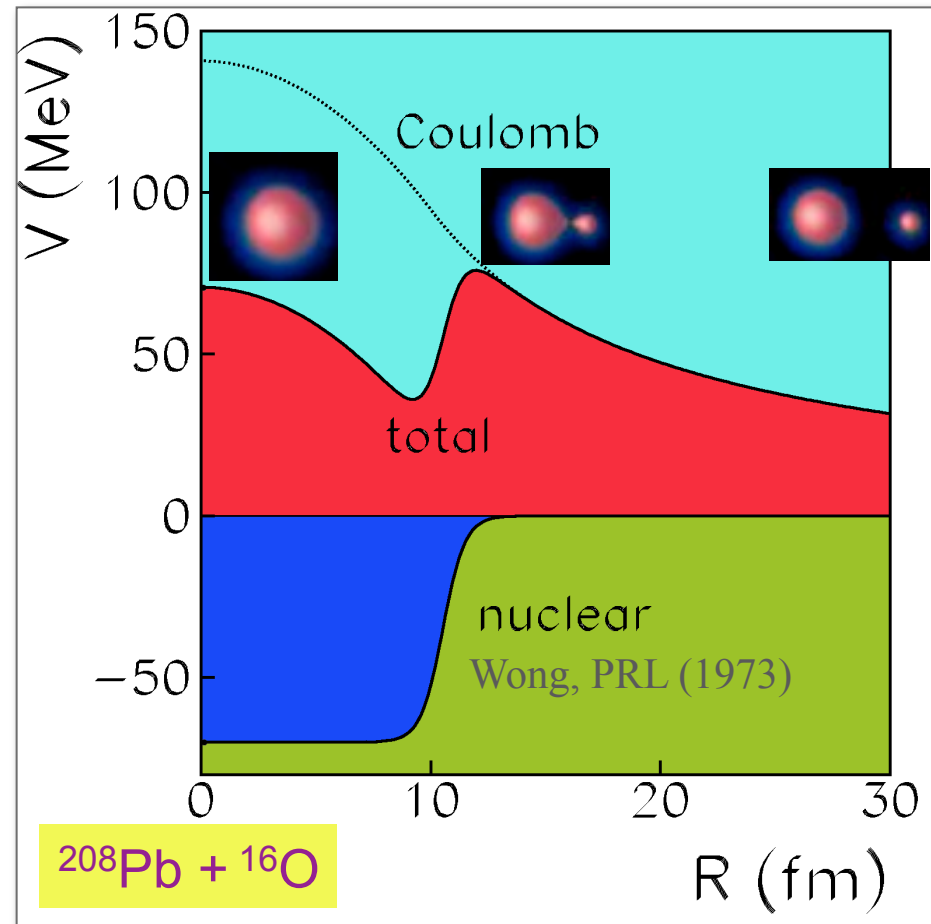
$$|\psi(0)\rangle = \exp(-i\mathbf{P}\hat{\mathbf{R}})|\psi_{HF}\rangle$$

D.J. Thouless and J.G. Valatin, NPA **31**, 211 (1962)



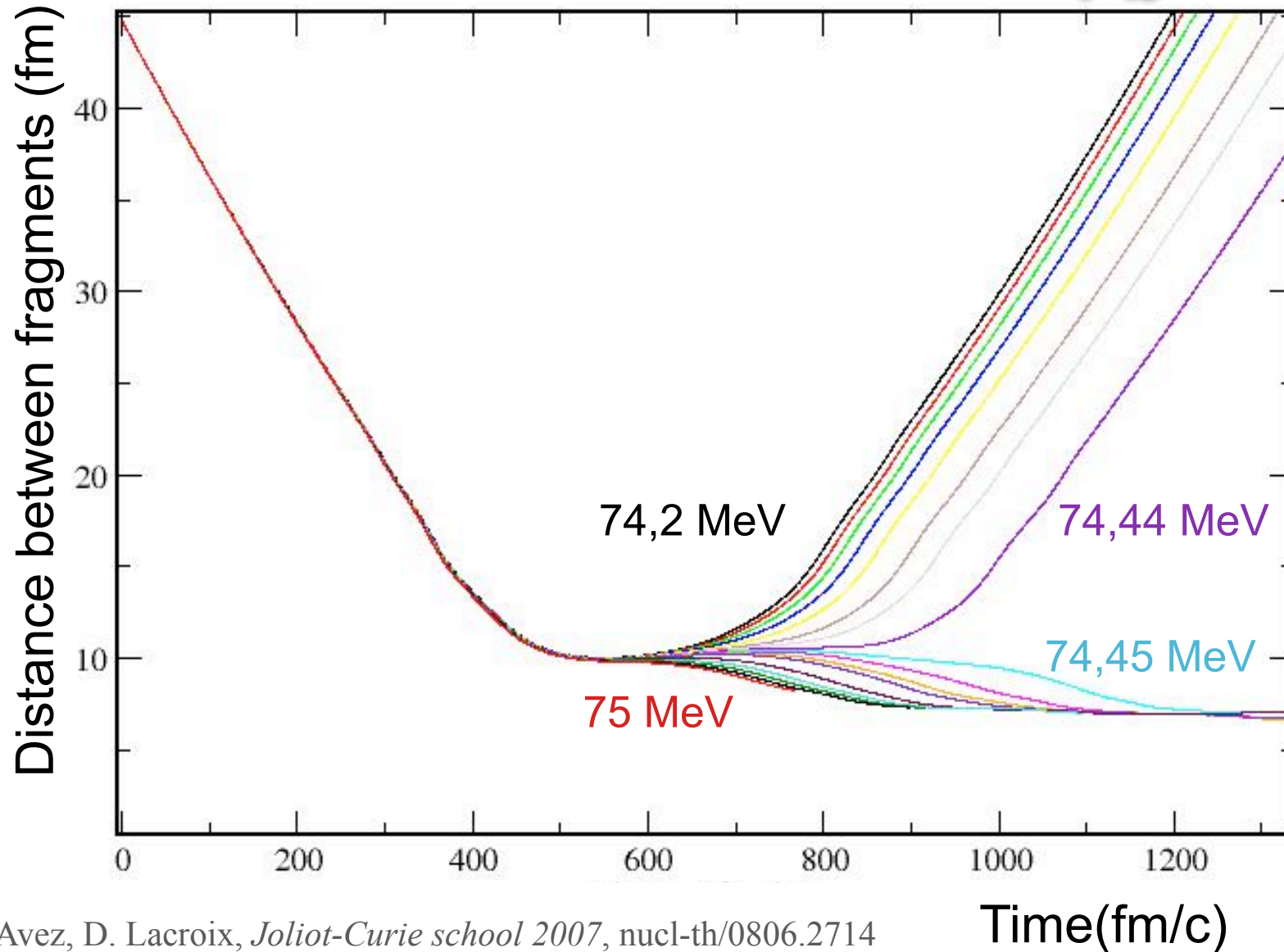
## II) Applications to fusion: *light and medium-heavy systems*

**fusion barriers**



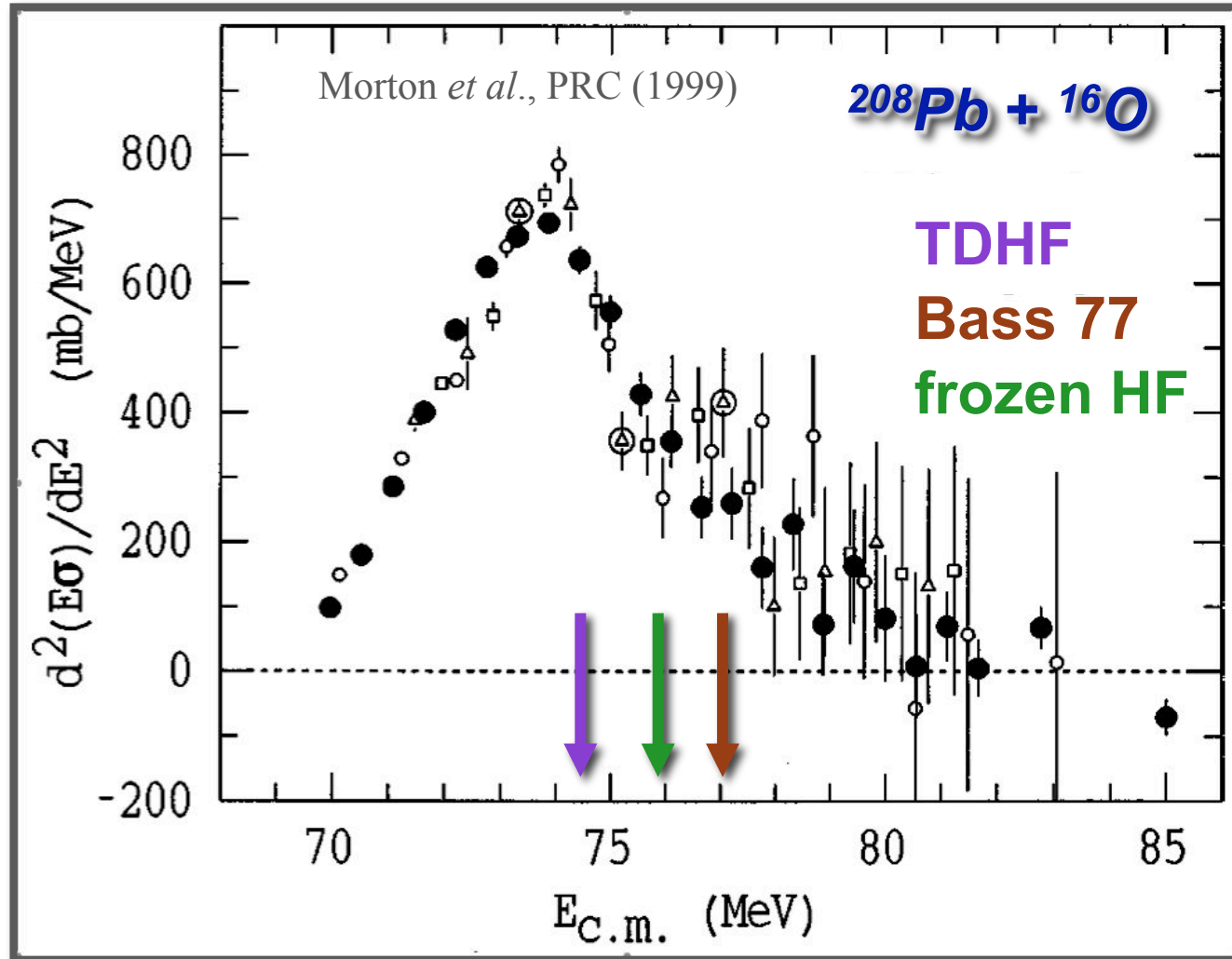
## II) Applications to fusion: *light and medium-heavy systems*

$^{208}\text{Pb} + ^{16}\text{O}$



## II) Applications to fusion: *light and medium-heavy systems*

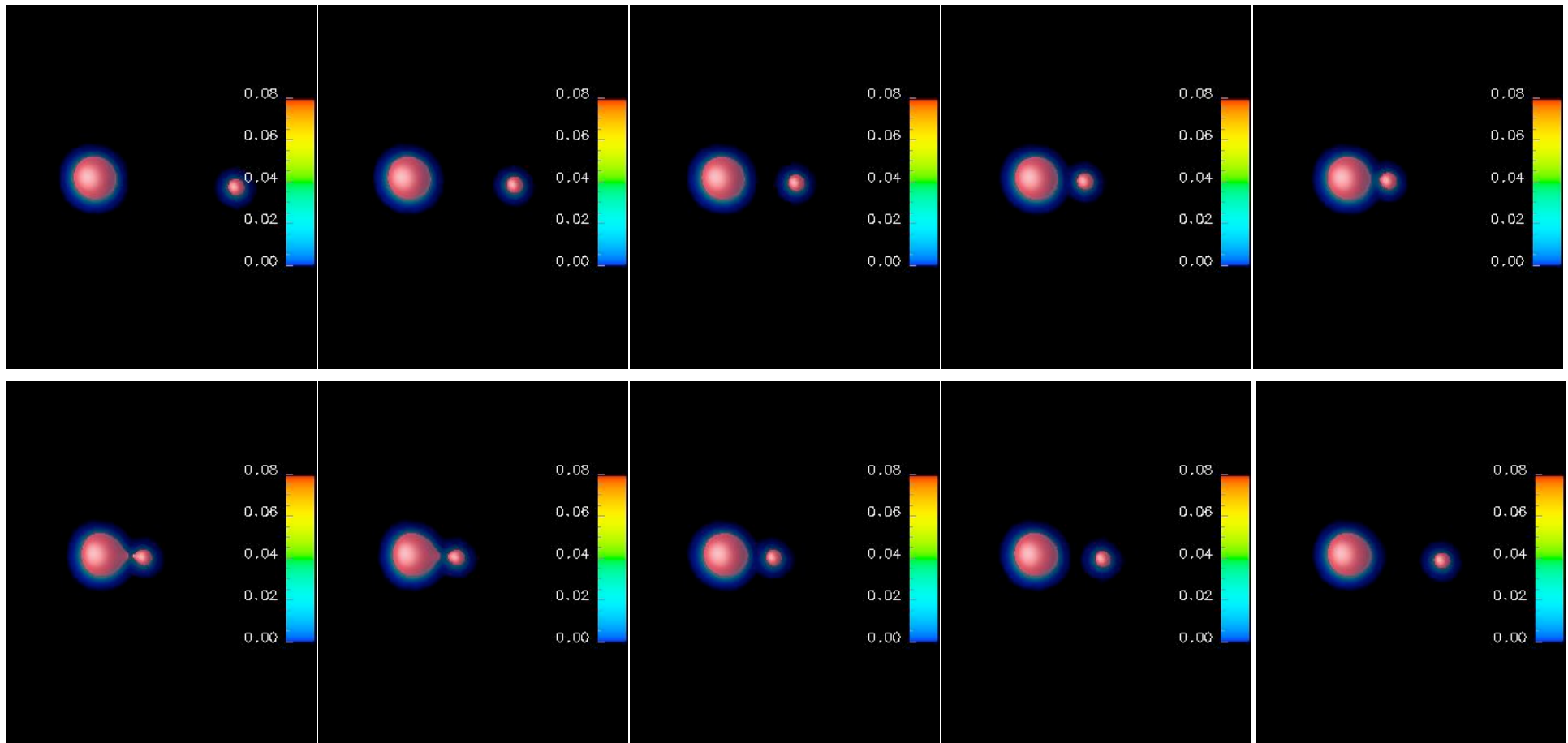
### Fusion barriers



## II) Applications to fusion: *light and medium-heavy systems*

$^{208}\text{Pb} + ^{16}\text{O}$

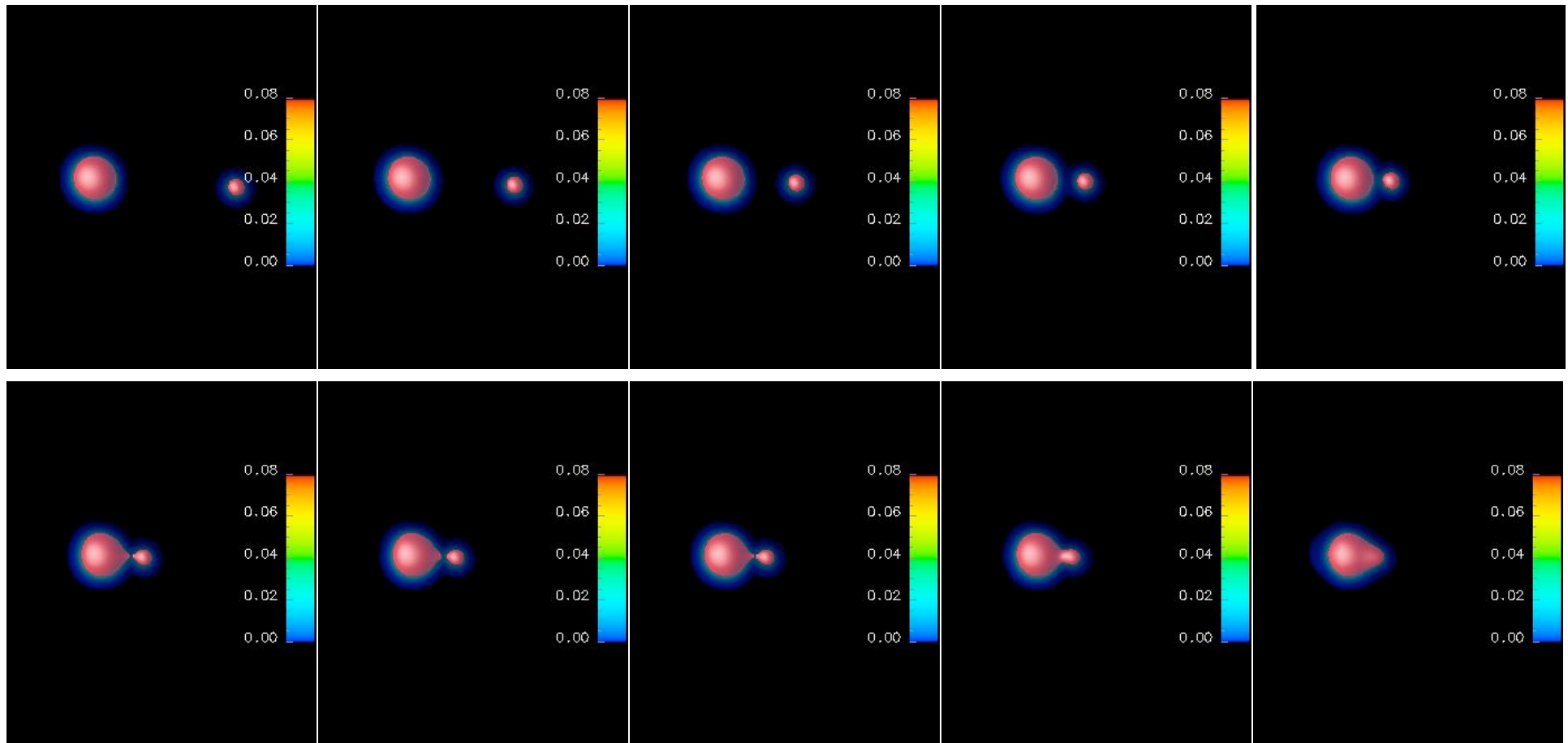
74.44 MeV



## II) Applications to fusion: *light and medium-heavy systems*

$^{208}\text{Pb} + ^{16}\text{O}$

74.45 MeV

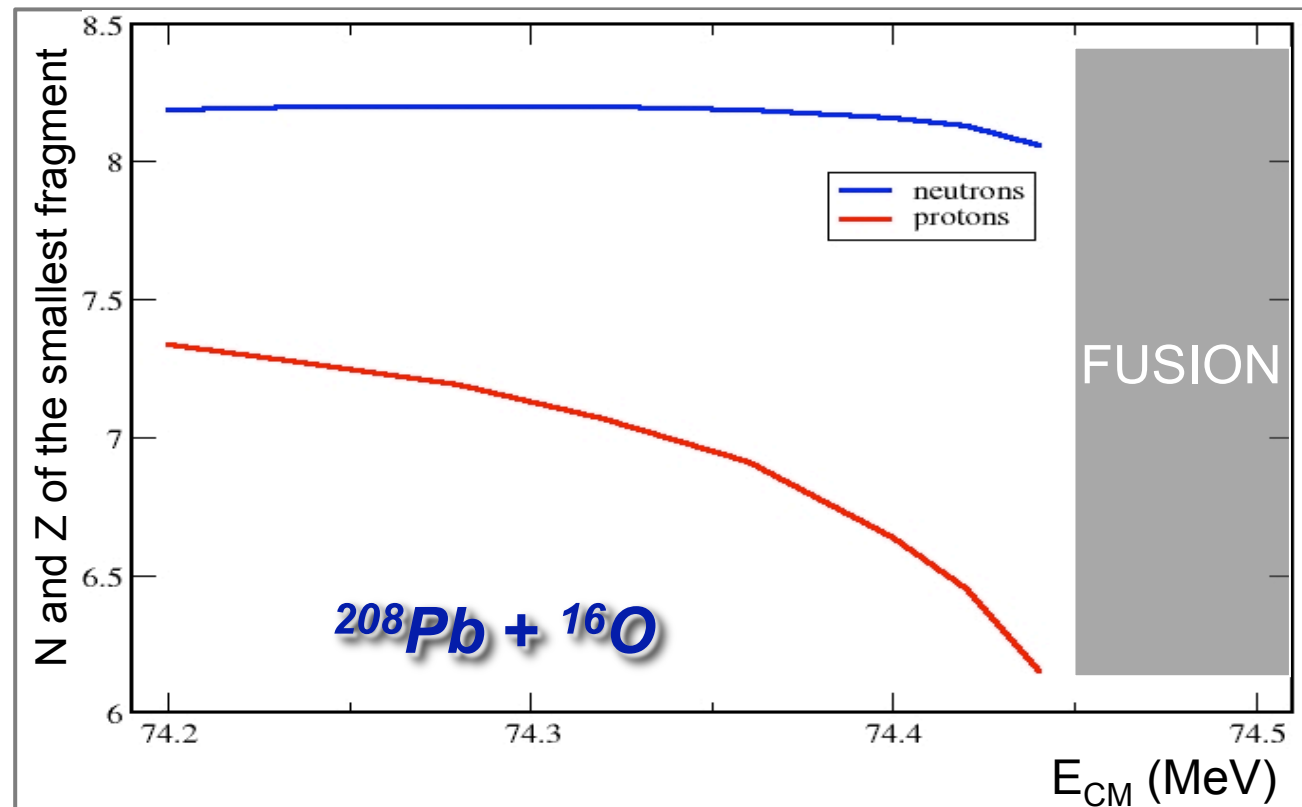


## II) Applications to fusion: *light and medium-heavy systems*

**couplings to transfer in  $^{16}\text{O}+^{208}\text{Pb}$**

*CRC calculations* I.J. Thompson *et al.*, NPA 505, 84 (1989).

**TDHF:**

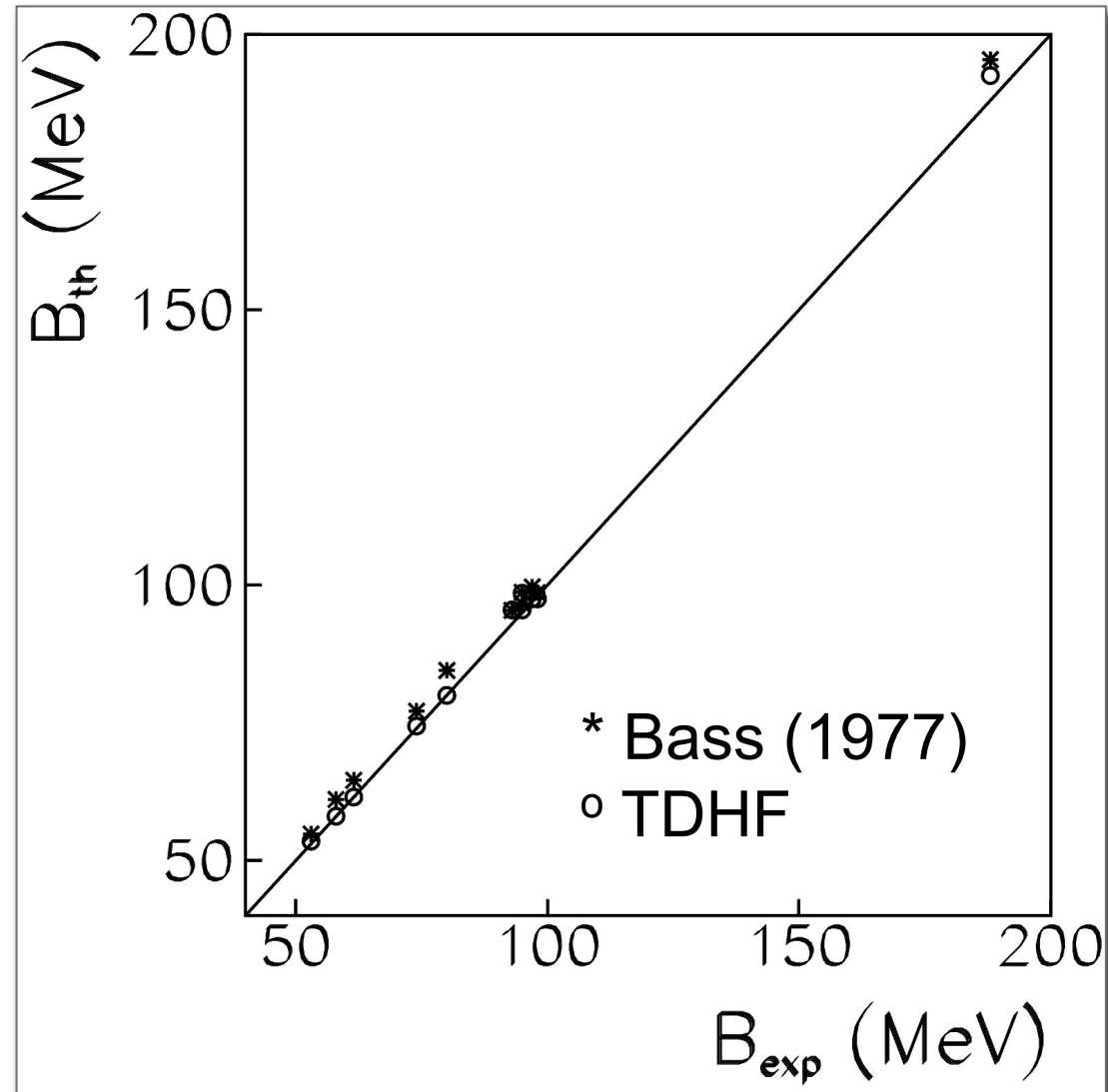


**isovector restoring force because of N/Z asymmetry**

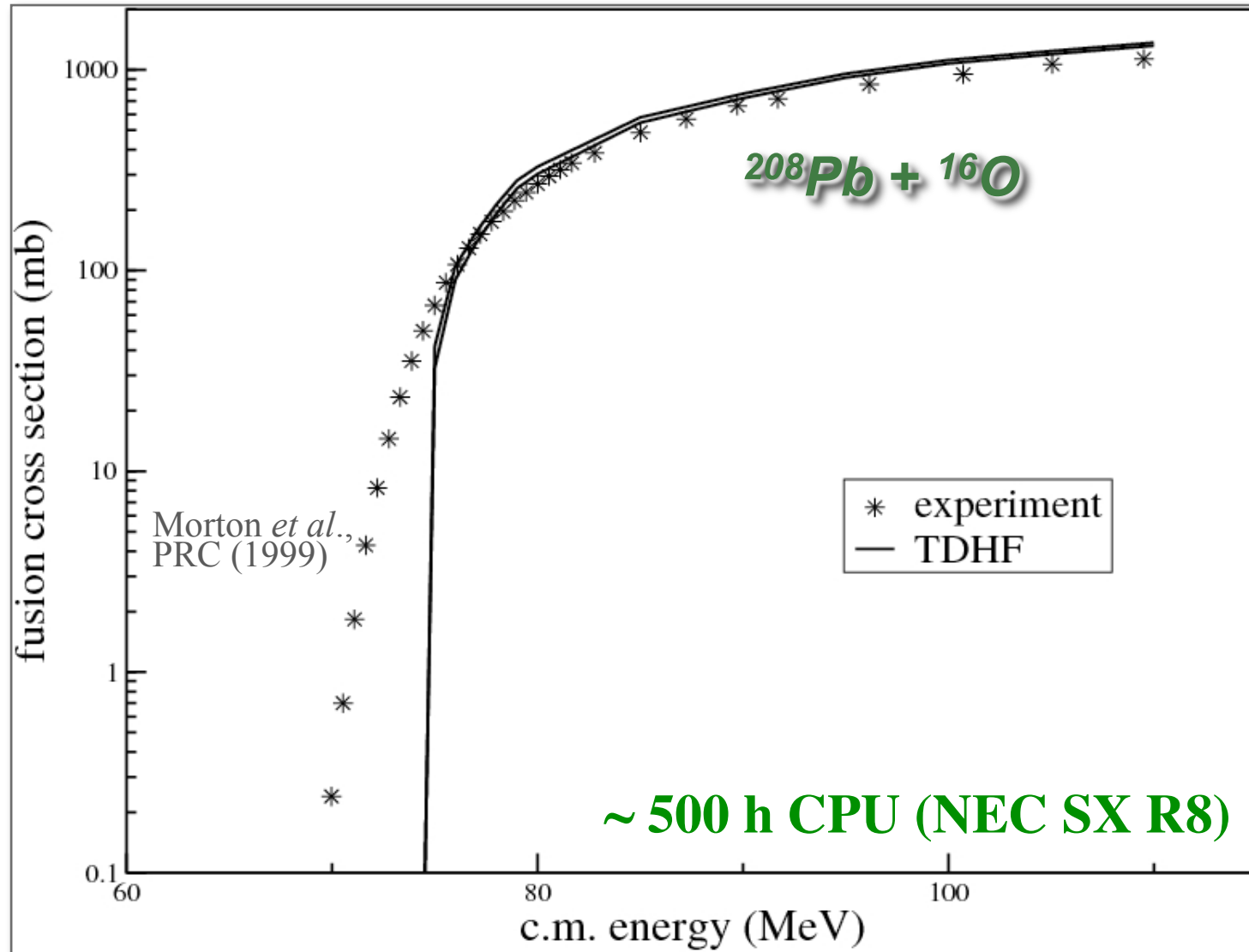
C. S., Ph. Chomaz and G. de France, PRL (2001) and PRC (2007)

## II) Applications to fusion: *light and medium-heavy systems*

systematics



## II) Applications to fusion: *light and medium-heavy systems*

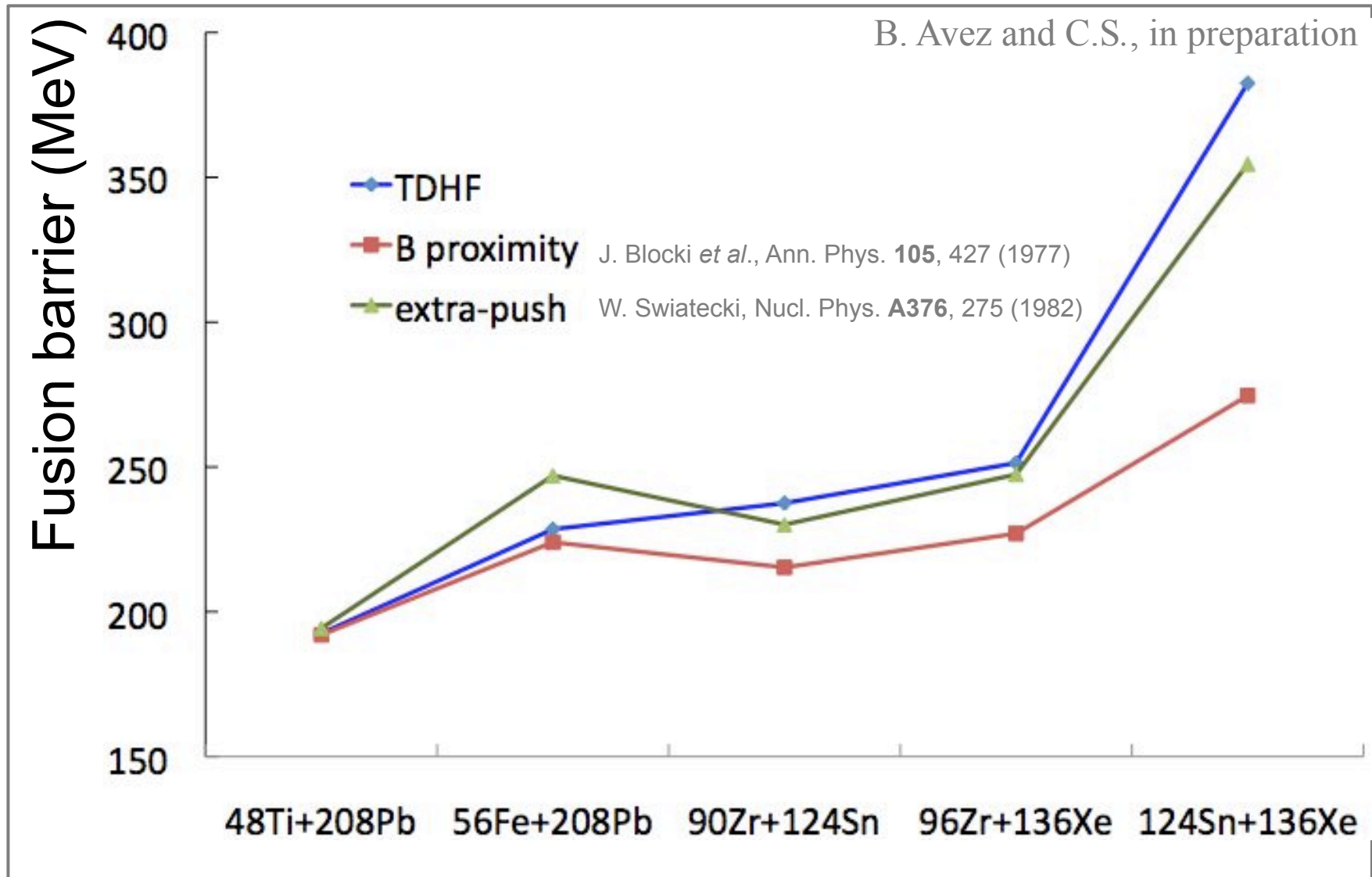




## II) Applications to fusion:

### *fusion hindrance of heavy systems*

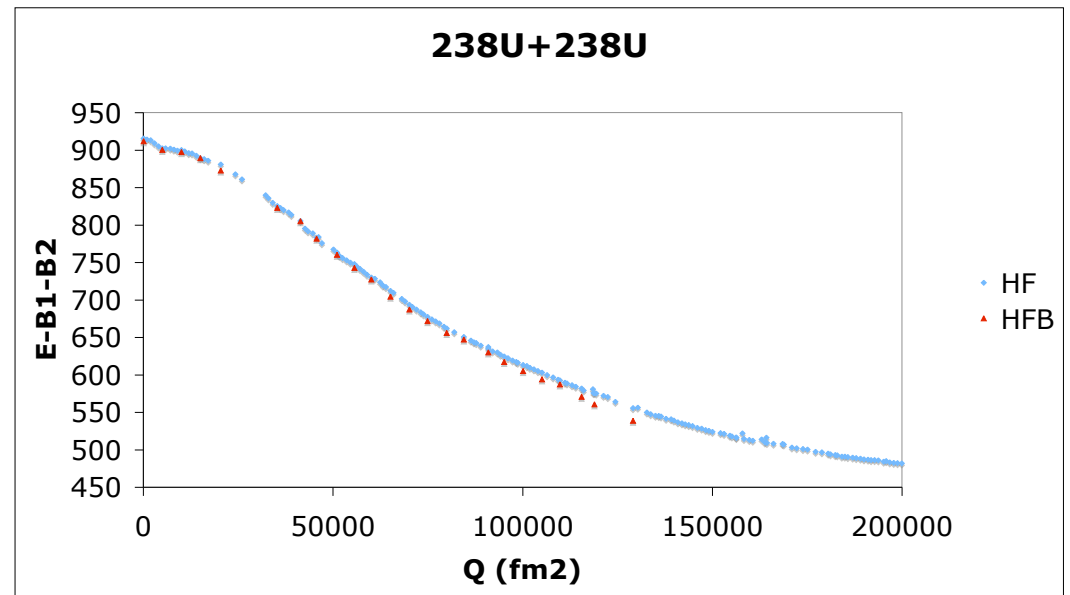
J.R. Nix and A.J. Sierk,  
PRC **15**, 2072 (1977)



## II) Applications to fusion: *collision time of $^{238}\text{U}+^{238}\text{U}$*

### No pocket for fusion

J.F. Berger *et al.*, PRC 41, 2483R (1990)

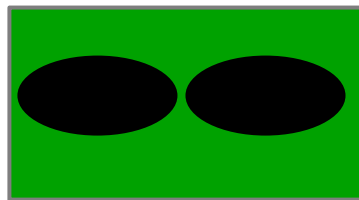


### Collision time

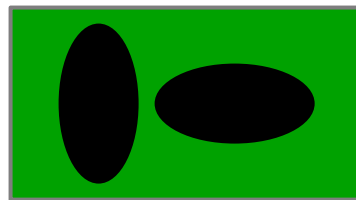
SHE formation, super-strong electric fields

( $e^+e^-$  production if  $T_{\text{coll}} \geq 1000$  fm/c J. Reinhart *et al.*, ZPA 303, 173 (1981))

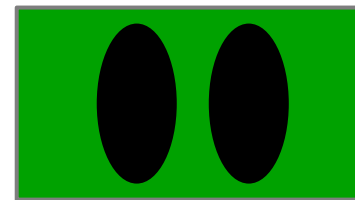
### Role of orientation



top on top



top on side

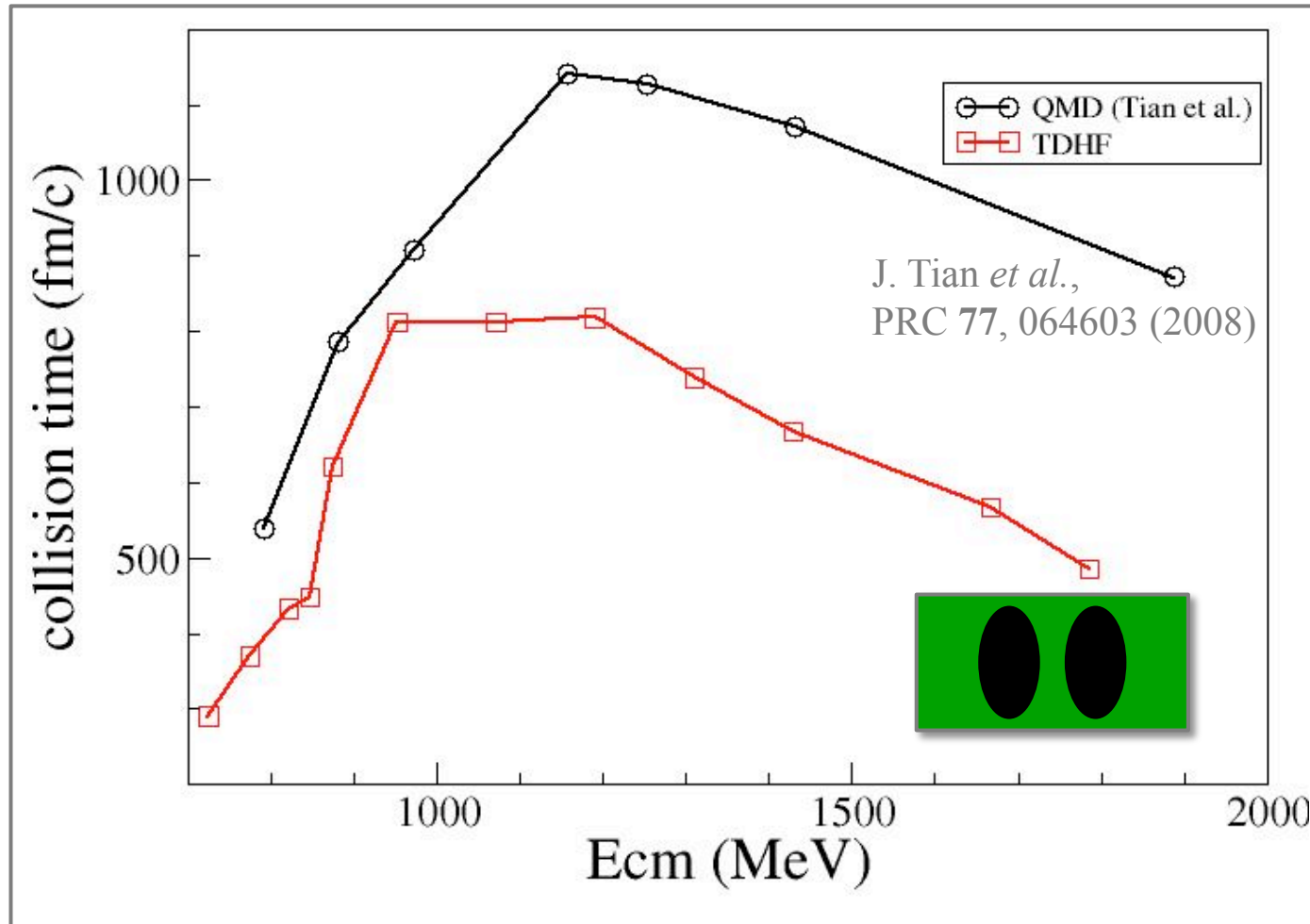


side on side

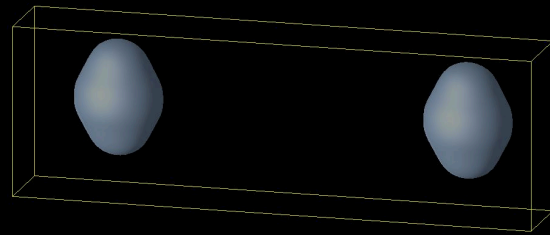
## II) Applications to fusion: *collision time of $^{238}\text{U}+^{238}\text{U}$*

### collision time maximum for side on side

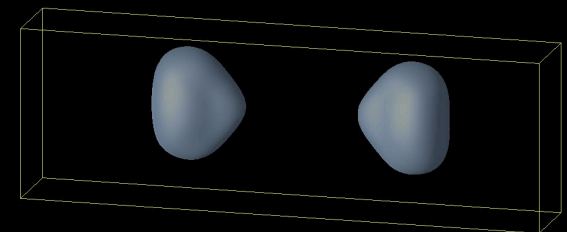
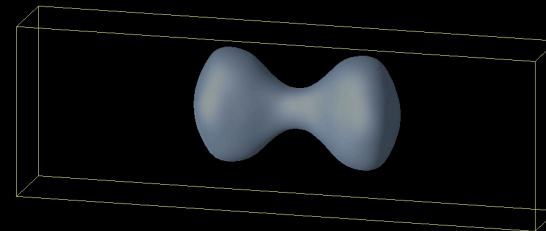
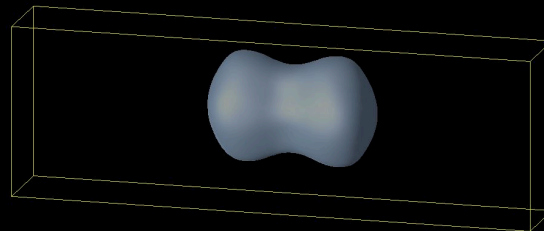
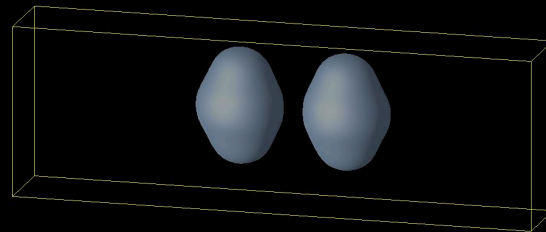
C. Golabek and C.S., in preparation



## II) Applications to fusion: *collision time of $^{238}\text{U}+^{238}\text{U}$*

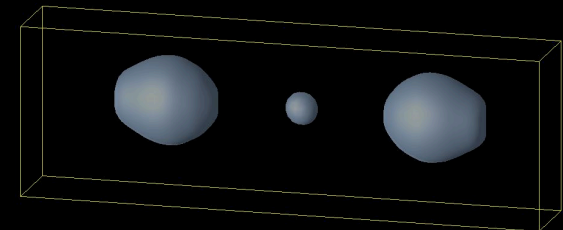
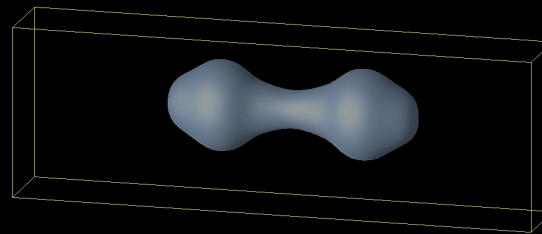
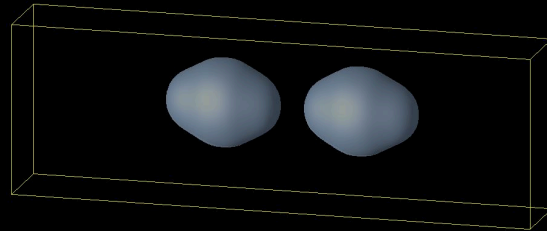
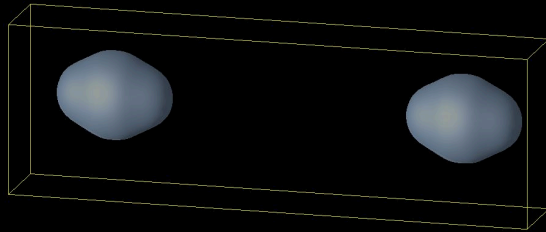


$$E_{\text{CM}} = 1071 \text{ MeV}$$



## II) Applications to fusion: *collision time of $^{238}\text{U}+^{238}\text{U}$*

$$E_{\text{CM}} = 874 \text{ MeV}$$



## Conclusions

- TDHF ok for fusion barriers and cross sections above B
- Fusion hindrance for heavy systems
- $^{238}\text{U}+^{238}\text{U}$  collision time might be too short for  $e^+e^-$  production

## Perspectives

- Fusion with exotic nuclei: *role of symmetry energy ?*
- Mechanisms responsible for fusion hindrance ?
- Effect of pairing ? *TDHFB* B. Avez, C.S. and Ph. Chomaz, PRC 2008.
- Beyond TDHF to go below the barrier.

# Perspectives

## TDHF publications in nuclear physics

