

Cluster productions in intermediate-energy proton-nucleus reactions

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Tenaya Lodge at Yosemite

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Actual Condition of Intranuclear Cascade Model

➤ Conventional intranuclear cascade (INC) models

✓ Neutron and proton productions

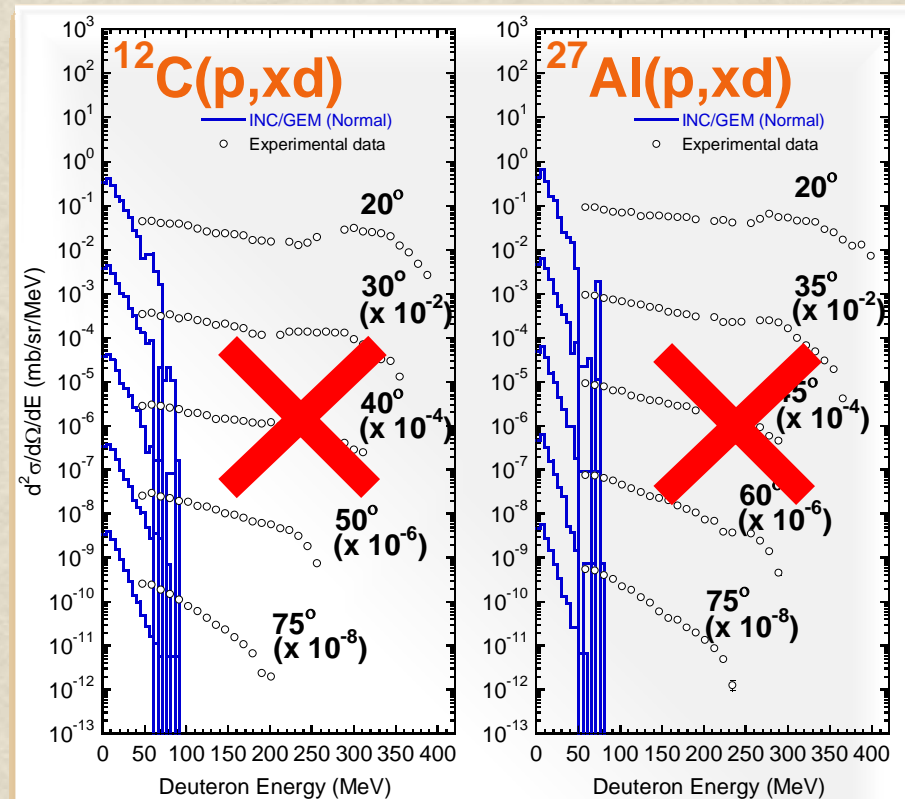


PREDICTABLE!

✓ Cluster productions



UNPREDICTABLE!



392 MeV proton induced
DEUTERON production DDXs

Mechanism of Cluster Productions

➤ P.E. Hodgson and E. Betak, *Phys. Rep.* 374, 1-89 (2003)

“The mechanisms of cluster reactions show special features such as the competition between *pickup* and *knockout* processes and the contributions of several successive steps in the reaction.”

➤ C. Kalbach, *Phys. Rev. C* 71, 034606 (2005)

Pre-equilibrium exciton model (below about 100 MeV, phenomenological)
with *pickup* plus *knockout*

It is necessary to introduce both *knockout* mechanism and *pickup* mechanism into the INC model as well as the exciton model.

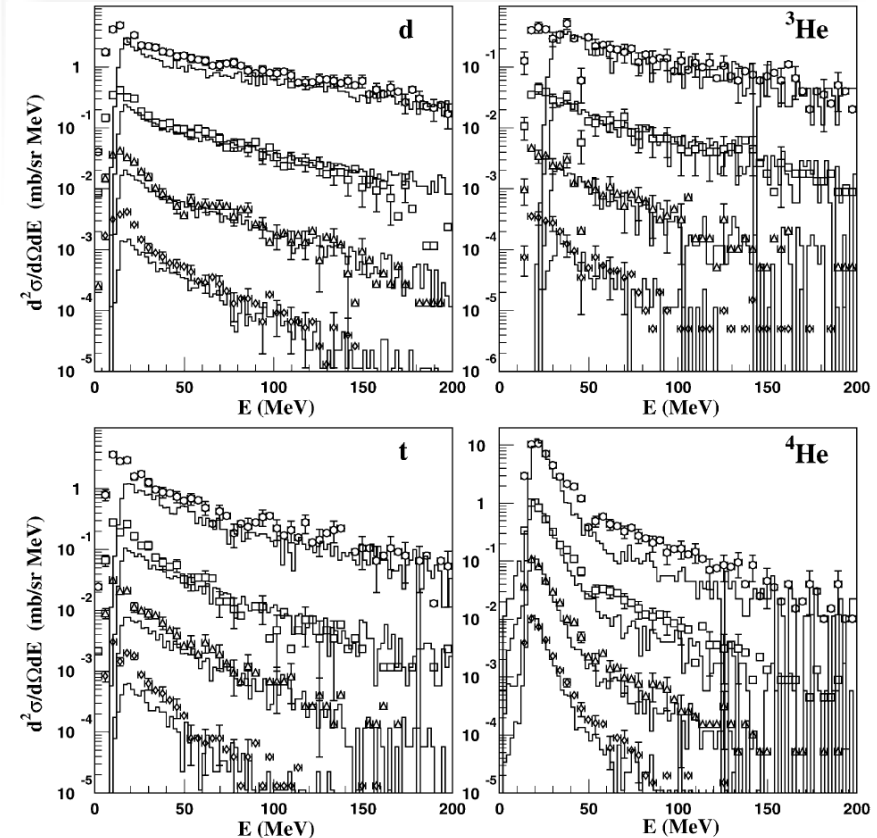
Cluster productions (INC model)

- ◆ Liège INC model
+ surface coalescence*



PREDICTABLE?

It is necessary to introduce "knockout" in addition to surface coalescence (pickup) into INC model.



p(2.5 GeV) + Au reaction

*) Boudard, et al. Nucl. Phys. A 740 (2004) 195-210

Purpose of This Study

Introduce cluster production mechanism (*pickup (surface coalescence)* + *knockout*) within the framework of the INC model and investigate their applicability.

In terms of “*knockout*” mechanism, we implement it into the INC model in our own original way.

Our INC code

INC model

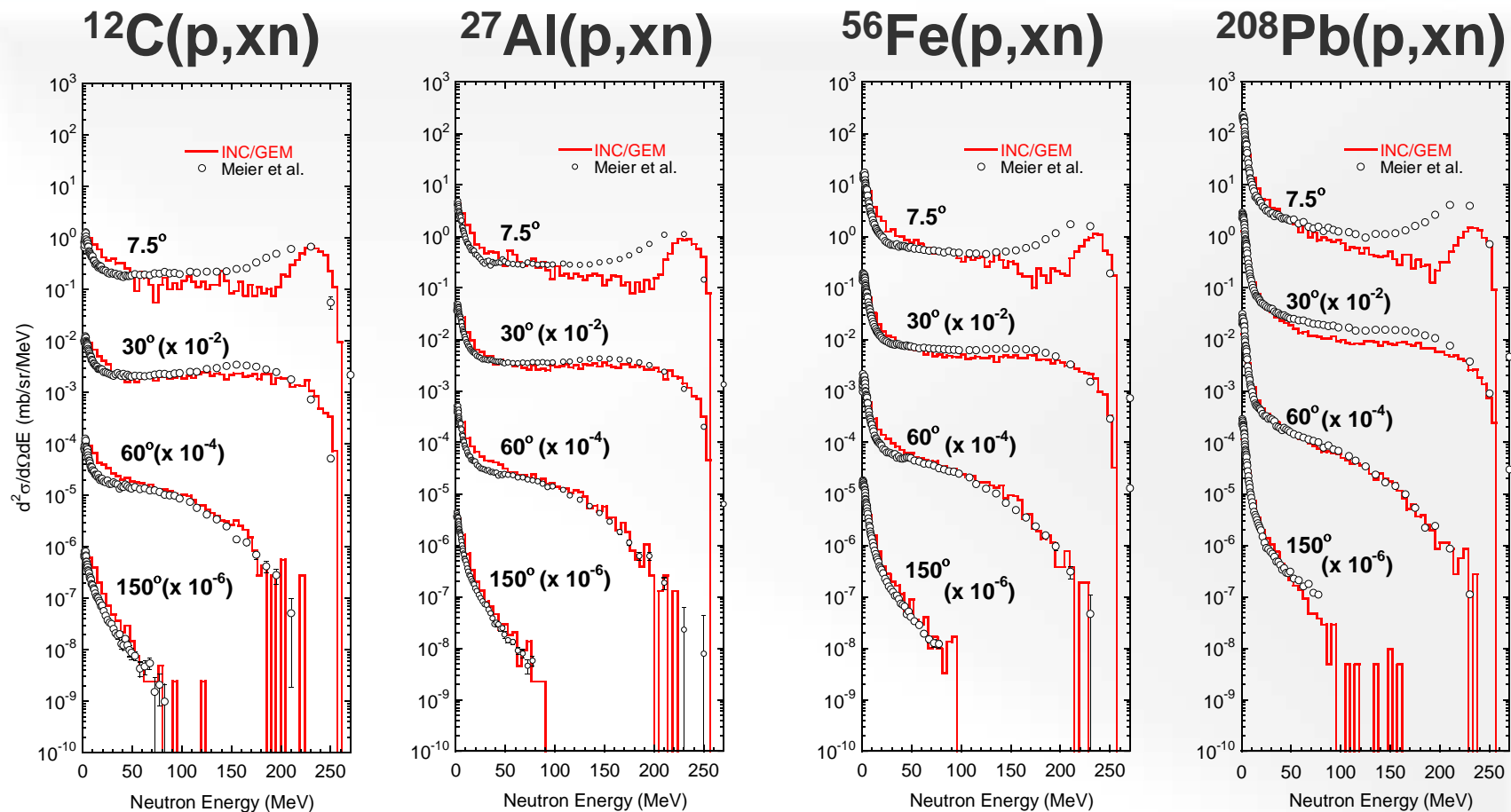
Equation of Motion — Newtonian equation without interaction

Target — Potential: Square well potential
Spatial dist.: Wood-Saxon dist.
(Negele's systematics)
Momentum dist.: Uniform Fermi gas dist.

NN elastic cross section — Cugnon's systematics
Angular distribution

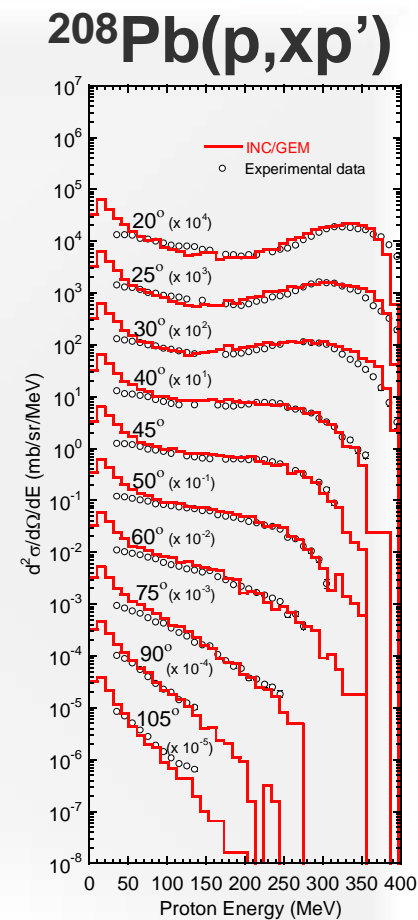
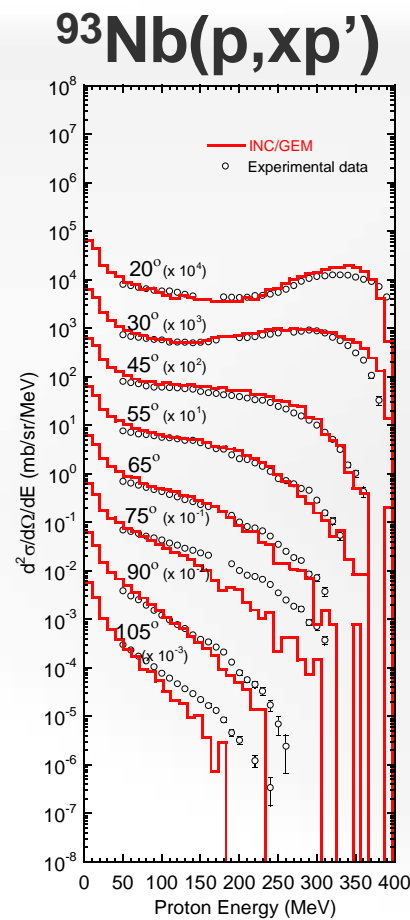
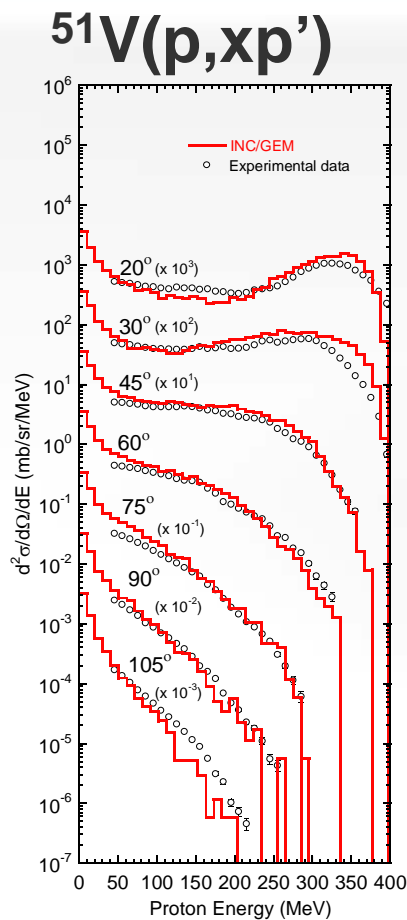
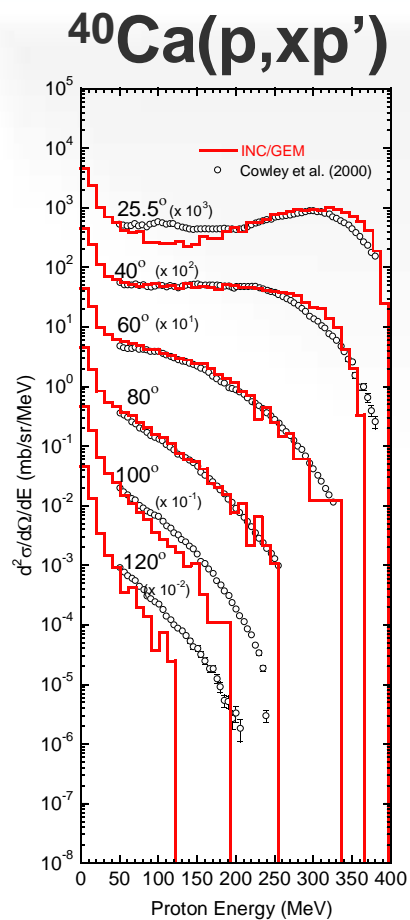
Evaporation stage calculation — GEM code (developed by Furihata)

Comparison with Experimental Data (1)



256 MeV proton induced **NEUTRON** production double-differential cross sections

Comparison with Experimental Data (2)

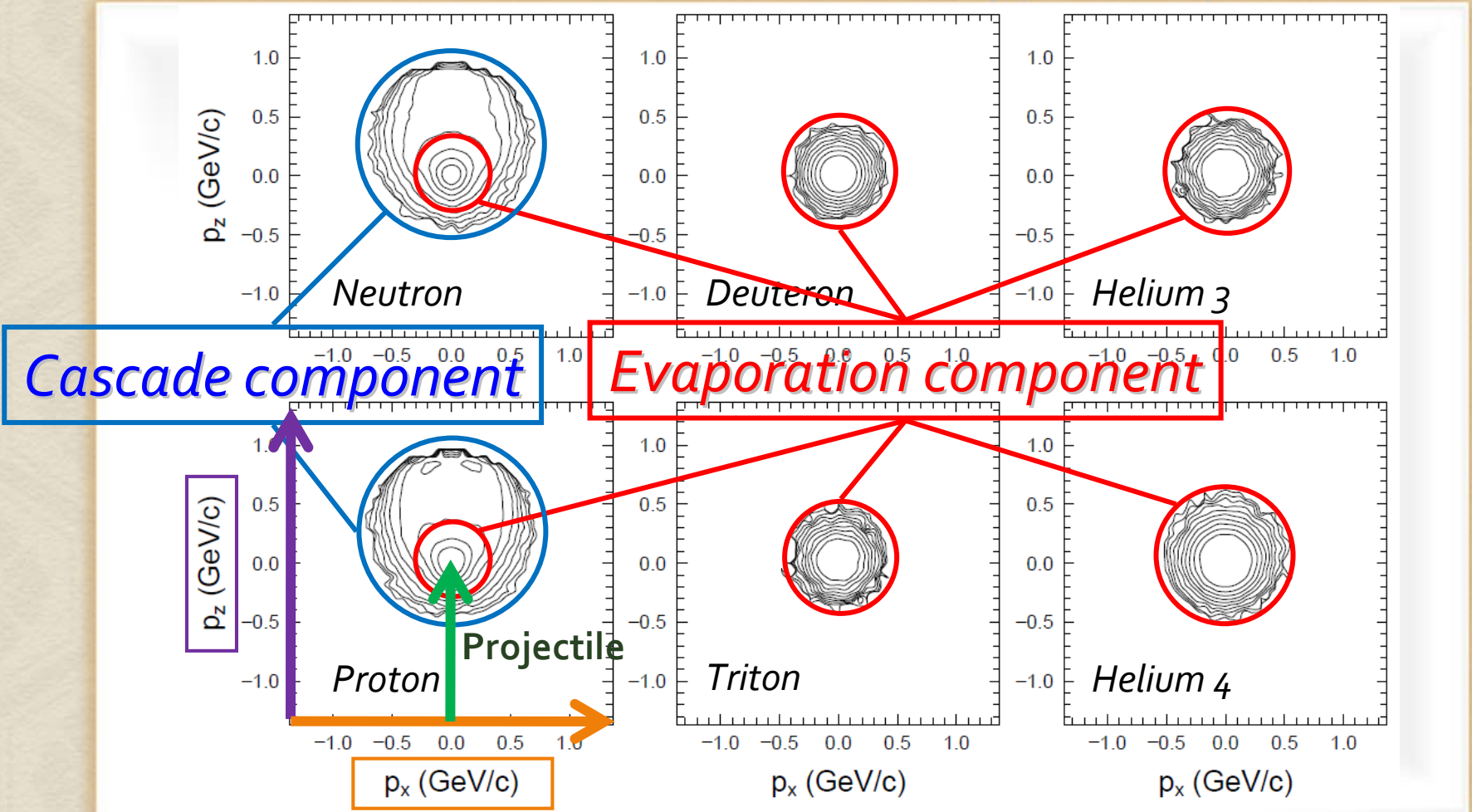


392 MeV proton induced **PROTON** production double-differential cross sections

Contour Plot of Momentum distributions of Secondary Particles

INC + GEM

p(392 MeV) + ^{27}Al reaction



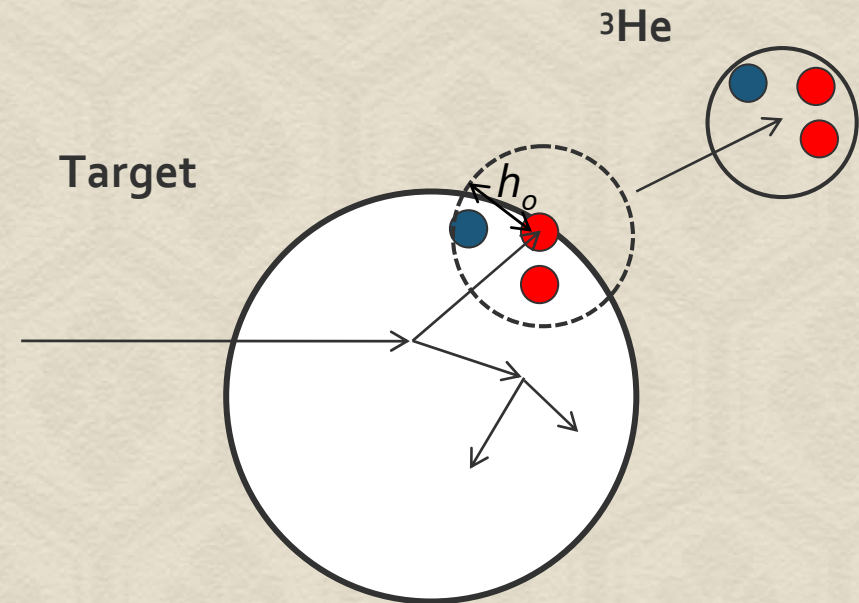
Mechanism of Cluster Productions (1)

□ Surface Coalescence* (pickup)

When a nucleon is ready to get across and leave the nuclear surface, it picks up nucleons and they form a cluster.

✓ Conditional expression

$$r_{ij} p_{ij} < h_0, \quad (h_0 = 1800 \text{ fm MeV}/c)$$



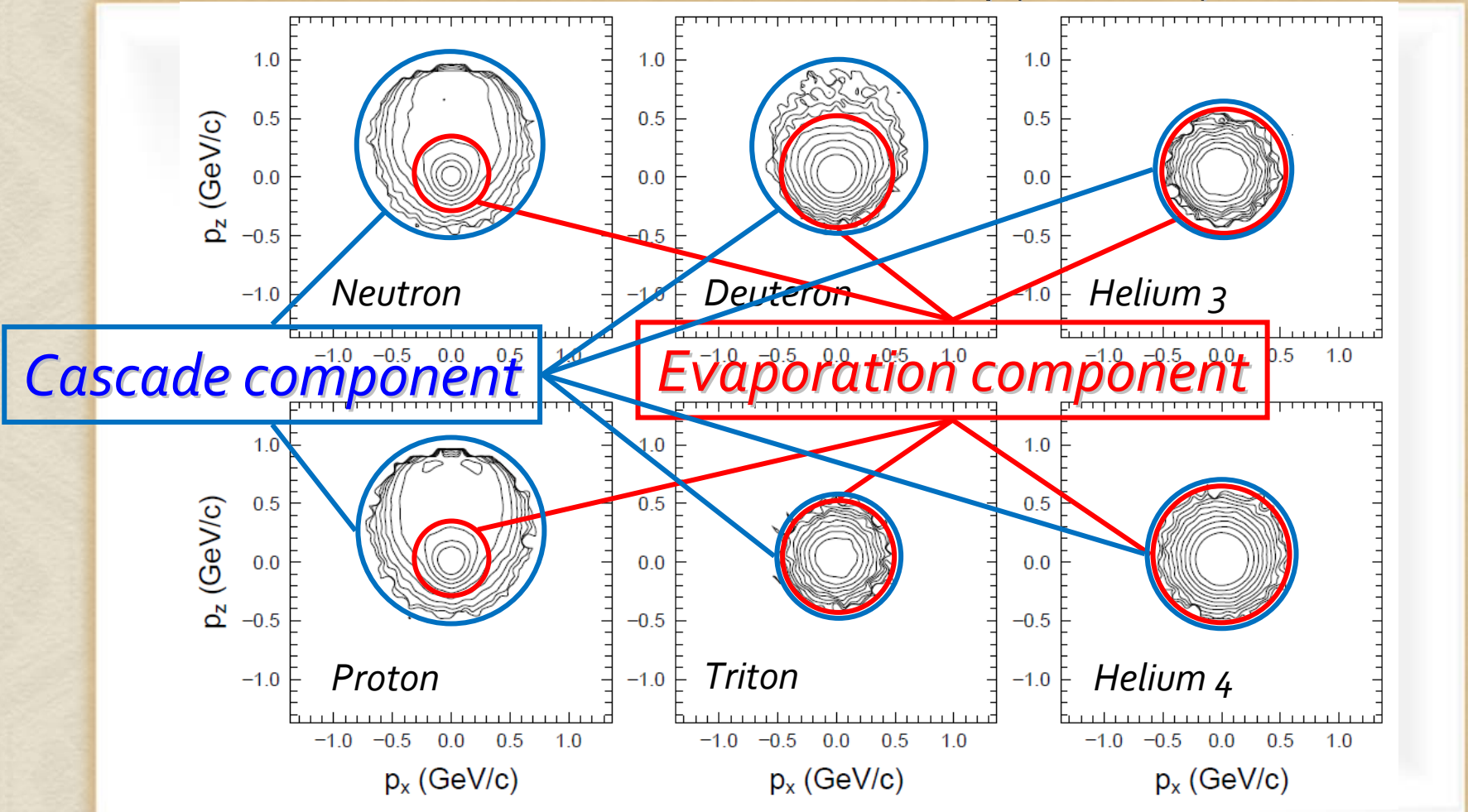
Schematic representation of the *surface coalescence* mechanism

*) A. Boudard, *et al. Nucl. Phys. A* 740 (2004) 195-210

Contour Plot of Momentum Distribution of Secondary particles

INC with **Surface Coalescence** + **GEM**

p(392 MeV) + ^{27}Al reaction



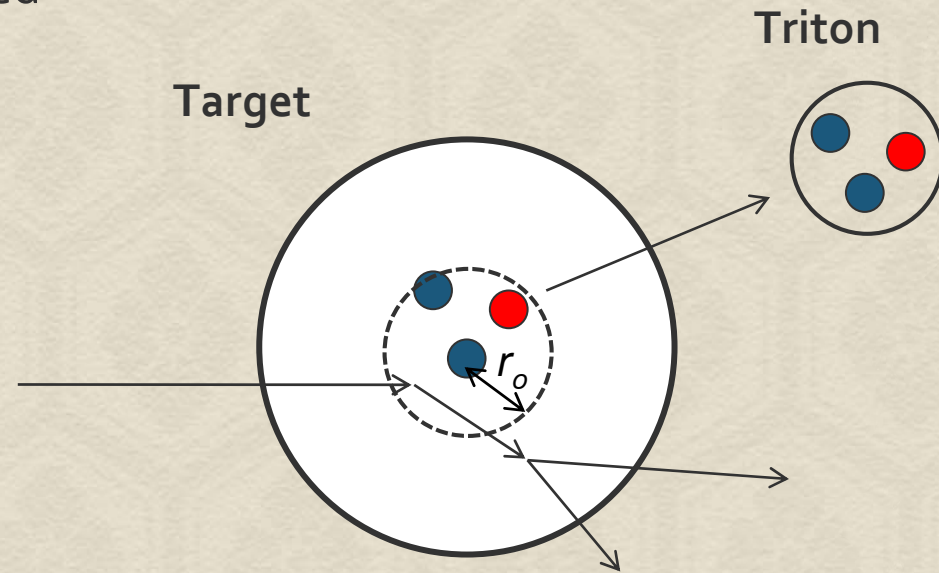
Mechanism of Cluster Productions (2)

□ Knockout

If there are nucleons near the bombarded nucleon, the scattering is regarded as *nucleon-cluster elastic scattering*.

✓ Conditional expression

$$\underline{r_{ij} < r_0, \quad (r_0 = 1.2 \text{ fm})}$$

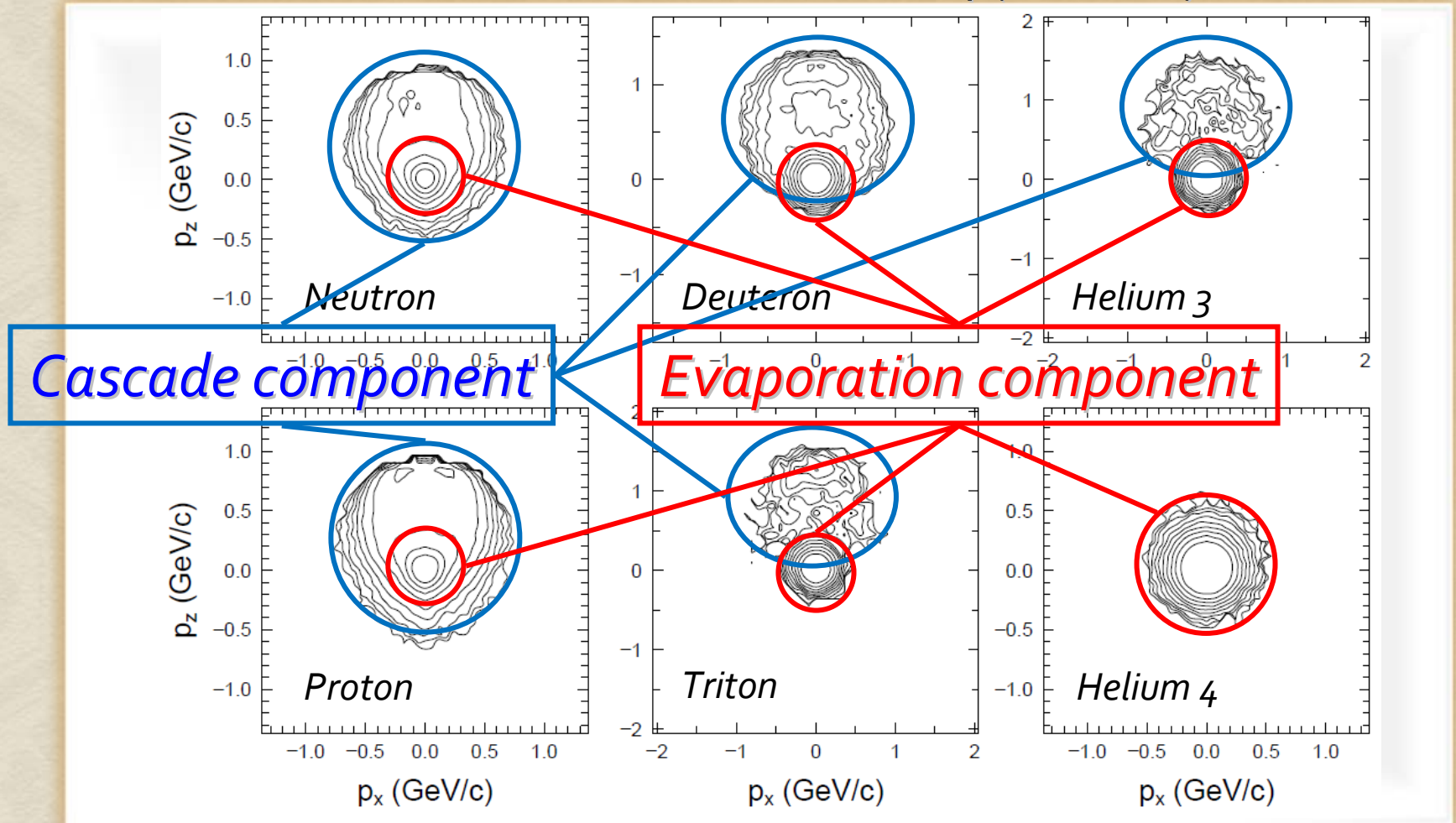


Schematic representation of
The knockout mechanism

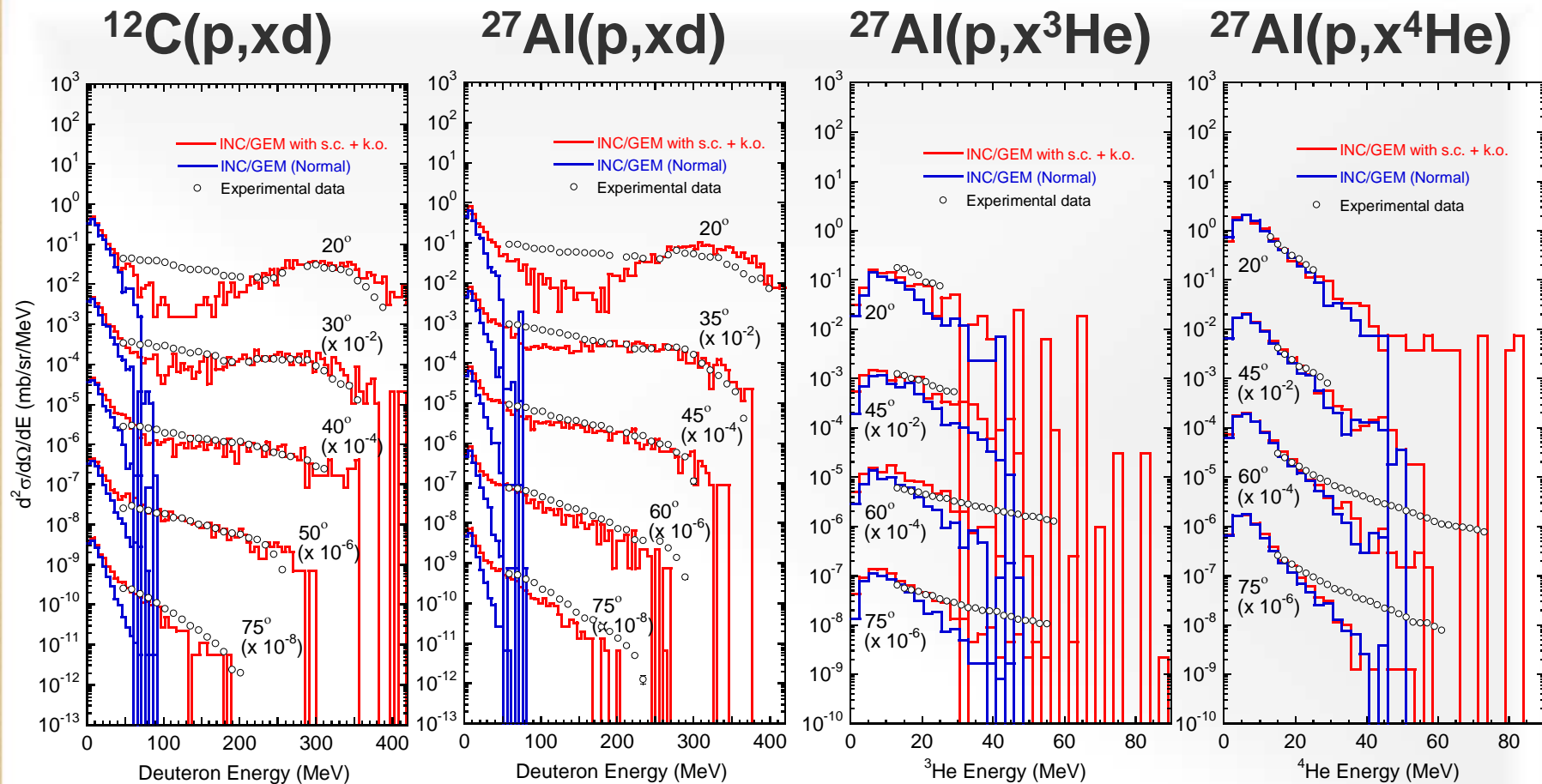
Contour Plot of Momentum distribution of Secondary Particles

INC with **Knockout** + **GEM**

p(392 MeV) + ^{27}Al reaction



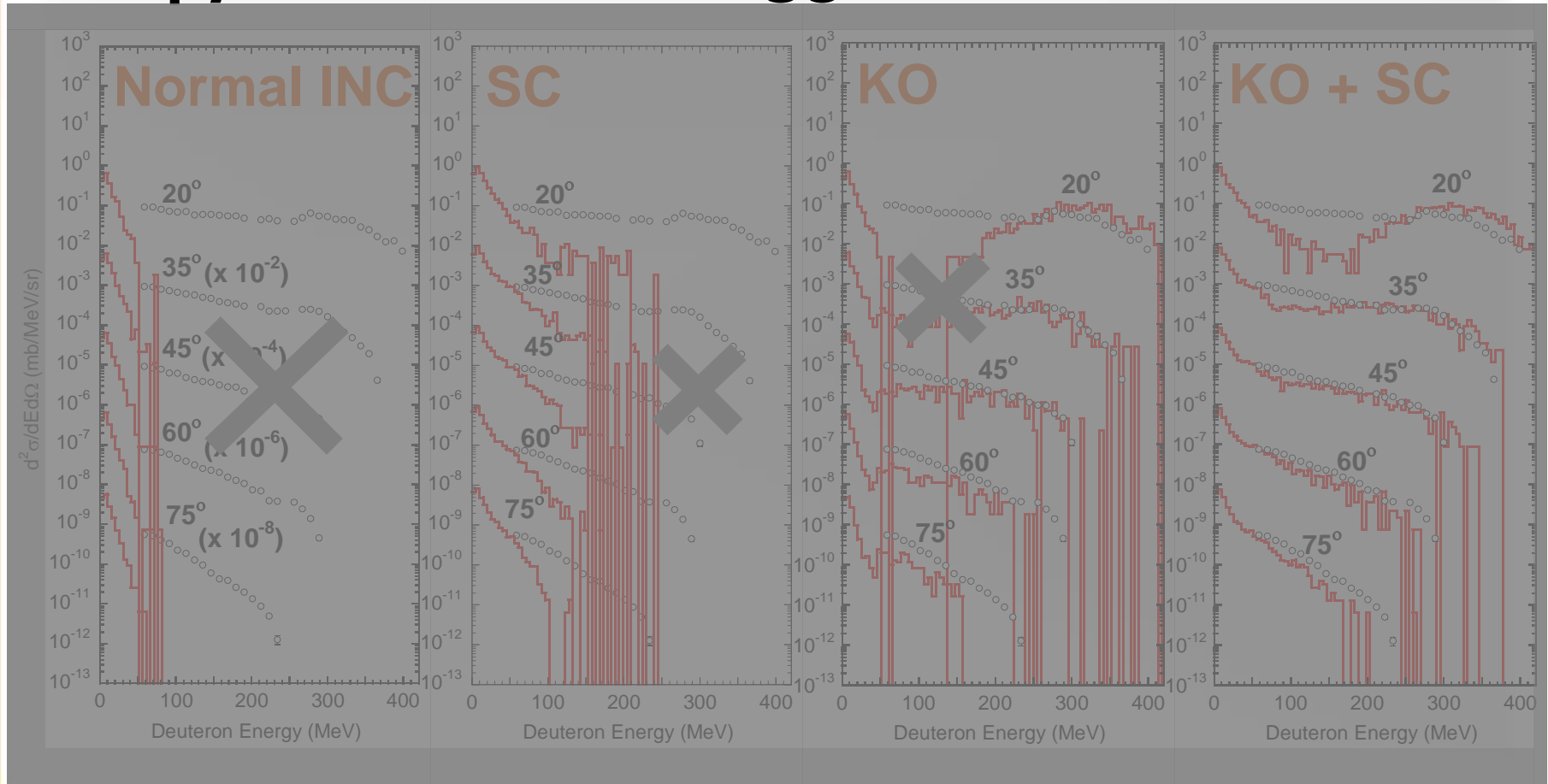
Comparison with Experimental Data (3)



392 MeV proton induced **CLUSTER** production double-differential cross sections

Contribution of Each Mechanism

$^{27}\text{Al}(p,xd)$ reaction at 392 MeV



Summary and Conclusion

- ◆ We developed a nuclear reaction code based on the intranuclear cascade (INC) model which describe not only nucleon productions but also cluster productions.
- ◆ It was found that combination of *surface coalescence(pickup)* plus *knockout* is effective to describe cluster productions .

Outline

- ◆ Motivation & Background

 - Early studies and technical issues

- ◆ Theory & our code

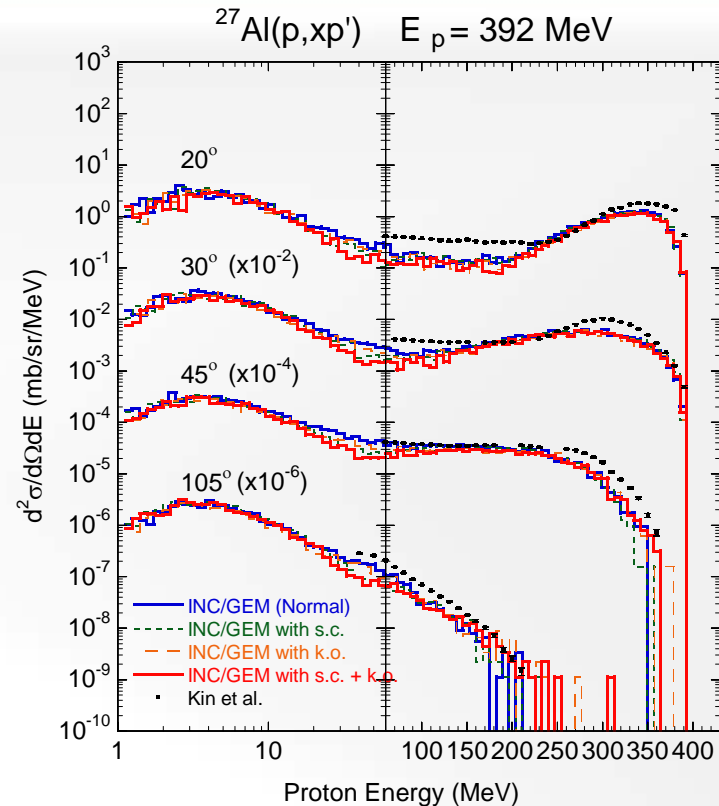
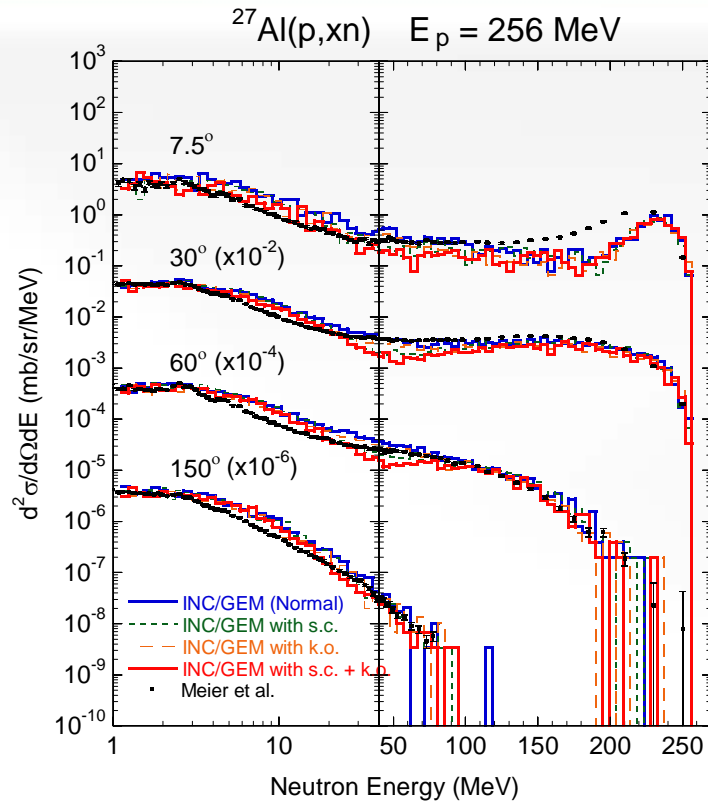
 - Description of our intranuclear cascade model and cluster production mechanism

- ◆ Results

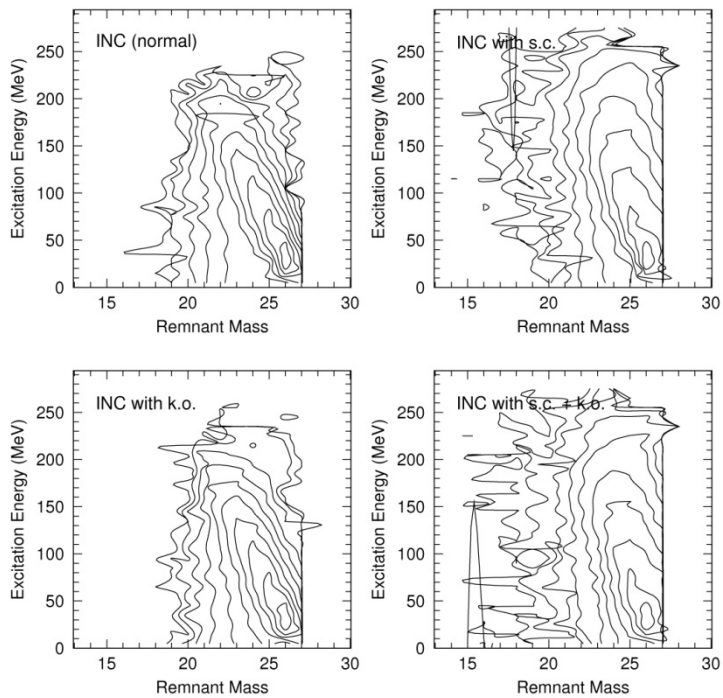
 - Comparison with experimental data

- ◆ Summary

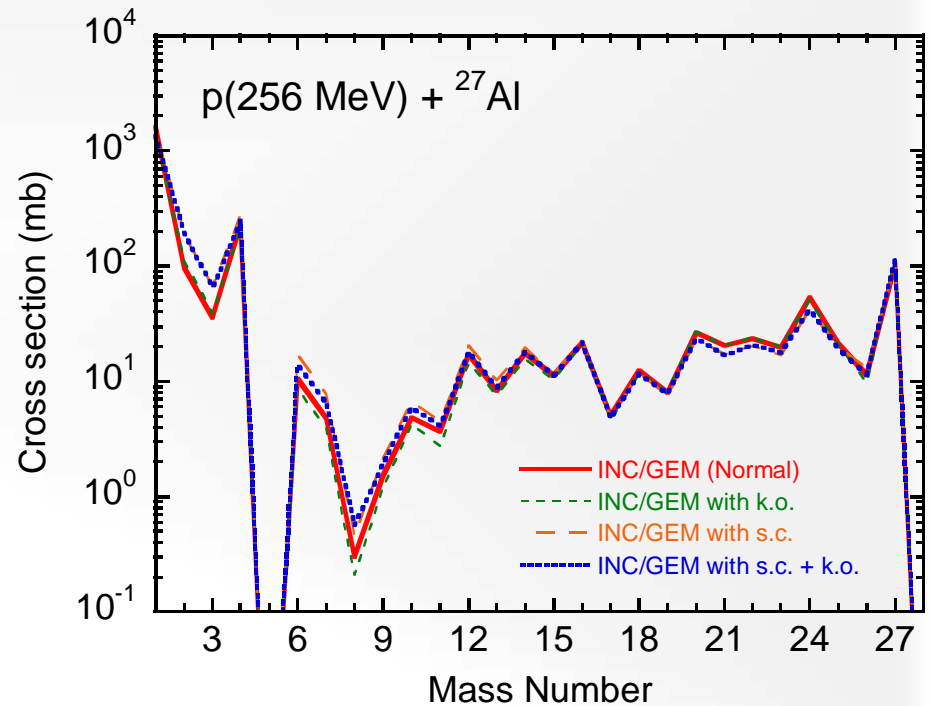
Influence upon Nucleon Production Spectra



Introduction of cluster production mechanism does not affect nucleon production spectra.



Remnant mass-excitation energy distribution



Mass distribution of residual nuclei

Kinematics of the Knockout

N - AN elastic scattering

Relative momentum in the center-of-momentum system

$$\mathbf{p}_{\text{cm}} = \mathbf{p}_{\text{proj}} + \beta T \quad \text{with} \quad T = \gamma \left(\gamma \frac{\mathbf{p}_{\text{proj}} \cdot \beta}{\gamma + 1} - E_{\text{proj}} \right)$$

where

$$\beta = \frac{\mathbf{p}_{\text{proj}} + \mathbf{p}_{\text{clust}}}{E_{\text{proj}} + E_{\text{clust}}}, \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}},$$

$$\mathbf{p}_{\text{clust}} = \sum_{i=1}^{A_{\text{clust}}} \mathbf{p}_i \quad E_{\text{clust}} = \sqrt{p_{\text{clust}}^2 + (A_{\text{clust}} m)^2},$$

Kinetic energy of the cluster

Sum of momenta of
constituent nucleons

$$T_{\text{clust}} = -A_{\text{clust}} m + \sqrt{p_{\text{clust}}^2 + (A_{\text{clust}} m)^2} + V_0$$

Kinematics of the Surface Coalescence

Kinetic energy of the cluster outside the target nucleus

$$T_{\text{clust}} = -A_{\text{clust}} m + \sqrt{p_{\text{clust}}^2 + (A_{\text{clust}} m)^2} + A_{\text{clust}} V_0 \quad \text{+ binding energy?}$$

with

$$\mathbf{p}_{\text{clust}} = \sum_{i=1}^{A_{\text{clust}}} \mathbf{p}_i \quad \text{+ intrinsic momentum?}$$

