

# Shape coexistence in

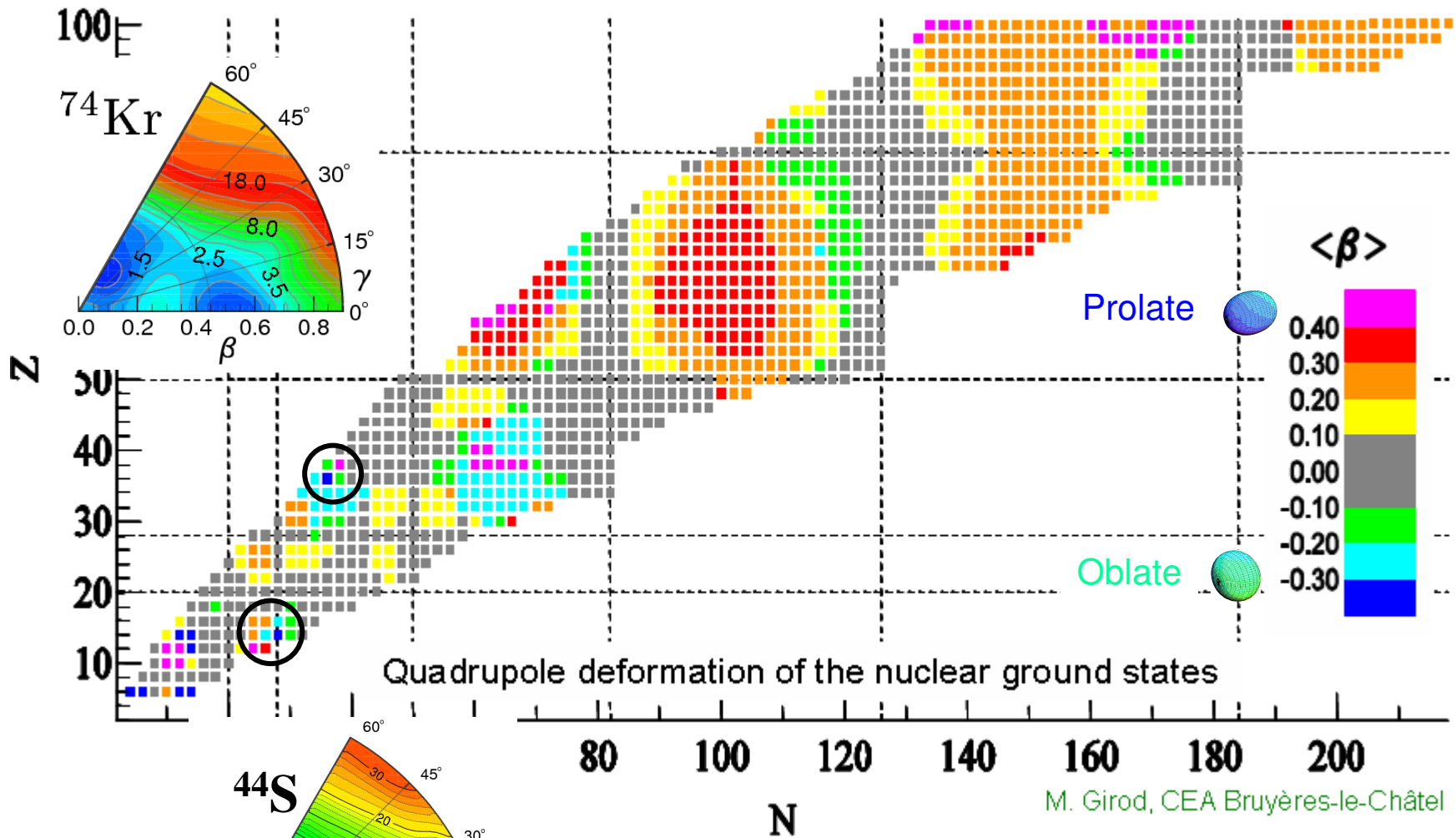
## Kr and Se isotopes near $N=Z$

(incl. new bonus material)

Andreas Görger

Service de Physique Nucléaire  
CEA Saclay

# Nuclear shapes

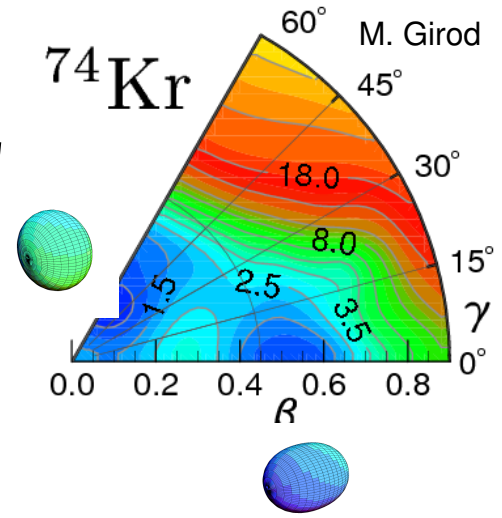
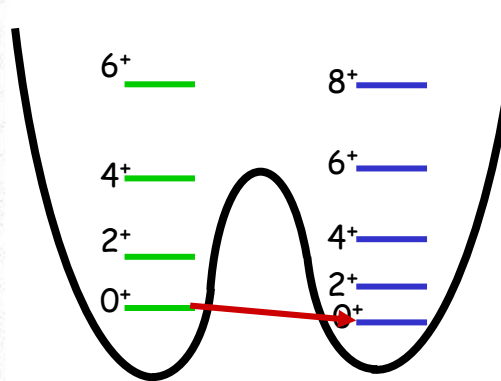
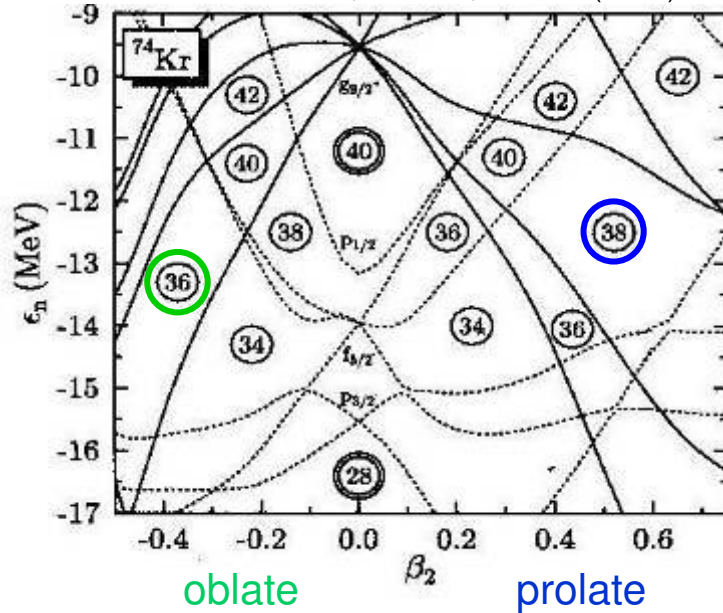


quadrupole moments of excited states, transition rates

- shape coexistence
- shape evolution with N, Z, energy, spin
- evolution of shell structure far from stability
- benchmarks for nuclear structure theory

# Shape coexistence

M. Bender et al., PRC 74, 024312 (2006)



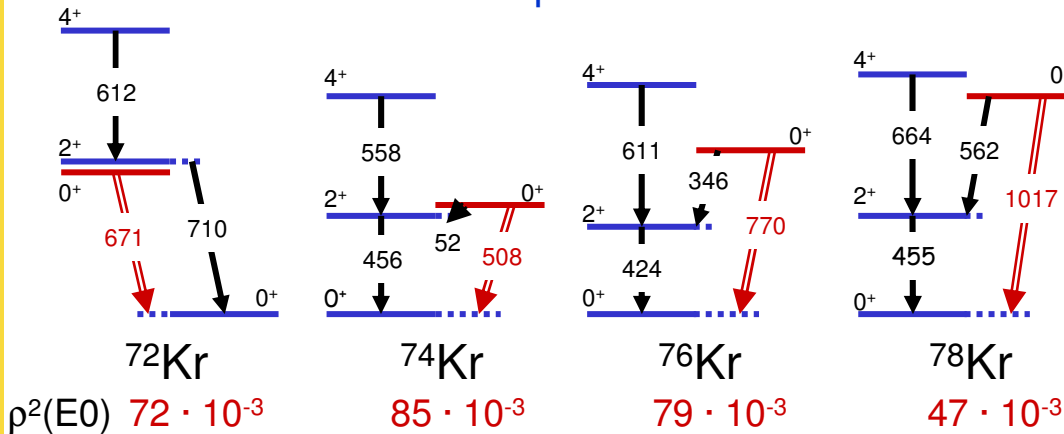
Configuration mixing:

$$|0_1^+\rangle = +\cos\eta |0_{\text{pro}}^+\rangle + \sin\eta |0_{\text{obl}}^+\rangle$$

$$|0_2^+\rangle = -\sin\eta |0_{\text{pro}}^+\rangle + \cos\eta |0_{\text{obl}}^+\rangle$$

electric monopole transition

$$\langle 0_2^+ || \mathbf{M}(E0) || 0_1^+ \rangle \propto \sin\eta \cos\eta (\beta_{\text{pro}}^2 - \beta_{\text{obl}}^2)$$

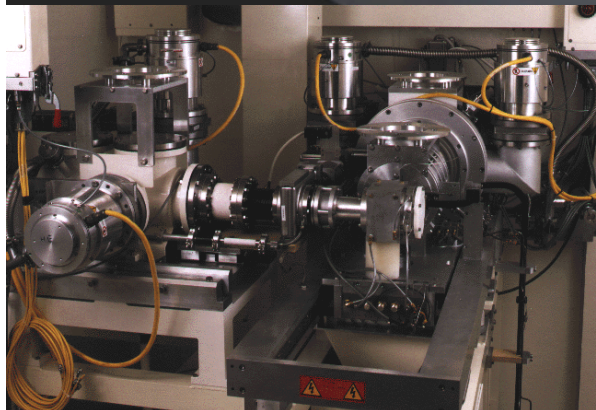
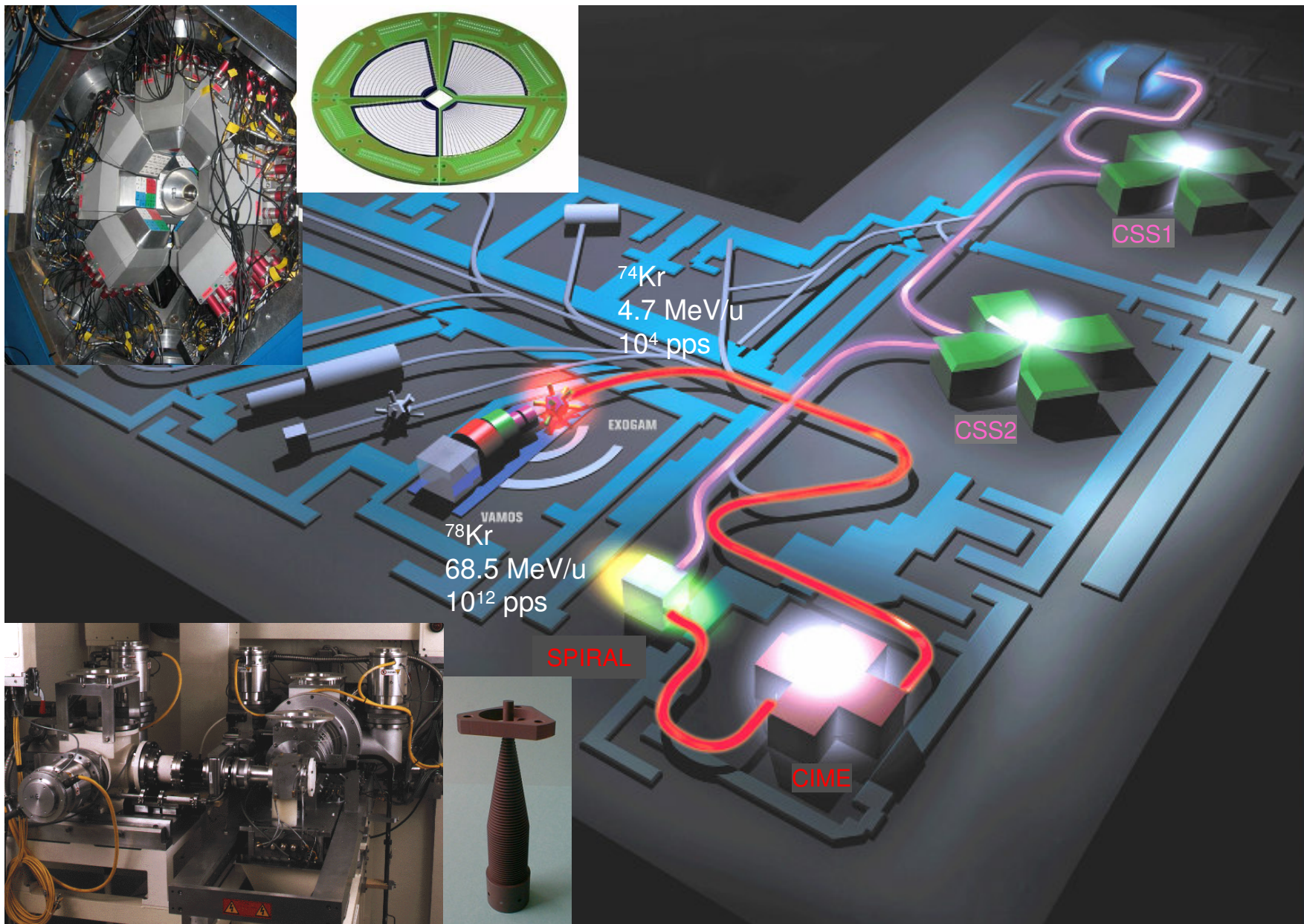


- shape isomers
- shape inversion for  $^{72}\text{Kr}$

E. Bouchez et. al.,  
Phys. Rev. Lett. 90, 082502 (2003)

# Coulomb excitation of radioactive beams from SPIRAL / GANIL

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# Multi-step Coulomb excitation of $^{74,76}\text{Kr}$ on $^{208}\text{Pb}$

l r f u

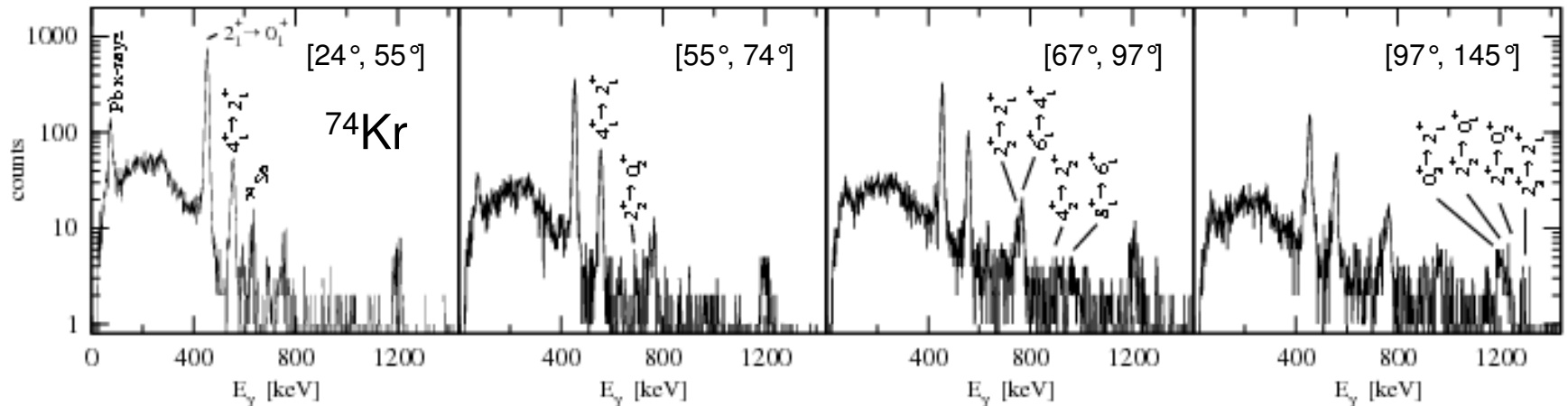
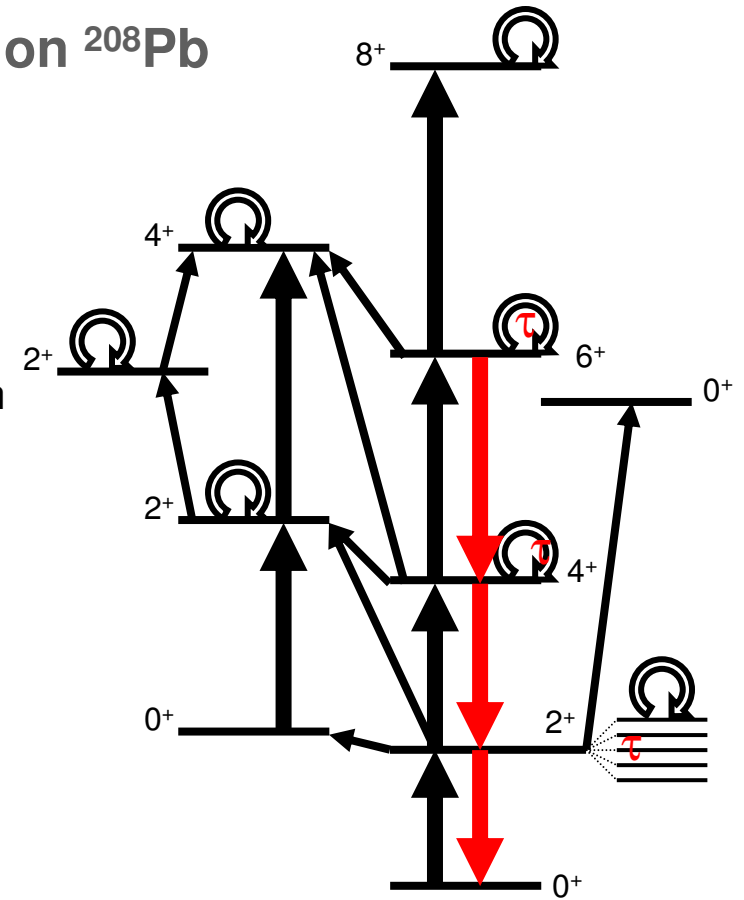
cea

saclay

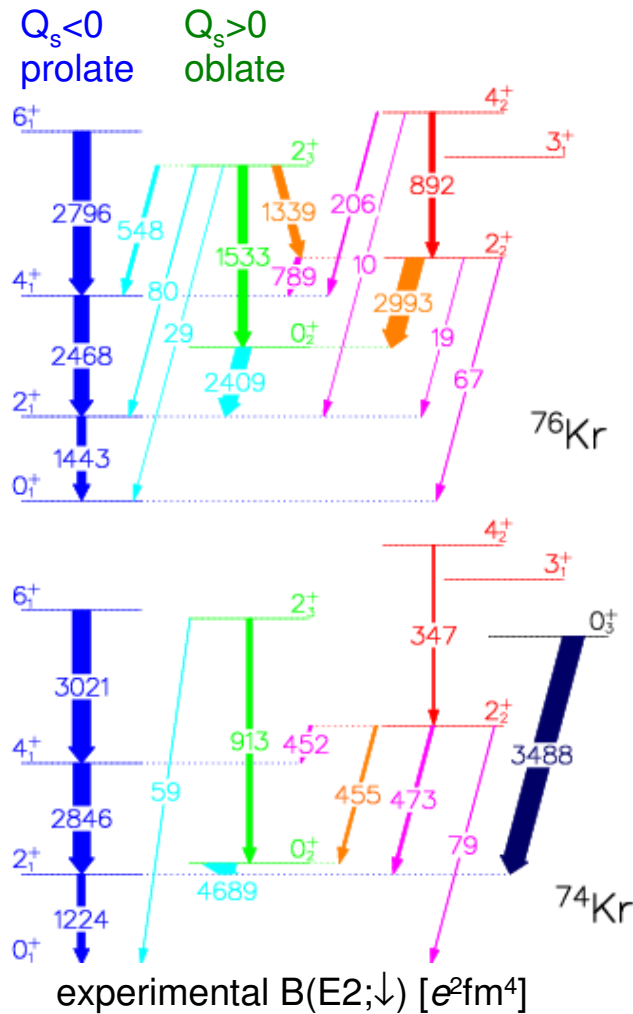
- safe energy  $\Rightarrow$  purely electromagnetic excitation
- transitional matrix element  $\Rightarrow$  **B(E2)**
- diagonal matrix element  $\Rightarrow$   **$Q_s$**
- reorientation effect  $\Rightarrow$  sensitive to nuclear shape
- $\sim 20$  matrix elements involved in multi-step excitation
- de-excitation  $\gamma$ -ray yields  $\Rightarrow$   **$d\sigma/d\theta$**
- $\chi^2$  minimization of matrix elements to reproduce experimental  $\gamma$ -ray yields (code GOSIA)
- spectroscopic data (lifetimes, branching ratios) as additional data points for  $\chi^2$  fit
- lifetimes: B(E2) independent of  $Q_s$

RDDS measurement at Legnaro for  $^{74,76}\text{Kr}$

A. Görgen et al. Eur. Phys. J. A 26, 153 (2005)



# Experimental results and comparison with theory

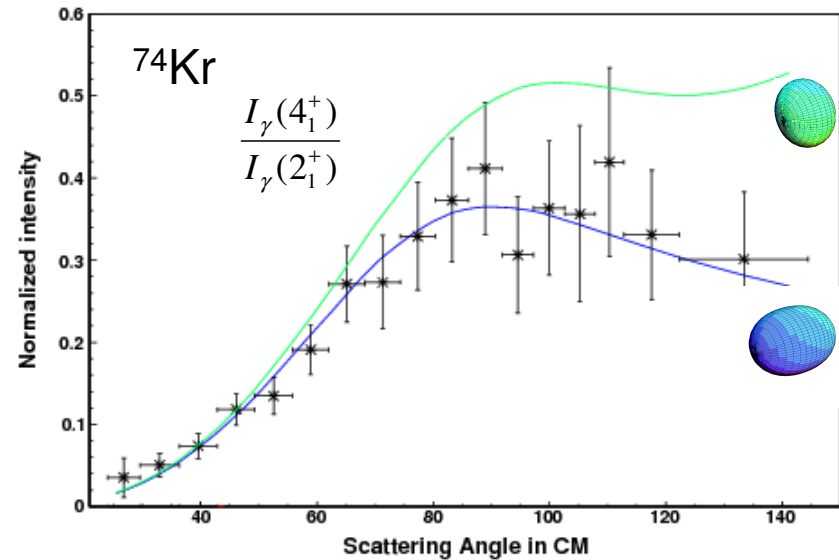


E. Clément et al., Phys. Rev. C 75, 054313 (2007)

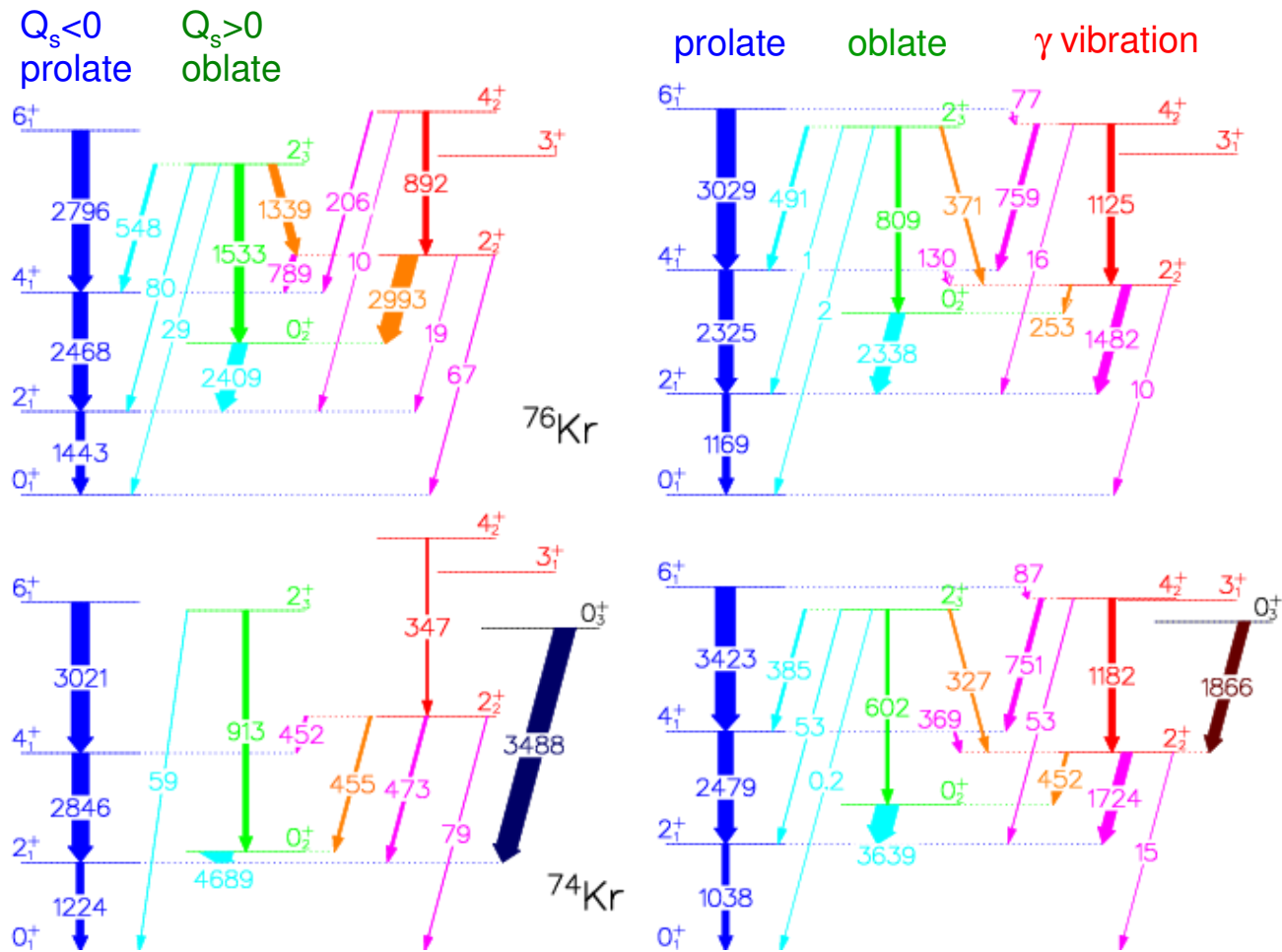
- first reorientation measurement with radioactive beam
- quantitative understanding of shape coexistence and configuration mixing

$$\langle 2_1^+ \| \mathcal{M}(E2) \| 2_1^+ \rangle = -0.70_{-0.30}^{+0.33} \Rightarrow \text{prolate shape}$$

$$\langle 4_1^+ \| \mathcal{M}(E2) \| 4_1^+ \rangle = -1.02_{-0.21}^{+0.59}$$



# Experimental results and comparison with theory



experimental  $B(E2; \downarrow)$  [ $e^2\text{fm}^4$ ]

E. Clément et al., Phys. Rev. C 75, 054313 (2007)

theory: Gogny 5-dim GCM(GOA)  
CEA Bruyères-le-Châtel

- first reorientation measurement with radioactive beam
- quantitative understanding of shape coexistence and configuration mixing

# Shape transition in the light krypton isotopes

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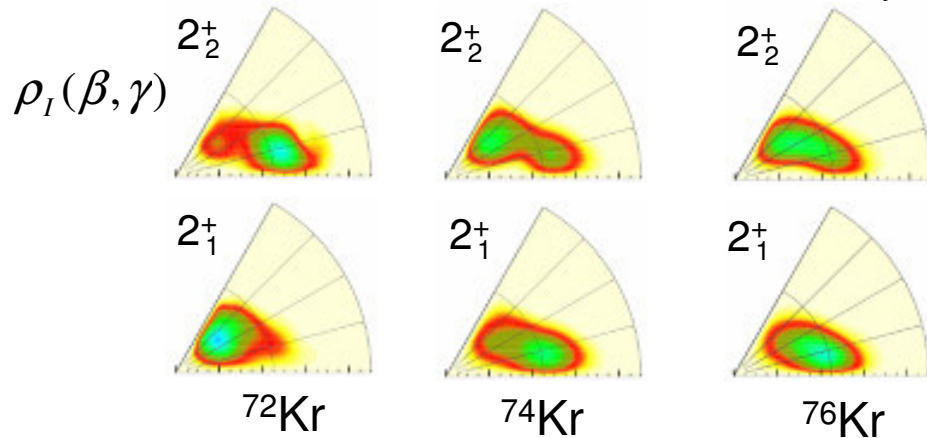
cea

saclay

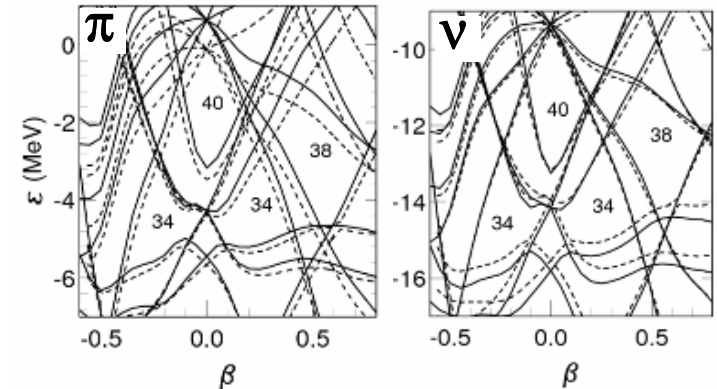
GCM(GOA) configuration mixing calculation

- 5 dimensional:  $q_{20}$ ,  $q_{22}$ , Euler angles
- Gogny D1S interaction

M. Girod et al.,  
submitted to  
Phys. Lett. B



— Gogny D1S  
..... Skyrme SLy6

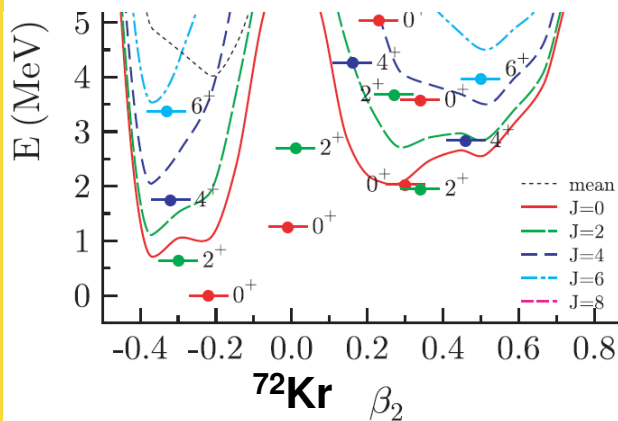


➤ equivalent on mean-field level

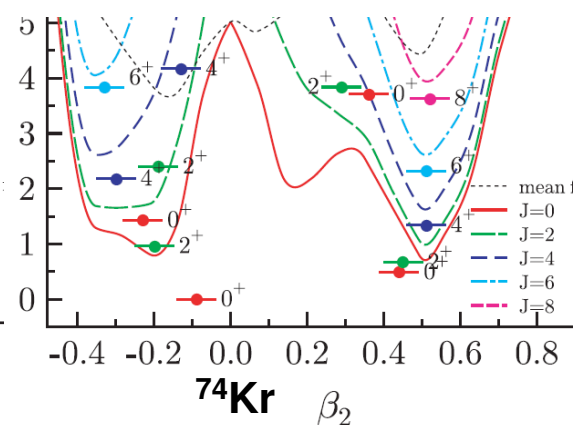
➤ **need to include triaxiality to describe prolate-oblate shape coexistence**

GCM configuration mixing calculation

- axial deformation only:  $q_{20}$
- Skyrme SLy6 interaction

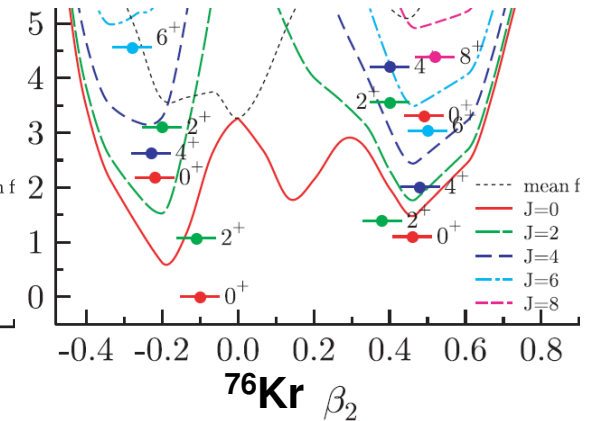


Andreas Gørgen



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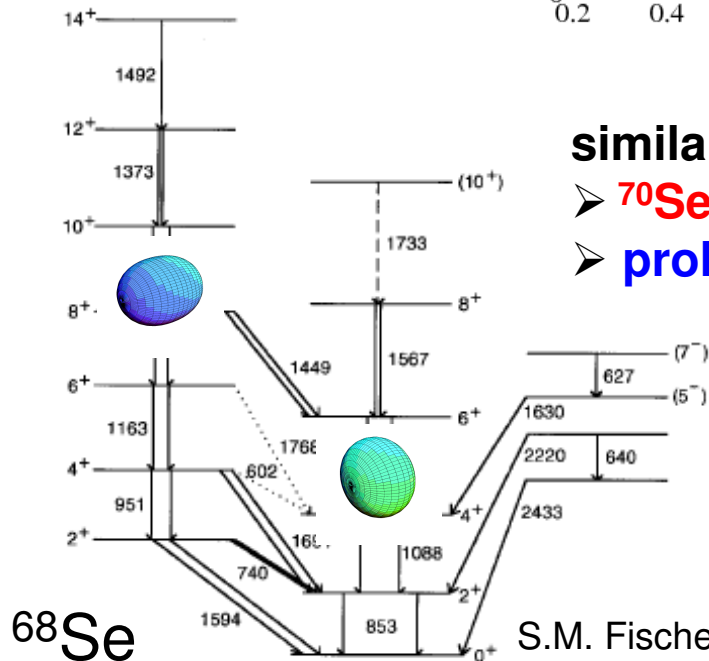
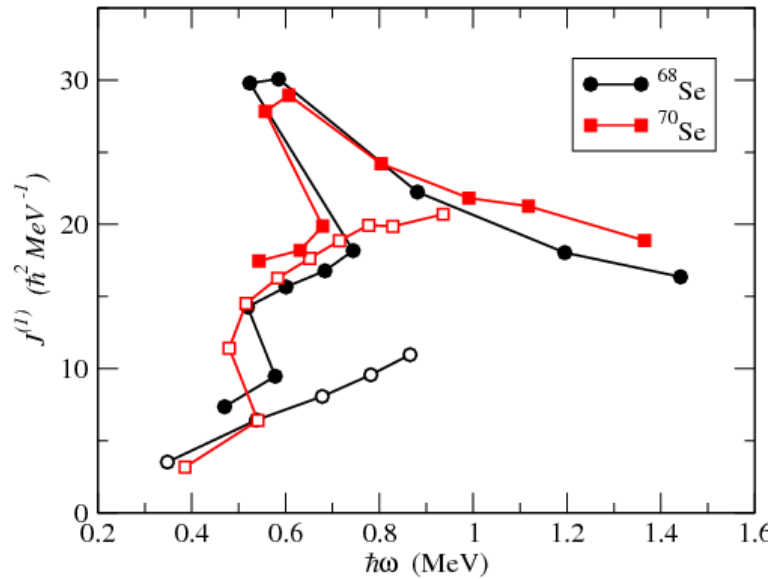
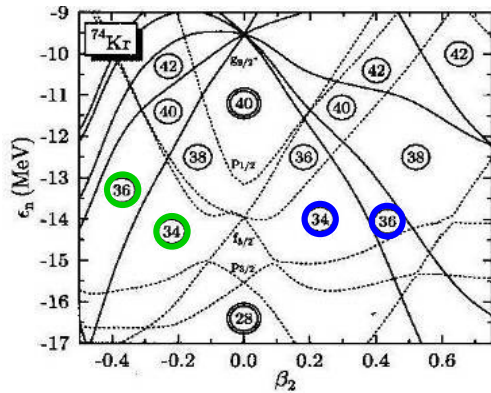
M. Bender et al., PRC 74, 024312 (2006)



1.-5.12.2008



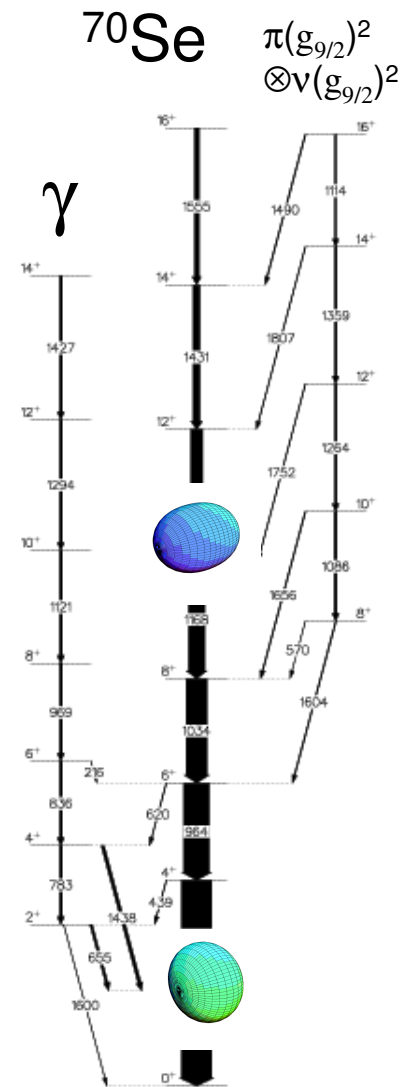
# Shape coexistence in light Selenium isotopes



<sup>68</sup>Se

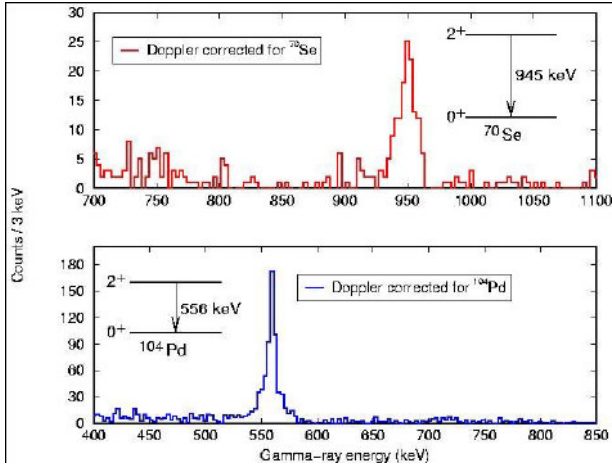
similar  $J^{(1)}$  in <sup>68</sup>Se and <sup>70</sup>Se:  
 ➤ <sup>70</sup>Se oblate near ground state  
 ➤ prolate at higher spin

S.M. Fischer et al.,  
 PRC 67, 064318 (2003)



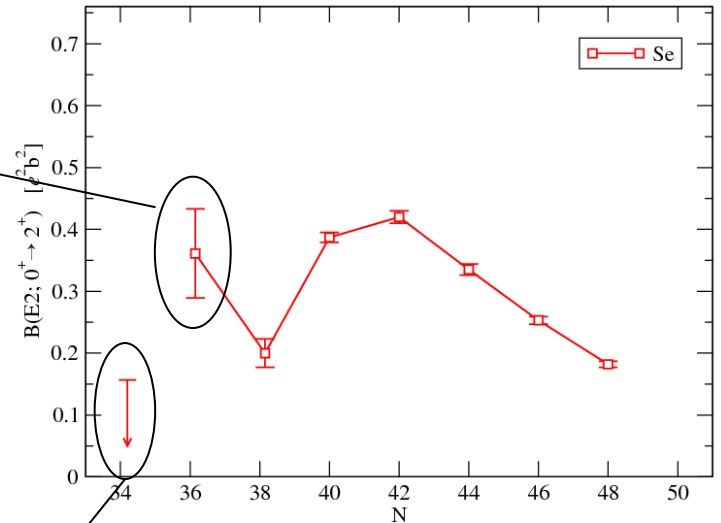
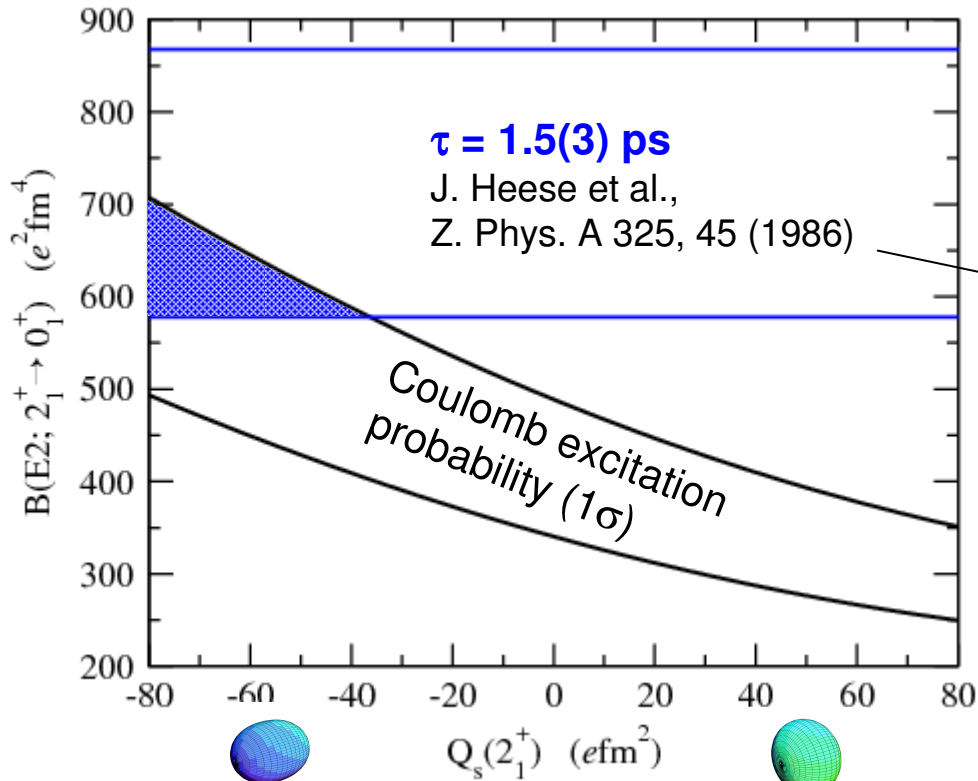
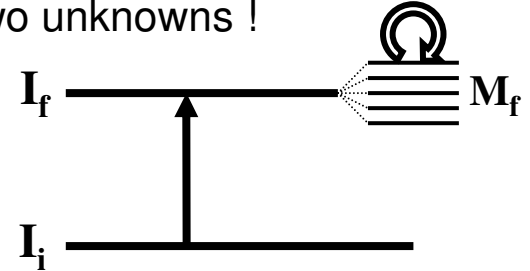
G. Rainovski et al.,  
 J.Phys.G 28, 2617 (2002)

# Coulomb excitation of $^{70}\text{Se}$ at CERN / ISOLDE



- $^{70}\text{Se}$  on  $^{104}\text{Pd}$  at 2.94 MeV/u
- integral measurement
- excitation probability via normalization to target
- depends on  $B(E2)$  and  $Q_s$
- one measurement, two unknowns !

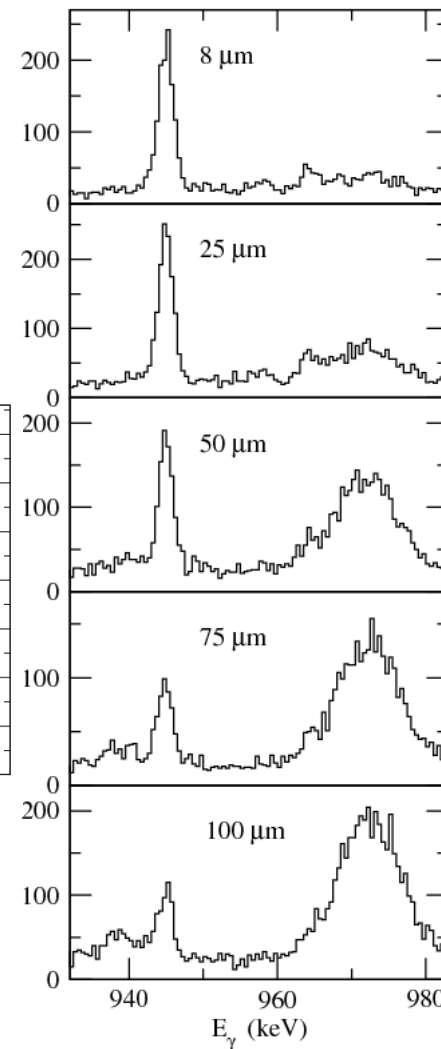
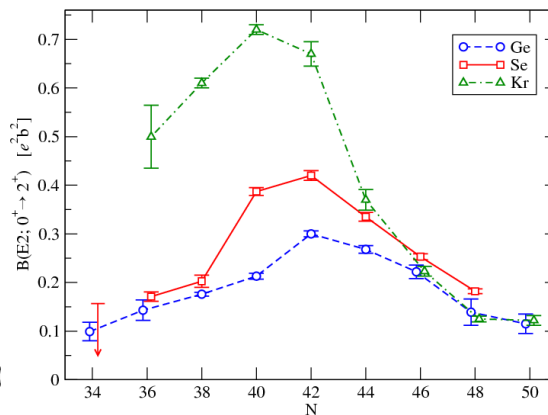
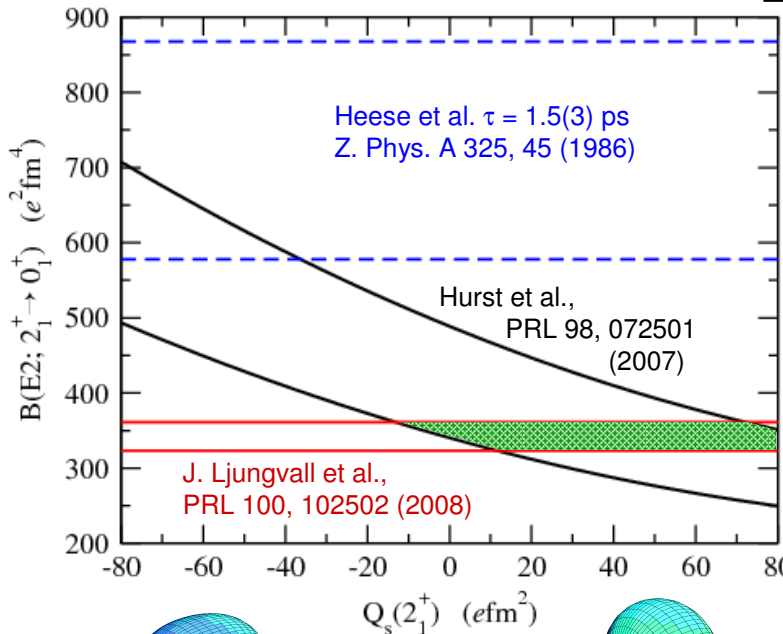
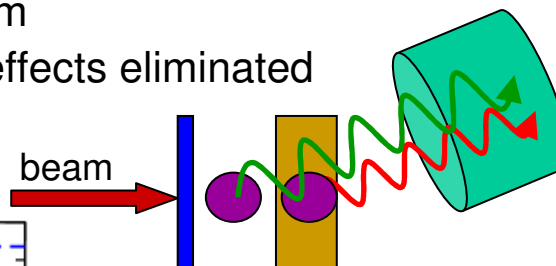
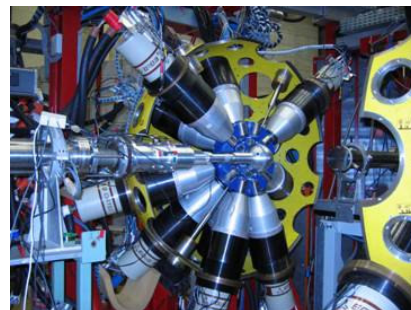
A.M. Hurst et al.,  
PRL 98, 072501 (2007)



GANIL intermediate-energy Coulex  $^{68}\text{Se}$   
E. Clément et al., NIM A 587, 292 (2008)

# Lifetimes in $^{70}\text{Se}$ and $^{72}\text{Se}$ revisited

- Recoil-distance Doppler Shift
- GASP and Köln Plunger at Legnaro
- $^{40}\text{Ca}(^{36}\text{Ar}, \alpha 2p)^{70}\text{Se}$
- 12 distances between 8 and 400  $\mu\text{m}$
- gated from above  $\Rightarrow$  side feeding effects eliminated
- $^{70}\text{Se}, \tau(2^+) = 3.2(2) \text{ ps}$



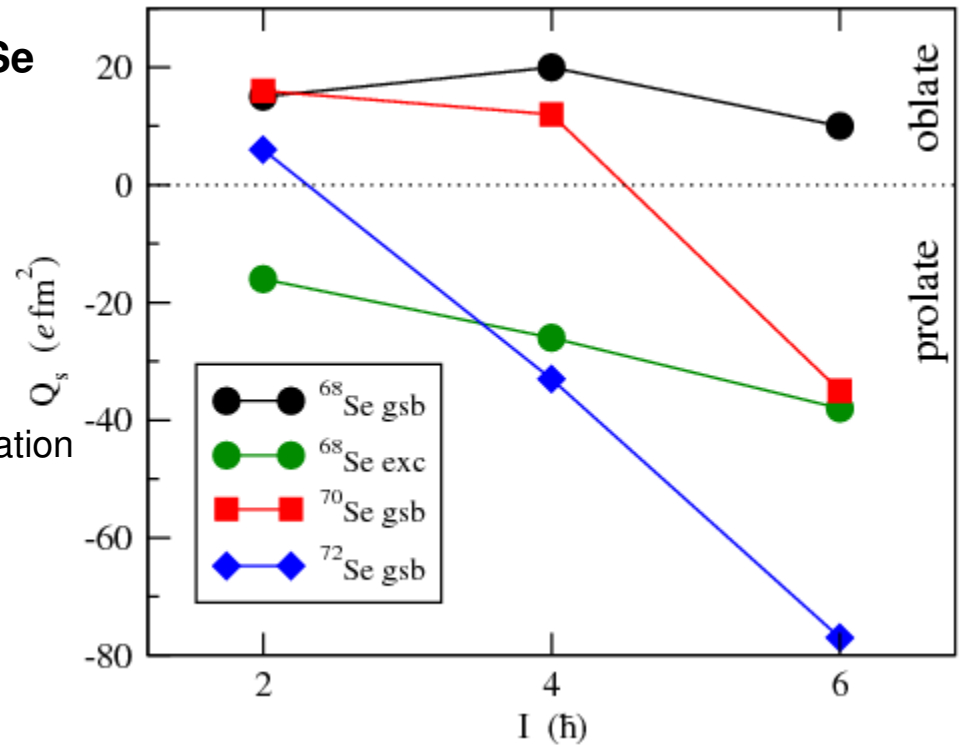
# Shape evolution in the light Selenium isotopes

lr fu

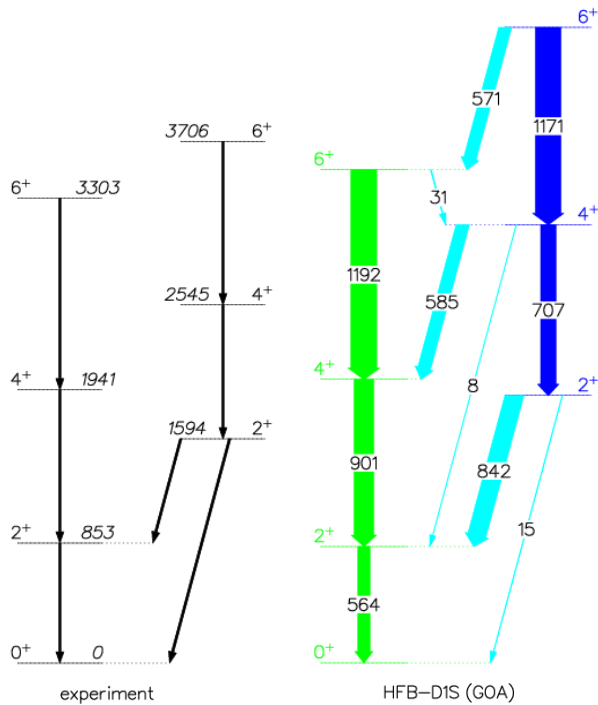
cea

saclay

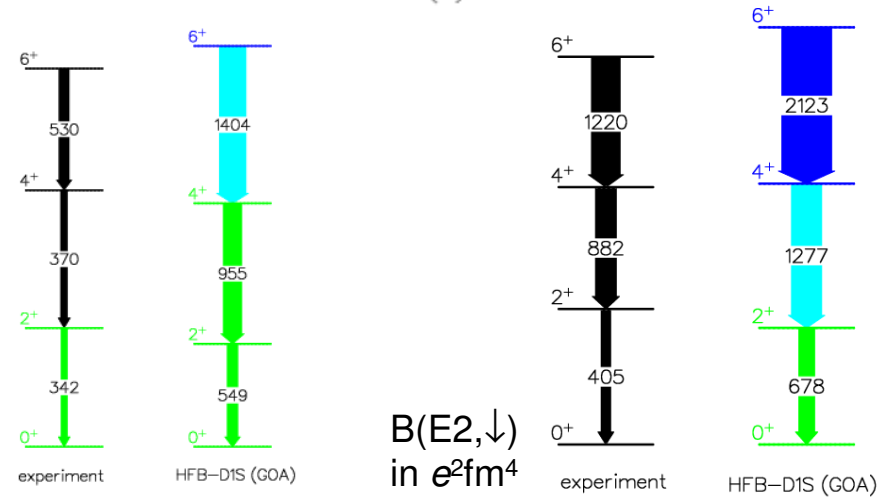
- **oblate** rotation prevails only in  $^{68}\text{Se}$   
 ⇒ best example for shape coexistence in  $A=70$  region
- experimental matrix elements and quadrupole moments needed for  $^{68}\text{Se}$



$Q_s$  from Gogny configuration mixing calculation



Andreas G3rger  $^{68}\text{Se}$



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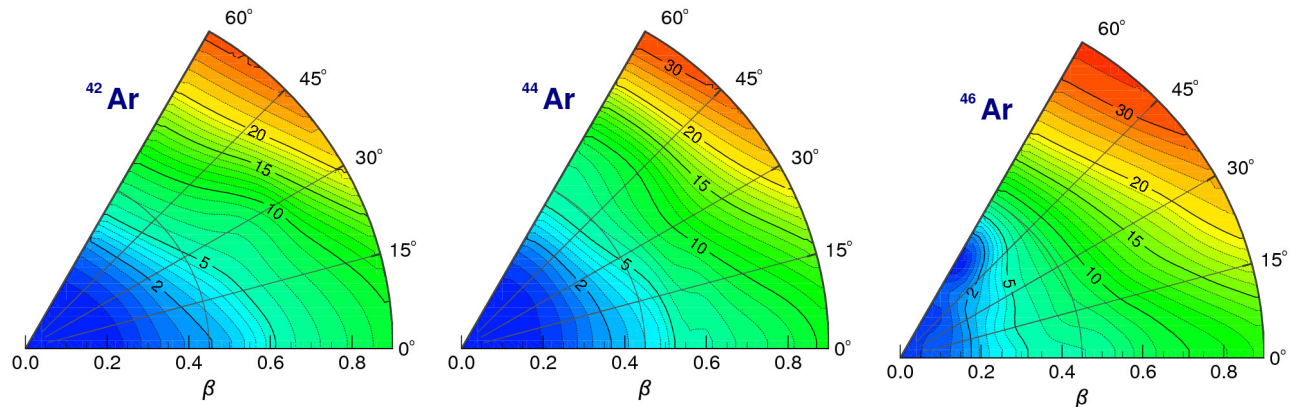
$^{70}\text{Se}$

1.-5.12.2008

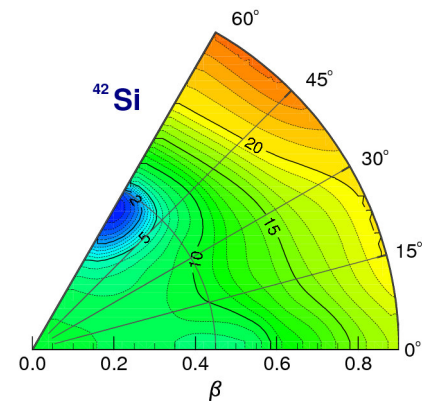
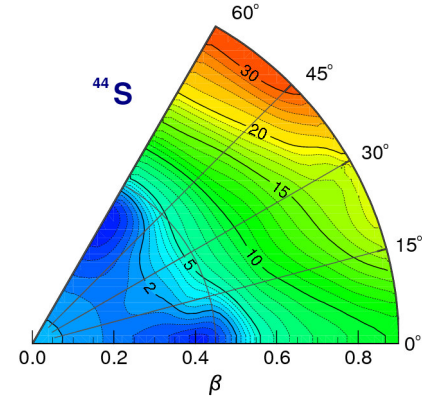
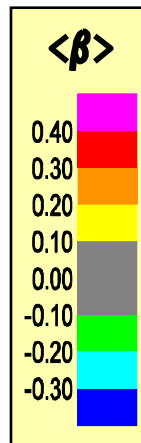
$^{72}\text{Se}$  12

$B(E2, \downarrow)$   
in  $e^2fm^4$

# Development of deformation for N=28 below $^{48}\text{Ca}$



20	Ca 40 96.94	Ca 42 0.65	Ca 44 2.08	Ca 46 0.003	Ca 48 0.19	Ca 50 13.9 s
18	Ar 38 0.07	Ar 40 99.59	Ar 42 32.9 y	Ar 44 11.9 m	Ar 46 8.4 s	Ar 48 0.48 s
16	S 36 0.015	S 38 170 m	S 40 8.8 s	S 42 1.01 s	S 44 123 ms	S 46 50 ms
14	Si 34 2.77 s	Si 36 0.45 s	Si 38 >1 $\mu\text{s}$	Si 40 33 ms	Si 42 13 ms	Si 44 10 ms
12	Mg 32 86 ms	Mg 34 20 ms	Mg 36 3.9 ms	Mg 38 >260 ns	Mg 40 1 ms	
	20	22	24	26	28	30



M. Girod  
Bruyères-le-Châtel

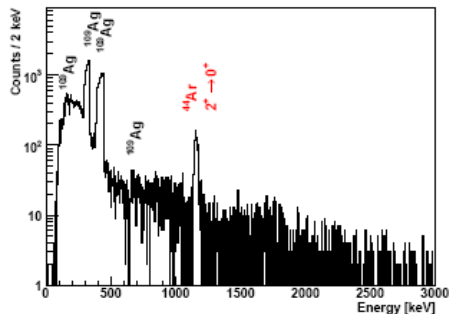
# Coulomb excitation of $^{44}\text{Ar}$ at SPIRAL

l r f u

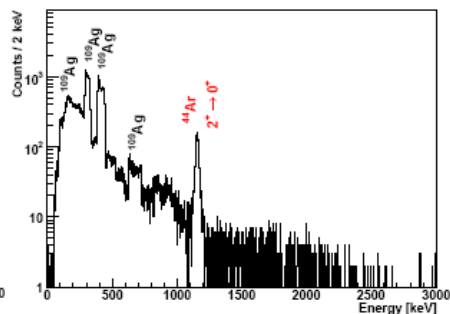


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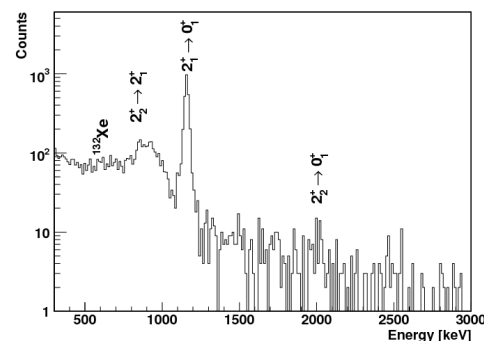
$^{109}\text{Ag}$  target,  $35^\circ < \theta_{\text{cm}} < 70^\circ$



$^{109}\text{Ag}$  target,  $70^\circ < \theta_{\text{cm}} < 130^\circ$

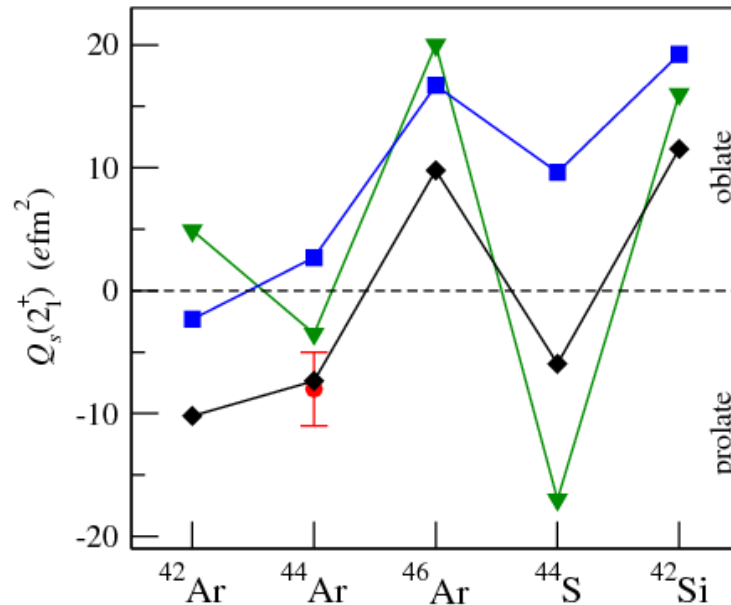
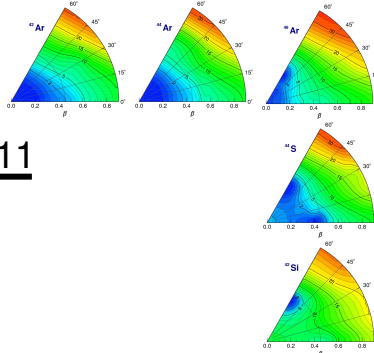
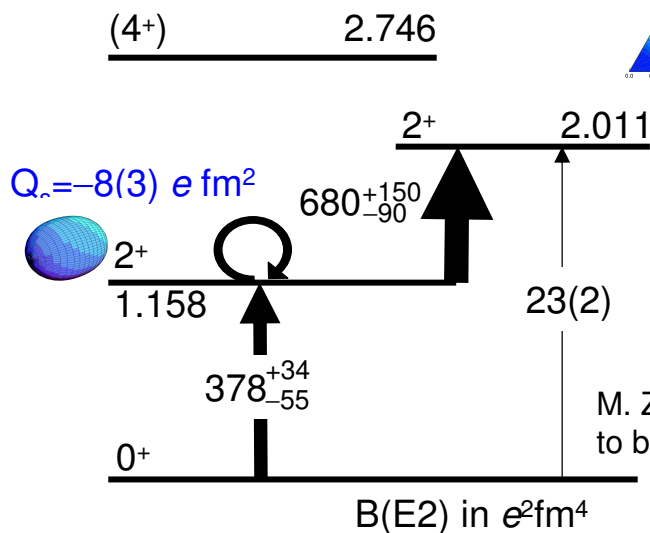


$^{208}\text{Pb}$  target,  $30^\circ < \theta_{\text{cm}} < 130^\circ$



- EXOGAM + DSSD
- SPIRAL beam  $^{44}\text{Ar}$
- $3 \cdot 10^5$  pps
- 2.7-A MeV on  $^{109}\text{Ag}$
- 3.7-A MeV on  $^{208}\text{Pb}$

- Experiment
- ▼ Shell Model
- AMPGCM (1D)
- ◆ GCM+GOA (5D)



SM : Retamosa et al. PRC 55, 1266 (1997)

Caurier et al. Nucl. Phys. A 742, 14 (2004)

AMPGCM: R. Rodríguez-Guzmán et al. PRC 65, 024304 (2002)

GCM(GOA)-5D: M. Girod

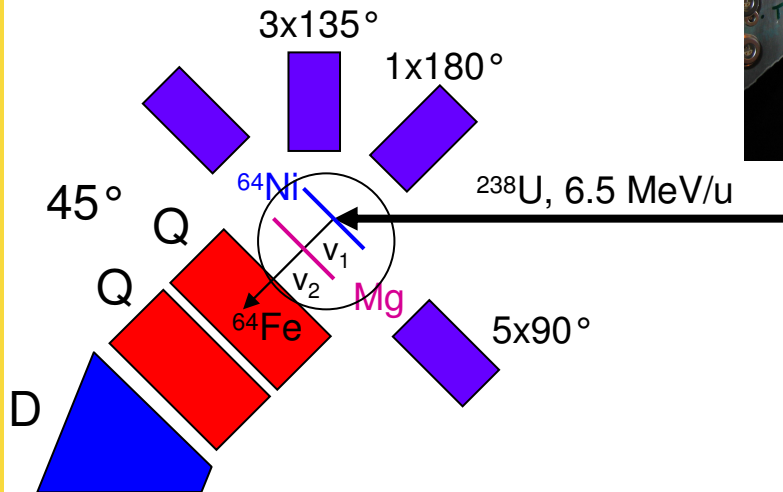
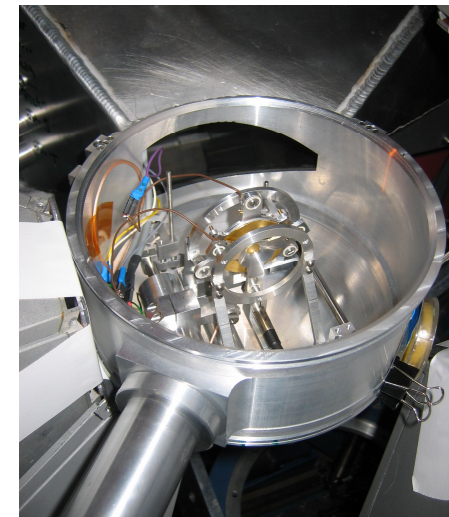
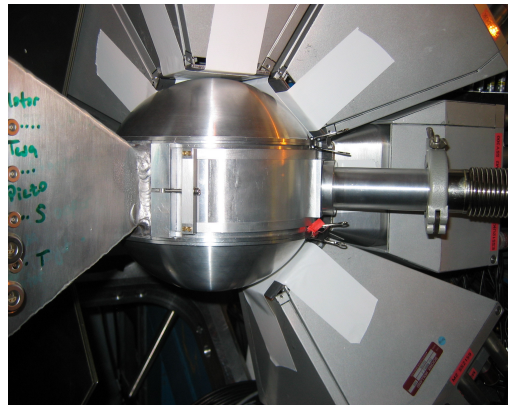
# Picosecond lifetimes in neutron-rich nuclei?


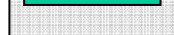
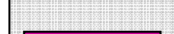


Multi-nucleon transfer  $^{238}\text{U} + ^{64}\text{Ni}$

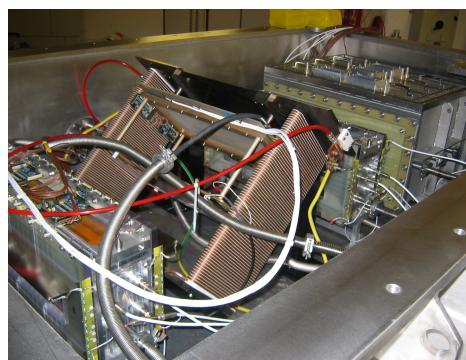
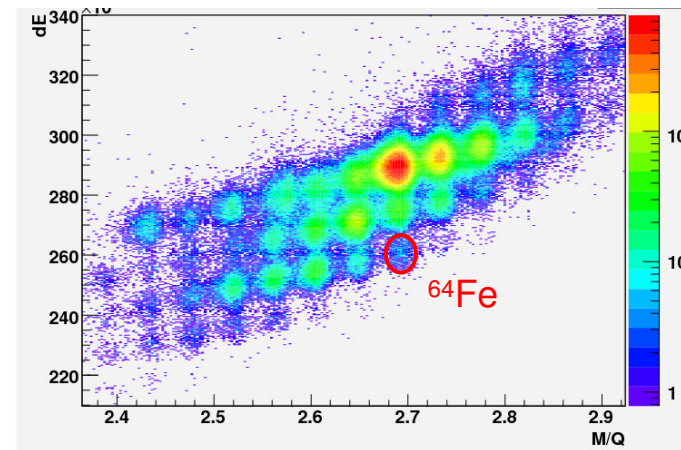
EXOGRAM

VAMOS

differential RDDS Plunger



-  drift chamber: x,y
-  Se-D: trigger,  $t_1$
-  drift chamber: x,y
-  ionisation chamber:  $\Delta E$
-  silicon wall: E,  $t_2$



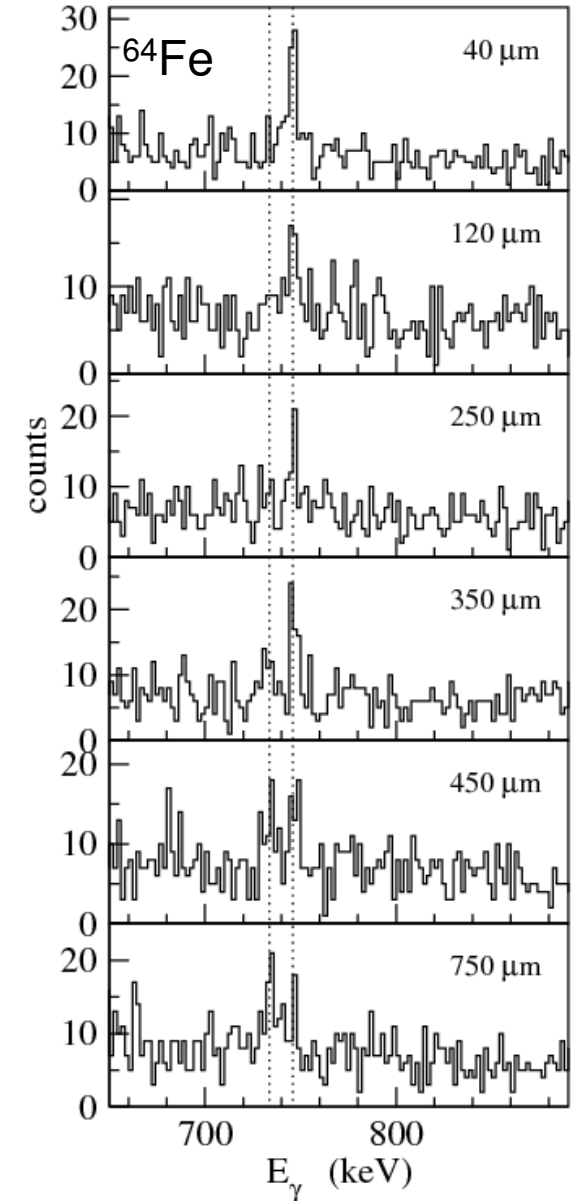
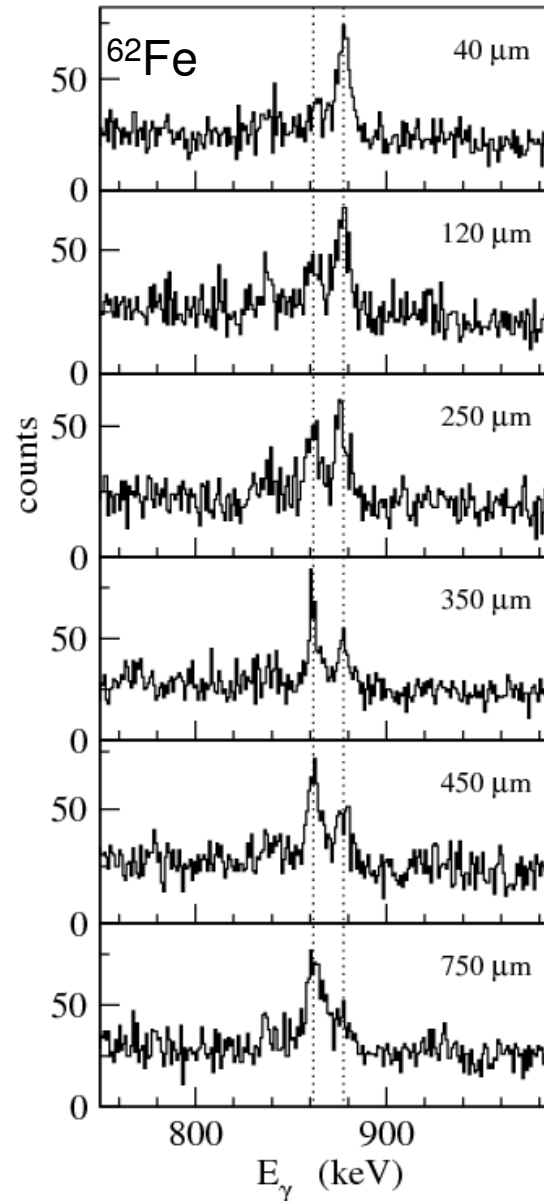
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## RDDS lifetimes in $^{62}\text{Fe}$ et $^{64}\text{Fe}$

- beam:  $^{238}\text{U}$  at 1547 MeV
  - target:  $^{64}\text{Ni}$ , 1.5 mg/cm<sup>2</sup>
  - degrader:  $^{\text{nat}}\text{Mg}$ , 5 mg/cm<sup>2</sup>
  - 6 distances 40 – 750  $\mu\text{m}$
- 
- new technique to measure picosecond lifetimes in neutron-rich nuclei
  - many more neutron-rich nuclides produced
  - many more lifetimes to be measured

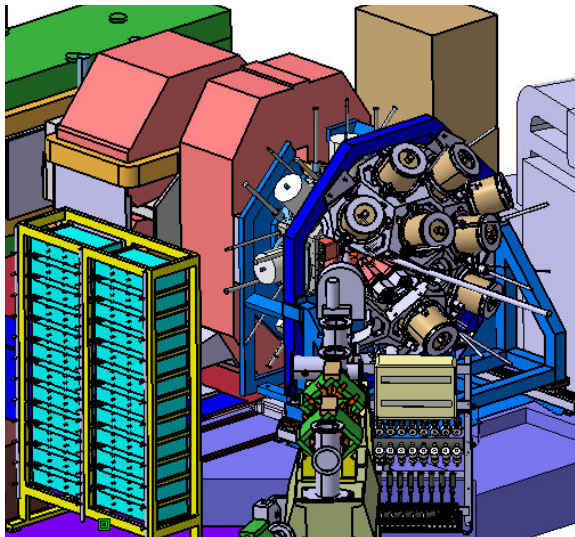




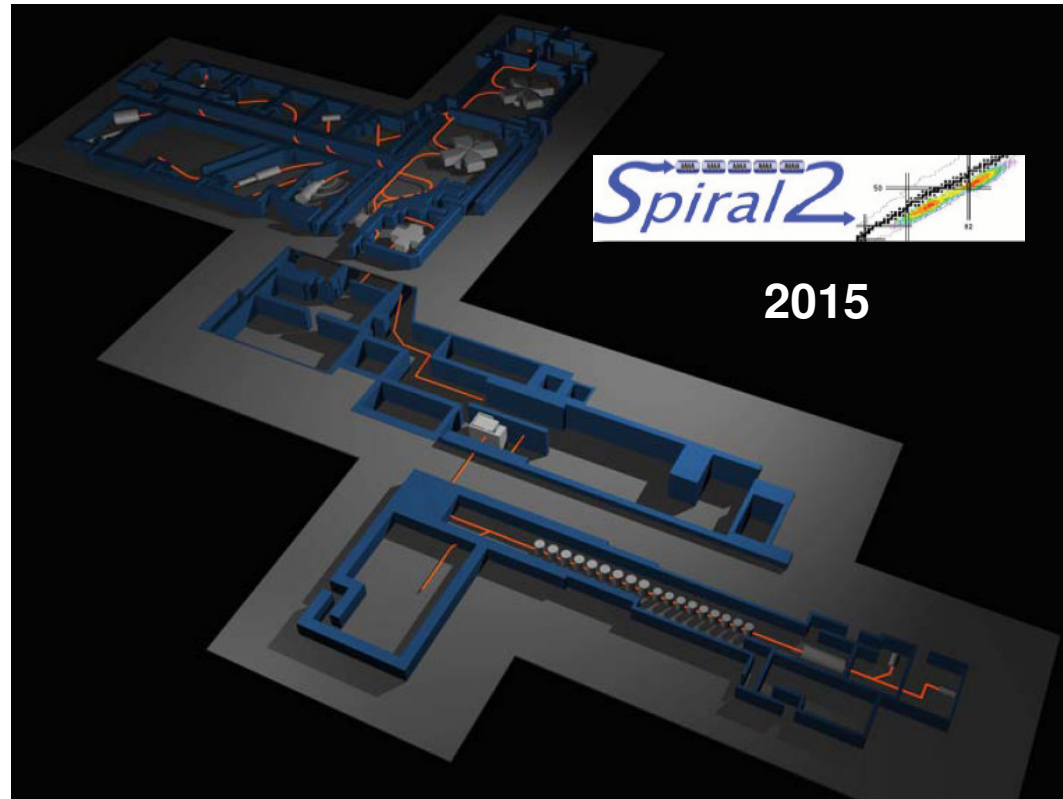
## Conclusions and Perspectives

- shape coexistence and evolution in Kr and Se near  $N=Z$
- onset of deformation and shape coexistence near  $N=28$
- nuclear shapes very sensitive to underlying nuclear structure
- quadrupole moments and transition rates as benchmarks for theory
- importance of triaxiality for GCM calculations
- complementary techniques
  - low-energy Coulomb excitation with RIB
  - RDDS lifetime measurements (fusion evaporation, multi-nucleon transfer)

2010



AGATA + EXOGAM + VAMOS



# Collaboration

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cea

saclay

## Coulomb excitation $^{74}\text{Kr}$ and $^{76}\text{Kr}$

Saclay: E. Clément, A. Görgen, W. Korten,  
E. Bouchez, A. Chatillon, A. Hürstel,  
Y. Le Coz, A. Obertelli, Ch. Theisen,  
J.N. Wilson, M. Zielińska  
Liverpool: C. Andreoiu, P.A. Butler, R.-D. Herzberg,  
D.G. Jenkins, G.D. Jones  
GSI: F. Becker, J. Gerl  
GANIL: J. M. Casandjian, G. de France  
Surrey: W. N. Catford, C.N. Timis  
Warsaw: T. Czosnyka, J. Iwanicki,  
P. Napiorkowski  
NBI: G. Sletten

## Lifetime measurement $^{74}\text{Kr}$ and $^{76}\text{Kr}$

Saclay: A. Görgen, E. Clément, A. Chatillon,  
W. Korten, Y. Le Coz, Ch. Theisen  
IKP Köln: A. Dewald, B. Melon, O. Möller, K.O. Zell  
Legnaro: N. Marginean, R. Menegazzo,  
D. Tonev, C.A. Ur

## Lifetime measurement $^{70}\text{Se}$ and $^{72}\text{Se}$

Saclay: J. Ljungvall, A. Görgen, C. Dossat, W. Korten,  
A. Obertelli, Ch. Theisen, M. Zielińska  
IKP Köln: A. Dewald, B. Melon, T. Pissulla, K.O. Zell  
Legnaro: R. Menegazzo, R. Orlandi, R.P. Singh,  
C.A. Ur, J.J. Valiente-Dobón  
Oslo: S. Siem  
Warsaw: J. Srebrny

## Coulomb excitation $^{44}\text{Ar}$

Saclay: M. Zielińska, A. Görgen, E. Clément,  
W. Korten, A. Bürger, C. Dossat,  
J. Ljungvall, A. Obertelli, Ch. Theisen  
Surrey: W. N. Catford  
Warsaw: J. Iwanicki, P. J. Napiorkowski,  
D. Pietak, J. Srebrny, K. Wrzosek  
NBI: G. Sletten

## Lifetime measurement $^{62}\text{Fe}$ and $^{64}\text{Fe}$

Saclay: J. Ljungvall, A. Obertelli,  
A. Görgen, W. Korten  
GANIL: E. Clément, G. de France, A. Navin,  
M. Rejmund, S. Aradhana  
CEA/DIF: L. Gaudefroy  
IKP Köln: A. Dewald, M. Hackstein,  
T. Pissulla, W. Rother, K.O. Zell  
Legnaro: D. Mengoni, F. Recchia, E. Sahin,  
J.J. Valiente-Dobón  
Valencia: A. Gadea  
Oslo: A. Bürger  
Warsaw: M. Zielińska

## Theory:

CEA/DIF: M. Girod, J.-P. Delaroche